Hydrate Phase Equilibria Study of CO2 Containing Gases in Thermodynamic Promoter Aqueous Mixtures
Veronica Belandria

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Etude Expérimentale des Equilibres d’hydrates de Mélanges de Gaz Contenant du CO₂ en Solutions Aqueuses de Promoteur Thermodynamique

Hydrate Phase Equilibria Study of CO₂ Containing Gases in Thermodynamic Promoter Aqueous Mixtures

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Chapter 4: Development of a New Apparatus for Simultaneous Measurements of Gas Hydrates Dissociation Conditions and Compositional Analysis

4.1 Introduction

4.2 Apparatus
   4.2.1 Equilibrium cell
   4.2.2 Sample supplying system
   4.2.3 Composition analyzing system
   4.2.4 Measurement, control and acquisition of temperature and pressure

4.3 Experimental Procedure
   4.3.1 Preparation of the feed
   4.3.2 Fluids supply to the equilibrium cell
   4.3.3 Isochoric Pressure Search Method

4.4 Results and discussion

Chapter 5: Thermodynamic Stability of Hydrates from Gas Mixtures Containing CO₂

5.1 Introduction

5.2 Gas Hydrate Formation in Carbon Dioxide + Nitrogen + Water Systems
   5.2.1 Equilibrium Dissociation Conditions
   5.2.2 Compositional Analysis of Equilibrium Phases

5.3 Study of Gas Hydrate Formation in (Carbon Dioxide + Hydrogen + Water) Systems
   5.3.1 Equilibrium Dissociation Conditions
   5.3.2 Compositional Analysis of Equilibrium Phases

Chapter 6: Thermodynamic Stability of Semi-Clathrate Hydrates

6.1 Phase Equilibria of Semi-Clathrate Hydrates of Carbon Dioxide, Methane and Nitrogen in Non-Stoichiometric TBAB Aqueous Solutions

6.2 Thermodynamic Properties of Semi-Clathrate Hydrates of (Carbon Dioxide + Nitrogen) Gas Mixtures in TBAB Aqueous Mixtures
   6.2.1 Phase Equilibrium Measurements for Semi-Clathrate Hydrates of the CO₂ + N₂ + Tetra-n-Butylammonium Bromide Aqueous Solution Systems
   6.2.2 Compositional Properties for Semi-Clathrate Hydrates of the CO₂ + N₂ + Tetra-n-Butylammonium Bromide Aqueous Solution Systems

Chapter 7: Conclusions and Outlook

7.1 Conclusions

7.2 Outlook

References

Acknowledgements

Curriculum Vitae

Publications

Appendix A: Measured Hydrate Phase Equilibrium Data for CO₂ Containing Gases

Appendix B: Tetra-n-Butyl Ammonium Bromide + Water Systems: Density Measurements and Correlation
List of Figures

1.1 Worldwide CO$_2$ industrial emissions and economic recessions in the past 50 years .................. 13
1.2 Carbon dioxide hydrates phase equilibrium in CO$_2$ + water system ................................. 15
1.3 Hydrate crystal unit structures: sI, sII and sH ............................................................... 23
1.4 Typical phase diagram for pure water .................................................................................. 26
1.5 Pressure-temperature diagram for methane + water system in the hydrate region ............. 27
1.6 Pressure-temperature phase diagram for hydrocarbon + water systems .......................... 28
1.7 Pressure-temperature phase diagram for multicomponent natural gas systems ................. 28
1.8 Carbon dioxide hydrate phase boundary compared to nitrogen, hydrogen and methane ......... 31
1.9 Flow diagram of a hydrate-based CO$_2$ recovery process ................................................. 33
1.10 Flow diagram of an integrated cryogenic and hydrate CO$_2$ capture process ...................... 33
1.11 Conceptual separation stages required for recovering CO$_2$ from (CO$_2$ + N$_2$) hydrates ....... 34
1.12 Promotion effect of various quaternary ammonium salts on the phase equilibrium conditions of CO$_2$ clathrate hydrates .............................................................. 38
1.13 TBAB semi-clathrate structure .......................................................................................... 39
1.14 Temperature-composition phase diagram of (TBAB + H$_2$O) semi-clathrates under atmospheric pressure, as reported by Arjmandi and coworkers (2007). Symbols represent experimental data and figures along the composition lines stand for hydration numbers ................................. 40
1.15 Carbon dioxide + TBAB semi-clathrates phase boundary ................................................ 40
2.1 Process design strategy ........................................................................................................ 47
2.2 Detail of Deaton and Frost’s hydrate formation equilibrium cell ........................................ 53
2.3 (a) Schematic diagram of the QCM, and (b) the QCM mounted within a high pressure cell ........ 54
2.4 High-pressure micro DSC VII measurement device .......................................................... 55
2.5 Hydrate dissociation conditions (HDC) determination following the isochoric pressure-search method .......................................................... 58
2.6 Front view of the gas chromatograph used in this work and main components ..................... 59
2.7 Gas chromatogram exhibiting an effective separation of a (CO$_2$ + N$_2$) gas mixture .......... 60
2.8 Calibration devices used in this work .................................................................................. 61
2.9 Relative uncertainty on pressure transducers calibration ................................................... 62
2.10 Pt-100 Platinum resistance thermometer probe calibration ................................................. 64
2.11 Thermal conductivity detector calibration .......................................................................... 66
2.12 Refractive index calibration for TBAB aqueous solutions .................................................. 67
2.13 Chromatogram profile for a (CO$_2$ + N$_2$) gas mixture in the presence of TBAB aqueous solution ................................................................. 68
3.1 Flow diagram of the experimental setup ............................................................................... 73
3.2 Partial pictures of the apparatus .......................................................................................... 74
3.3 Representative isochoric curve, and pressure and temperature plots obtained during a hydrate formation/dissociation experiment .................................................. 76
3.4 Experimental dissociation pressures for methane simple hydrates ..................................... 77
3.5 Experimental dissociation pressures for carbon dioxide simple hydrates ......................... 77
3.6 Experimental dissociation pressures for various (methane + carbon dioxide) gas hydrates at different CO$_2$ load mole fractions ......................................................... 78
3.7 Relative deviation of experimental dissociation pressures for (CO$_2$ + CH$_4$) clathrate hydrates and predictions of HWHYD thermodynamic model ............................................... 80
3.8 Experimental, calculated (using eq. 3.2) and predicted (HWHYD model) dissociation pressures for (CO$_2$ + CH$_4$) clathrate hydrates .......................................................... 81
3.9 Relative deviation of the experimental and predicted (HWHYD model) dissociation pressures for various (CO$_2$ + CH$_4$) clathrate hydrates ......................................................... 82
3.10 Relative deviation of experimental and calculated pressures (using eq. 3.2) dissociation pressures for (CO$_2$ + CH$_4$) clathrate hydrates .......................................................... 83
3.11 Experimental dissociation conditions for various (CO$_2$ + CH$_4$) clathrate hydrates and predictions of the thermodynamic model (HWHYD, 2000), at different CO$_2$ mole fractions loaded .................................................................................. 84
3.12 Comparison of experimental dissociation pressures for various \((\text{CO}_2 + \text{CH}_4)\) clathrate hydrates with the calculated values using eq. (3.2) ................................................................. 85
4.1 Schematic flow diagram of the new apparatus .......................................................................................... 93
4.2 Partial pictures of the main components of the new apparatus ............................................................... 93
4.3 Cross section of the equilibrium cell and photograph of equilibrium cell on its aluminum support ........ 94
4.4 (a) Lateral section of the equilibrium cell (b) Detail of the protection grid for the capillary sampler. ........ 95
4.5 (a) Lateral and (b) cross sections of the grid support. ............................................................................. 96
4.6 Chromatogram profile for nitrogen gas samples under gas-hydrate-liquid water equilibrium ............... 97
4.7 Flow diagram of the electromagnetic rapid on-line sampler-injector .................................................... 98
4.8 Layout for chromatograms acquisition using Winilab III software ...................................................... 99
4.9 Layout for temperature and pressure data acquisition software .......................................................... 100
4.10 Hydrate formation/dissociation process, cooling and heating isochors and determination of hydrate phase boundaries and composition of the equilibrium phases ........................................................ 103
4.11 Hydrate dissociation conditions measured in this work for (methane + carbon dioxide) clathrate hydrates at various \(\text{CO}_2\) load mole fractions. ................................................................. 106
4.12 Hydrate dissociation conditions (literature and this work) for (methane + carbon dioxide) clathrate hydrates at selected \(\text{CO}_2\) load mole fractions ................................................................. 107
4.13 (a) \(p-y\) phase diagram of (methane + carbon dioxide) clathrate hydrates at different equilibrium temperatures (b) \(p-z\) phase diagram of (methane + carbon dioxide) clathrate hydrates at 280.2 K ................. 109
4.14 Pressure-composition phase diagram of the (methane + carbon dioxide) clathrate hydrates: This work and CSMGem model predictions ........................................................................ 111
5.1 Experimental dissociation conditions for \((\text{nitrogen} + \text{carbon dioxide})\) clathrate hydrates at different \(\text{CO}_2\) load mole fractions. This work and HWHYD model predictions ........................................... 118
5.2 Experimental dissociation conditions for \((\text{nitrogen} + \text{carbon dioxide})\) clathrate hydrates at different \(\text{CO}_2\) load mole fractions: Literature, this work and HWHYD model predictions ........................................... 119
5.3 ARD between experimental and predicted dissociation pressures for \((\text{nitrogen} + \text{carbon dioxide})\) clathrate hydrates at different \(\text{CO}_2\) mole fractions loaded. ................................................................. 121
5.4 Pressure - composition phase diagram for \((\text{nitrogen} + \text{carbon dioxide} + \text{water})\) systems under \((\text{L}_w-\text{H-G})\) equilibrium at different temperatures ................................................................. 122
5.5 Pressure - composition phase diagram for \((\text{nitrogen} + \text{carbon dioxide} + \text{water})\) systems under \((\text{L}_w-\text{H-G})\) equilibrium at selected temperatures. ........................................................................ 124
5.6 Pressure - composition phase diagram for the \((\text{nitrogen} + \text{carbon dioxide} + \text{water})\) systems under \((\text{L}_w-\text{H-G})\) equilibrium: Experimental and literature ................................................................. 125
5.7 Pressure-composition phase diagram for the \((\text{nitrogen} + \text{carbon dioxide} + \text{water})\) systems under \((\text{L}_w-\text{H-G})\) equilibrium at selected temperatures. This work and CSMGem model predictions ................................................................. 126
5.8 Experimental (literature and this work) dissociation conditions for gas hydrates of \((\text{CO}_2 + \text{H}_2)\) formed in the presence water at various feed gas compositions. ................................................................. 128
5.9 Pressure - gas phase composition phase diagram for \((\text{hydrogen} + \text{carbon dioxide} + \text{water})\) systems under \((\text{L}_w-\text{H-G})\) equilibrium at different temperatures ................................................................. 131
5.10 Pressure - gas phase composition phase diagram for \((\text{hydrogen} + \text{carbon dioxide} + \text{water})\) systems under \((\text{L}_w-\text{H-G})\) equilibrium at different temperatures. This work and literature ................................................................. 133
6.1 Experimental dissociation conditions (literature and this work) for \((\text{methane} + \text{TBAB})\) semi-clathrates .... 142
6.2 Experimental dissociation conditions (literature and this work) for \((\text{carbon dioxide} + \text{TBAB})\) semi-clathrates ........................................................................................................ 143
6.3 Experimental hydrate dissociation conditions (literature and this work) for \((\text{nitrogen} + \text{TBAB})\) semiclathrates. ........................................................................................................ 144
6.4 Dissociation conditions (Literature and this work) for semi-clathrates of \((\text{CO}_2 + \text{N}_2)\) formed at various \(\text{CO}_2\) feed gas compositions in the presence of TBAB aqueous solutions ................................................................. 148
6.5 Experimental dissociation conditions for semi-clathrates of \((0.749\ \text{mole fraction CO}_2 + 0.251\ \text{mole fraction N}_2)\) formed in the presence of TBAB aqueous solutions and predictions of CSMGem and HWHYD thermodynamic models in the absence of thermodynamic promoter ................................................................. 151
6.6 Experimental dissociation conditions for semi-clathrates of (0.399 mole fraction CO$_2$ + 0.601 mole fraction N$_2$) formed in the presence of TBAB aqueous solutions and predictions of CSMGem and HWHYD thermodynamic models in the absence of thermodynamic promoter .......................................................... 152
6.7 Experimental dissociation conditions for semi-clathrates of (0.151 mole fraction CO$_2$ + 0.849 mole fraction N$_2$) formed in the presence of TBAB aqueous solutions and predictions of CSMGem and HWHYD thermodynamic models in the absence of thermodynamic promoter .......................................................... 153
6.8 Pressure-composition (gas phase) diagram for semi-clathrates of the (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems at various temperatures and 0.05 mass fractions TBAB .......................................................... 159
6.9 Pressure-composition (gas phase) diagram for semi-clathrates of the (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems at various temperatures and 0.30 mass fractions TBAB .......................................................... 160
6.10 Pressure-composition (gas phase) diagram for semi-clathrates of the (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems at selected temperatures and different initial TBAB concentrations .......................................................... 161
6.11 Pressure-composition (TBAB in the liquid phase) diagram for semi-clathrates of (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems at various temperatures and 0.05 mass fractions TBAB .......................................................... 162
## List of Tables

1.1 Summary of major economic crises leading to important growth of global CO$_2$ industrial emissions since the 1960s ................................................................. 13  
1.2 Main features of post-combustion, pre-combustion and oxy-fuel combustion capture approaches .......... 19  
1.3 Significant research contributions relevant to clathrate hydrate formation of CO$_2$ and tetra alkyl ammonium salts from 1778 to 2007 ......................................................... 22  
1.4 Molecular diameter to cavity diameter ratio for cavity type for the gases of interest within this research .... 24  
1.5 Literature experimental studies for hydrate phase equilibria of gas mixtures containing CO$_2$ + CH$_4$, N$_2$ and H$_2$ ........................................................................................................... 36  
2.1 Commonly used experimental procedures for measuring hydrate dissociation conditions .................. 50  
2.2 Pressure transducers calibration coefficients ......................................................................................... 63  
3.1 Purities and suppliers of chemicals ..................................................................................................... 72  
3.2 Operating conditions of the gas chromatograph ...................................................................................... 74  
4.1 Experimental data reported in the literature for the dissociation conditions of the binary gas hydrates of (carbon dioxide + methane) ................................................................. 90  
4.2 Experimental data reported in the literature for the p, T, and composition of the gas and hydrate phases at (L$_m$-H-G) equilibrium conditions for the binary clathrate hydrates of (carbon dioxide + methane) ............... 90  
4.3 Main characteristics of previous and new experimental setups .......................................................... 91  
5.1 Literature phase equilibrium data of the (carbon dioxide + nitrogen + water) ternary hydrate system ........ 115  
5.2 Review of the compositions of the gas and hydrate phases at hydrate equilibrium conditions reported in the literature for (carbon dioxide + nitrogen + water) ternary system ..................................................... 115  
5.3 Literature review of the experimental data on compositions of the gas and hydrate phases for the (carbon dioxide + hydrogen + water) systems .............................................................. 116  
5.4 Summary of the hydrate phase equilibrium data measured in this work for (CO$_2$ + N$_2$ + H$_2$O) systems ................................. 124  
5.5 Experimental studies on molar compositions of gas hydrates formed in the (CO$_2$ + H$_2$ + H$_2$O) ternary systems ......................................................................................................................... 132  
5.6 Summary of the hydrate phase equilibrium data measured in this work for the (CO$_2$ + H$_2$ + H$_2$O) systems 133  
6.1 Experimental data available in the literature for (CH$_4$ + TBAB) semi-clathrates ................................ 137  
6.2 Experimental data available in the literature for (CO$_2$ + TBAB) semi-clathrates .................................... 137  
6.3 Experimental data available in the literature for (N$_2$ + TBAB) semi-clathrates ........................................ 137  
6.4 Experimental data available in the literature for (CO$_2$ + N$_2$ + TBAB) semi-clathrates ........................ 138  
6.5 Purities and suppliers of materials ....................................................................................................... 140  
6.6 Semi-clathrate hydrate phase equilibrium data for the (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems .......... 149  
6.7 Operating conditions of a conceptual CO$_2$ hydrate-based separation process from (CO$_2$ + N$_2$) gas mixtures at two concentrations of TBAB in aqueous solutions ..................................................... 158
Nomenclature

List of symbols

AARD  absolute average relative deviation [%]
ARD   absolute relative deviation [%]
B     coefficient of density correlation
DE    differential evolution
e     parameter of coefficient equation for density correlation
f     fugacity or parameter of coefficient equation for density correlation
F     number of independent variables or degrees of freedom
g     parameter of coefficient equation for density correlation
G     gas
H     hydrate
H     Henry’s constant [MPa]
HDC   hydrate dissociation condition
L     liquid
n     number of moles
N     number of components
p     pressure [MPa]
q     hydration number
RD    relative deviation [%]
t     time (min, s)
T     temperature [K]
V     volume [m³]
v     molar volume [m³/mol]
x     mole fraction in liquid/aqueous phase
y     mole fraction in gas phase
w     mass fraction
z     water-free mole fraction of CO₂ in hydrate phase

Greek Letters

η     refractive index
π     number of phases
ρ     density
θ     fractional cage occupancy of hydrate guests
**Subscripts**

- $i$: $i^{th}$ unknown variables
- $D$: refractive index in $n_D$
- $m$: gas mixture
- $L$: large cage
- $S$: small cage
- $R$: retention time in gas chromatography
- $W$: water
- $1$: carbon dioxide
- $2$: methane, nitrogen or hydrogen
- $3$: water

**Superscripts**

- $exp$: experimental
- $G$: gas phase
- $H$: hydrate phase
- $L$: liquid phase
- $pred$: predicted
- $t$: total
Introduction
Résumé

Ce chapitre introductif présente le contexte industriel et les motivations liés à la recherche sur les hydrates de dioxyde de carbone. Cette thèse est consacrée à l’étude expérimentale des équilibres de phases de systèmes conduisant à la formation d’hydrates de dioxyde de carbone. En conséquence, nous donnons tout d’abord un aperçu général sur les hydrates et les clathrates, ainsi que sur leurs applications potentielles dans l’industrie et en génie des procédés, y compris dans le domaine du captage de CO₂. Les principes fondamentaux des équilibres de phases en présence d’hydrates et l’utilisation de promoteurs thermodynamiques permettant d’améliorer les conditions de formation d’hydrates sont mis en évidence. Enfin, nous décrivons les objectifs et les grandes lignes de la thèse.

Abstract

This introductive chapter provides the industrial context and motivations behind carbon dioxide hydrate research. As this thesis is concerned with the phase equilibria of carbon dioxide hydrate-forming systems from experimental point of view, a general overview to clathrate hydrate compounds and their potential application in industry and process engineering, including CO₂ capture is given. The fundamentals of hydrate phase equilibria and the use of thermodynamic promoters to enhance the hydrate formation conditions are highlighted and finally, the aims and the outline of the thesis are presented.
Chapter 1 - Ph.D. Dissertation V. BELANDRIA

1 Introduction

1.1 The Growing Need for CO₂ Capture

One of today’s major challenges within process engineering is the implementation of safer, economical and sustainable technologies to meet human ever-increasing needs. Accurate thermodynamic data form the basis in determining the feasibility of applying new processes in industry. This thesis deals with experimental thermodynamics aspects in the context of an alternative carbon dioxide (CO₂) separation approach, through gas hydrate formation.

It is believed that global atmospheric concentrations of CO₂, methane (CH₄) and nitrous oxide (N₂O) have significantly increased as a result of continued economic development and industrialization. Preliminary estimates show a global increase in CO₂ emissions of more than 5 % in 2010 alone, which is the highest growth rate registered over the past two decades (Olivier et al., 2011), as evidenced in Figure 1.1. The major recent economic crises leading to important growth of global CO₂ industrial emissions are listed in Table 1.1. In addition to the increasing levels of CO₂ and other greenhouse gases in the atmosphere, global mean surface temperatures have also increased (IPCC, 2007).

As a result, two major issues arise from today’s global energy discussion. The first is centered on the role of CO₂ in climate change and the second is the long-term sustainability of energy supply. Doubling or even tripling of the global energy demand is expected by 2050 (World Energy Council, 2012), while the latest IPCC (2007) assessment calls for 50 to 85% reduction in global emissions during the same period, in order to avoid dangerous changes in the atmosphere.

In light of these issues, worldwide efforts for a coordinated cooperation in scientific and public policy matters around environmental and energy goals, have resulted in the creation of international conventions and treaties, such as the Kyoto Protocol, promoted by the United Nations Framework Convention on Climate Change (UNFCCC). Within this context, sustainable development, energy supply security and mitigating climate change are the main drivers for energy research beginning the twenty first Century (European Commission, 2007).

Carbon dioxide Capture and Storage (CCS) have thus become a priority within energy research. CCS refers to capturing CO₂ directly from the emission sources by technological means, transport it and store it permanently (Tzimas & Peteves, 2003). As this thesis is
primarily concerned with CO₂ capture applications, no further discussion is given to carbon dioxide transportation or sequestration technologies.

![Graph showing worldwide CO₂ emissions and economic recessions](image)

**Figure 1.1.** Worldwide CO₂ industrial emissions and economic recessions in the past 50 years (modified from Peters et al., 2012). CO₂ emissions are given in Petagrams (Pg) of carbon per year. A Petagram is equal to a trillion (1,000,000,000,000) kilograms or a billion (1,000,000,000) tones. Linear trends are fitted to the five years preceding the beginning of each crisis.

**Table 1.1.** Summary of major economic crises leading to important growth of global CO₂ industrial emissions since the 1960s, as shown in Figure 1.1 (Peters et al., 2012).

<table>
<thead>
<tr>
<th>Year</th>
<th>Event</th>
</tr>
</thead>
<tbody>
<tr>
<td>1973</td>
<td>Oil crisis</td>
</tr>
<tr>
<td>1979</td>
<td>The US savings and loans crisis</td>
</tr>
<tr>
<td>1989</td>
<td>The collapse of the Former Soviet Union (FSU)</td>
</tr>
<tr>
<td>1997</td>
<td>The Asian financial crisis</td>
</tr>
<tr>
<td>2009</td>
<td>The recent global credit crisis</td>
</tr>
</tbody>
</table>
As stated in the European Commission (2007) report, current priorities within CO$_2$ capture include: CO$_2$ separation from flue gas (CO$_2$ + nitrogen), CO$_2$ separation from synthetic fuels (CO$_2$ + hydrogen) and CO$_2$ separation from biogas (CO$_2$ + CH$_4$). Consistent with these imperatives, this thesis contributes to the three preceding CO$_2$ capture objectives.

In 2007, the SECOHYA CO$_2$-Hydrate Separation project was established in France, jointly with the Agence Nationale de la Recherche (ANR) and five academic partners. The goal of this project is to develop a separation process to capture CO$_2$ based on a principle of gas hydrate crystallization (SECOHYA, 2007). The Thermodynamics and Phase Equilibria Laboratory (CEP-TEP) from MINES ParisTech, as member of this partnership, was requested to perform accurate hydrate phase equilibrium measurements of (carbon dioxide and methane, nitrogen or hydrogen) gas mixtures in the presence of tetra-n-butyl ammonium bromide (abbreviated TBAB) aqueous solutions. The scope of the task was specifically targeted to enhancing the fundamental knowledge of hydrate formation and dissociation and elucidating the promotion effect of the latter additive, from thermodynamic point of view (SECOHYA, 2007).

Although the phase behavior of gas hydrates has been extensively studied for decades, better understanding of thermodynamics of CO$_2$ hydrate-forming systems and reliable phase equilibrium data in the presence of thermodynamic additives are fundamental for developing thermodynamically well-founded models and to establish the feasibility of industrial processes involving carbon dioxide hydrates.

1.1.1 Carbon dioxide: Properties, formation, and phase behavior of the CO$_2$ + water system

Before studying the stability of mixed hydrate systems containing carbon dioxide, it is useful to consider some properties of CO$_2$ as a pure compound, as well as the phase behavior of CO$_2$ + water (H$_2$O) mixtures.

Carbon dioxide is a colorless, non-polar compound. It is considered non-harmful (below 1%, by volume), naturally abundant, inert and relatively cheap. Carbon dioxide has a triple point at a temperature of 216.6 K and pressure of 0.519 MPa (NIST WebBook, 2001), and a critical point located at 304.2 K and 7.380 MPa (NIST WebBook, 2001). Along with methane, ethane and propane, carbon dioxide is one of hydrate formers typically found in natural gas (Sloan & Koh, 2008).
Figure 1.2. Carbon dioxide hydrates phase equilibrium in CO$_2$ + water system. Symbols represent experimental data and lines are calculated three-phase equilibrium pressures using a lattice fluid equation of state (Yang et al., 2000).

Most relevant properties of carbon dioxide hydrate include: a density of 1120 kg · m$^3$ at 276 K, measured via X-ray diffraction by Udachin et al. (2001); and molecular weight and molar volume values of 0.1556 kg · kmol and 1.389 · 10$^{-4}$ m$^3$ · mol$^{-1}$, respectively, reported by Anderson (2003).

Figure 1.2 illustrates the phase behavior of CO$_2$ + water (H$_2$O) system, involving the formation of hydrate (H), water-rich liquid (L$_W$), CO$_2$-rich vapor (V$_{CO2}$), CO$_2$-rich liquid (L$_{CO2}$), and ice (I) phases. From this pressure-temperature phase diagram it can be seen that the stability region of CO$_2$ hydrates lies in the middle of the hydrate + ice + vapor (H–I–V$_{CO2}$), hydrate + liquid water + vapor (H–L$_W$–V$_{CO2}$) and hydrate + liquid water + liquid CO$_2$ (H–L$_W$–L$_{CO2}$) equilibrium curves. Any pressure-temperature condition within this region will lead to the coexistence of CO$_2$ hydrates together with gaseous CO$_2$ and liquid water. The lowest measured dissociation condition along the (H–L$_W$–V$_{CO2}$) line for hydrates formed in
the (CO₂ + H₂O) system is 1048 KPa at 271.8 K (Larson, 1955). Two quadruple points are distinguished, namely Q₁ and Q₂, located at (T = 273.1 K; p = 1.256 MPa) and (T = 283.0 K; p = 4.499 MPa), respectively (Sloan, 1998). Q₁ is the quadruple point, where ice + water + hydrate + gas (I-L W-H- V CO₂) coexist, while Q₂ is a (L W-H-V CO₂-L CO₂) equilibrium point.

The idealized dissociation of CO₂ hydrate to gaseous CO₂ and liquid water at the (H–L W– V CO₂) equilibrium can be represented through the following equation:

\[
\text{CO}_2 \cdot q \text{H}_2\text{O}(s) \leftrightarrow \text{CO}_2(g) + q\text{H}_2\text{O}(l) \tag{1.1}
\]

where \( q \) represents the number of hydrate water molecules per guest molecule, namely hydration number. The concept of hydration number is used later in Chapters 4 and 5 for determining the composition of mixed hydrate systems.

Based on reaction (1.1), the amount of energy required for dissociating CO₂ hydrates (per mole of CO₂ in the hydrate) has been reported to vary from (57.7 to 65.22) kJ · mol⁻¹ (Anderson, 2003). This advantageous exothermic nature of CO₂ hydrate’s formation compared to the heat of CH₄ hydrate dissociation (54.49 kJ· mol⁻¹) can be fully exploited for sequestering CO₂ with simultaneous production of natural gas from methane hydrates (Goel, 2006).

Gaseous carbon dioxide is mainly formed as a by-product from combustion of fossil fuels (e.g. natural gas, coal and oil). The combustion of all carbon-based fuels follows a very similar chemical reaction. As an example, the well-known reaction of carbon with oxygen is given below, where CO₂ enthalpy of formation is -393.5 kJ · mol⁻¹, as reported in the NIST WebBook (2001).

\[
\text{C} + \text{O}_2 \rightarrow \text{CO}_2 \tag{1.2}
\]

The major industrial sectors releasing CO₂ to the atmosphere include: thermal power generation, cement production, natural gas and oil refining, gas flaring, iron and steel production, gas leakages and waste (OECD/IEA, 2008). Since fossil fuels are usually combusted with excess air, other compounds are also formed together with CO₂, i.e. nitrogen (N₂), carbon monoxide (CO), water vapor, oxygen (O₂), etc. The ratio of these products in the exhaust gases and the exact temperature and pressure conditions depend on the plant type, operating conditions and the parameters of the combustion process (Tzimas & Peteves, 2003).
Indeed, the majority of CO\textsubscript{2} emission sources have a molar CO\textsubscript{2} concentration that has been reported to vary from roughly 15 mole % in flue gases, to about 4 mole % in natural gas combustion in combined cycle (IEA, 2001). Whereas in other processes involving hydrogen (H\textsubscript{2}) production from fossil fuels, \textit{e.g.} steam-natural gas reforming and/or integrated coal gasification power plants, a stream of almost pure CO\textsubscript{2} is produced (~ > 95 mole %). In such processes, it has been estimated that one ton of H\textsubscript{2} produced may also produce about 9 tons of carbon dioxide (Collodi & Wheeler, 2010).

As result of its increased concentration (0.039 \%, by volume) in the atmosphere (NOAA, 2012), carbon dioxide is currently considered a primary greenhouse gas contributing to the so-called global warming effect. Regardless remaining controversies and debates on this issue, research efforts are currently undergoing worldwide for continuing the development of technological solutions to enable CO\textsubscript{2} capture.

1.1.2 \textit{Solutions for Capturing CO\textsubscript{2}}

According to the Intergovernmental Panel on Climate Change (IPCC) special report on CCS, the power plants activity constitutes more than 60 \% of CO\textsubscript{2} emissions, where N\textsubscript{2} and CO\textsubscript{2} are the most significant components (IPCC, 2007). On the other hand, the IEA (2008) assessment states that CCS technology alone has the potential to reduce greenhouse gas emission by 20 \% by 2050. CCS is thus recommended as “\textit{…one of the most promising solutions to stabilize atmospheric levels of CO}\textsubscript{2}…” (IPCC, 2007).

Based on process conditions, such as: CO\textsubscript{2} concentration, temperature, pressure, fuel type and degree of required CO\textsubscript{2} removal from the feed; most common CO\textsubscript{2} capture technologies fall under three general categories, namely: post-combustion, pre-combustion and oxy-fuel combustion. The first two approaches are considered economically feasible under specific conditions, while the third one is at demonstration phase (IPCC, 2007). The Lacq oxyfuel combustion CCS project, briefly described below, is an example of this. A variety of processes have been thus developed for separating and capturing CO\textsubscript{2}, and many of them are commercially available, as indicated in Table 1.2.

These processes are generally based on gas phase separation, absorption into a liquid, \textit{i.e.} amines absorption (Rubin & Rao, 2002), adsorption on a solid, and more recently, hybrid techniques such as adsorption/membrane systems, \textit{etc}. 

17
# Chapter 1 - Ph.D. Dissertation

## Drawbacks

- High regeneration costs
- Degradation of solvents due to the presence of impurities and by-products
- Low CO\(_2\) loading capacity
- Solvent can form corrosive solutions with flue gases.
- Lost solvent precipitates.
- Large equipment size
- Sorbent susceptible to degradation
- Cannot handle easily large concentrations of CO\(_2\)
- Adsorption time is not practical
- Low degree of CO\(_2\) separation
- Poor selectivity of sorbents to CO\(_2\)
- Operation costs higher than absorption processes
- Requires a high partial pressure of CO\(_2\) in the feed
- Capacity proportional to CO\(_2\) partial pressure and temperature
- Low selectivity of solvent causes H\(_2\) losses
- Low degree of selectivity to CO\(_2\)
- Corrosion might be caused by SO\(_2\)
- High cost of O\(_2\) production
- Operation and capital costs similar to post-combustion processes

## Advantages

- Well established process
- Solvent can be recycled
- Degree of CO\(_2\) purity > 95%
- Non dependence on human operators, minimizing labor costs
- Likely to be incorporated in existing power plants without significant modifications
- Commercially available
- Sorbent can be reused
- Low concentrations of CO\(_2\) yield an optimum performance
- Requires less energy for regeneration than chemical absorption processes
- Less expensive than post-combustion capture
- Commercially available
- Low maintenance required
- Needs less energy than PSA
- Refinery of liquefied CO\(_2\)
- Flue gas is mostly CO\(_2\) and H\(_2\)O
- Water can be removed by condensation
- Separation of CO\(_2\) is relatively inexpensive
- No need of control equipment for impurities
- Smaller size of equipment since only O\(_2\) is supplied for combustion

## Current application

- Separation of CO\(_2\) from natural gas and flue gases
- Production of hydrogen (mainly for fertilizer manufacture)
- Refinery of liquefied CO\(_2\)
- Oxyfuel exhaust gas (O\(_2\)/N\(_2\))

## Method

- Absorption (Chemical solvents)
- Adsorption (Solid sorbents)
- Physical absorption e.g. Pressure Swing Adsorption (PSA) and Temperature Swing Adsorption (TSA).
- Membrane separation
- Cryogenic separation

## Table 1.2. Main features of post-combustion, pre-combustion and oxy-fuel combustion capture approaches

<table>
<thead>
<tr>
<th>Capture approach</th>
<th>Separation task / feed</th>
<th>(p), (T) and feed composition</th>
<th>Method</th>
<th>Current application</th>
<th>Advantages</th>
<th>Drawbacks</th>
</tr>
</thead>
<tbody>
<tr>
<td>Post-combustion</td>
<td>Flue gas (CO(_2)/N(_2))</td>
<td>Near atmospheric pressure &lt; 373 K, 4 – 15 mole % CO(_2)</td>
<td>Absorption</td>
<td>Separation of CO(_2) from natural gas and flue gases</td>
<td>Well established process, Solvent can be recycled, Degree of CO(_2) purity &gt; 95%, Non dependence on human operators, minimizing labor costs, Likely to be incorporated in existing power plants without significant modifications, Commercially available, Sorbent can be reused, Low concentrations of CO(_2) yield an optimum performance</td>
<td>High regeneration costs, Degradation of solvents due to the presence of impurities and by-products, Low CO(_2) loading capacity, Solvent can form corrosive solutions with flue gases, Lost solvent precipitates, Large equipment size, Sorbent susceptible to degradation, Cannot handle easily large concentrations of CO(_2), Adsorption time is not practical, Low degree of CO(_2) separation, Poor selectivity of sorbents to CO(_2), Operation costs higher than absorption processes</td>
</tr>
<tr>
<td>Pre-combustion</td>
<td>Syngas (CO(_2)/H(_2))</td>
<td>&gt; 0.5 MPa, &gt; 373 K, 35 mole % CO(_2)</td>
<td>Physical absorption e.g. Pressure Swing Adsorption (PSA) and Temperature Swing Adsorption (TSA).</td>
<td>Production of hydrogen (mainly for fertilizer manufacture)</td>
<td>Requires less energy for regeneration than chemical absorption processes, Less expensive than post-combustion capture</td>
<td>Requires a high partial pressure of CO(_2) in the feed, Capacity proportional to CO(_2) partial pressure and temperature, Low selectivity of solvent causes H(_2) losses, Low degree of selectivity to CO(_2)</td>
</tr>
<tr>
<td>Oxy-fuel combustion</td>
<td>Oxyfuel exhaust gas (O(_2)/N(_2))</td>
<td>&gt; 5 MPa, &lt; 323 K, 90 mole % CO(_2)</td>
<td>Cryogenic separation</td>
<td>Refinery of liquefied CO(_2)</td>
<td>Flue gas is mostly CO(_2) and H(_2)O, Water can be removed by condensation, Separation of CO(_2) is relatively inexpensive, No need of control equipment for impurities, Smaller size of equipment since only O(_2) is supplied for combustion</td>
<td>Corrosion might be caused by SO(_2), High cost of O(_2) production, Operation and capital costs similar to post-combustion processes</td>
</tr>
</tbody>
</table>
Some other innovative concepts have been reviewed by Granite and O’Brien (2005). They include: electrochemical pumps, metal organic frameworks, ionic liquids, and enzyme-based, cryogenic and bio-mimetic approaches. The progress of CO\(_2\) capture technologies is an extensive topic itself and it has been well covered, with different levels of detail, in several reviews available in the literature (Tzimas & Peteves, 2003; Aaron & Tsouris, 2005; Zachary & Titus, 2008; Yang et al. 2008; Figueroa et al. 2008; Pennline et al. 2008 and Herzog, 2009). Essentially, the major benefits and drawbacks of the three CO\(_2\) capture approaches; as well as approximate process conditions are summarized in Table 1.2.

It is worthwhile to note that the conditions of the feed differ somewhat for the three approaches. As stated by Tzimas and Peteves (2003) “syngas has a higher CO\(_2\) concentration than flue gas and it is generally available at a higher pressure and temperature”. Besides, it has been estimated that the exhaust gas from oxyfuel combustion is produced at even higher pressures at ambient temperature.

As can be seen in Table 1.2, many of these technologies have proved their technical feasibility for capturing CO\(_2\) from industrial emissions. However, to address the current lack of demonstrated capabilities for large-scale CO\(_2\) capture (Figueroa et al., 2008; Folger, 2010), a number of demonstration projects are planned or undergoing worldwide. Examples are the Mountaineer power plant in West Virginia (USA) and the Lacq project in France. The first started capturing a portion of a 20 MW coal-based plant CO\(_2\) emissions in 2009 using chilled ammonia. About 100,000 tons of CO\(_2\) per year are stored in a deep saline aquifer injection well. The cost of the project is US$70 million, and it could be expanded to 235 MW in 2014-2015, as reported by the National Mining Association (NMA, 2012). The Lacq project is Europe’s first integrated CO\(_2\) capture and storage facility using oxyfuel combustion technology, including CO\(_2\) injection in a depleted on-shore hydrocarbon reservoir (TOTAL, 2007). The test started in 2010 and it plans to capture 120,000 tons of CO\(_2\) over two years, at a cost of US$85.6 million (TOTAL, 2007).

In continuation to the above efforts, critical issues regarding large energy consumption, corrosion, foamingess, low capacities, safety and environmental concerns are the focus of most current CO\(_2\) capture research projects. As a result, the development of alternative energy efficient and less costly processes for CO\(_2\) capture is necessary. In this regard, gas hydrates
crystallization approach has been proposed as an emerging concept to capture CO\textsubscript{2} (Spencer, 1997; Kang & Lee, 2000; Duc et al., 2007).

As gas hydrates (also denoted clathrate hydrates) have the capacity to store/separate gases, there is a large field of potentially interesting applications, such as CO\textsubscript{2} sequestration and CH\textsubscript{4} recovery from natural gas hydrates in deep sea sediments (Ohgaki et al., 1994), natural gas processing, storage and transportation (Koh, 2002), H\textsubscript{2} separation from steam reforming processes (Sugahara et al., 2005), H\textsubscript{2} storage (Strobel et al., 2006), sea water desalination (Seo & Lee, 2001), etc.

1.2 Gas Hydrates: An Introductory Overview

The purpose of this section is to provide a concise overview of clathrate hydrates fundamentals in order to set the theoretical formalisms for studying the phase equilibria of gas hydrate forming systems.

1.2.1 Historical Background

Prominent scientists of the 18\textsuperscript{th} and 19\textsuperscript{th} centuries including Joseph Priestley (1778), Sir Humphrey Davy (1810) and Michel Faraday (1823) are associated with the early discovery of gas hydrates (Makogon, 1997; Sloan & Koh, 2008). An approximation to hydrates’ composition was first reported for Cl\textsubscript{2} hydrates (Faraday, 1823). Afterwards gas hydrate research remained mainly a scientific curiosity for more than a century. A considerable number of hydrate formers together with the pressure and temperature conditions at which they are formed and their chemical compositions were identified over this period, including CO\textsubscript{2} hydrate systems investigated by Polish physicist and chemist Zygmunt Florenty Wróblewski in 1882 (Wróblewski, 1882).

Traditionally, the progress of clathrate hydrates research and development has been divided into three historical periods. Hammerschmidt’s discovery of hydrate plugs in natural gas pipelines in 1934 marked the beginning of an industry-oriented second research period (Sloan & Koh, 2008),
under the auspices of oil and gas companies. Most relevant research contributions related to CO\textsubscript{2} hydrates within this second period include the determination of the hydrate phase boundary between (273 and 283) K in the mid-1900s (Deaton & Frost, 1946), and the classification of CO\textsubscript{2} hydrate crystal as a structure I for the first time via X-ray diffraction technique (von Stackelberg & Müller, 1954).

More recently, the existence of natural gas hydrates as an energy resource (Makogon, 1965) intensified worldwide hydrate research interest within the scientific community and energy industry. This event established the beginning of the third historical research period.

Today gas hydrates are known to exist in the universe. The most common research interests on Earth focus in three large fields: 1) its avoidance in the oil and gas industry (Sloan & Koh, 2008), 2) as an alternative energy resource (Makogon, 2010), and 3) their beneficial application to novel technologies, such as: transport of natural gas as frozen hydrate (Gudmundsson & Hveding, 1995), high pressure SIMTECHE CO\textsubscript{2} hydrate separation process (Tam et al., 2001), air conditioning system using clathrate hydrate slurry (Obata et al., 2003), CO\textsubscript{2} gas hydrate engine systems (Obara et al., 2011), etc.

The major scientific research achievements over the past two centuries are thoroughly reviewed by Davidson (1973), Makogon (1997), Sloan and Koh (2008), Giavarini and Hester (2011), etc. The contributions listed in Table 1.3 are meant to provide a chronological background to carbon dioxide hydrate research, from about 1778 until just before starting the present research (2007).
Table 1.3. Significant research contributions relevant to clathrate hydrate formation of CO\textsubscript{2} and tetra alkyl ammonium salts from 1778 to 2007 (Makogon, 1997; Sloan & Koh, 2008).

<table>
<thead>
<tr>
<th>Year</th>
<th>Researcher</th>
<th>Contribution</th>
</tr>
</thead>
<tbody>
<tr>
<td>1778</td>
<td>Priestley</td>
<td>Formed SO\textsubscript{2} hydrates</td>
</tr>
<tr>
<td>1810</td>
<td>Davy</td>
<td>Identified Cl\textsubscript{2} hydrate</td>
</tr>
<tr>
<td>1823</td>
<td>Faraday</td>
<td>Deduced Cl\textsubscript{2} hydrate’s composition as (Cl\textsubscript{2}·10H\textsubscript{2}O)</td>
</tr>
<tr>
<td>1882</td>
<td>Cailletet and Bordet</td>
<td>Measured mixed gas hydrate systems: CO\textsubscript{2} + PH\textsubscript{3} and H\textsubscript{2}S + PH\textsubscript{3}</td>
</tr>
<tr>
<td>1882</td>
<td>Wróblewski</td>
<td>Studied CO\textsubscript{2} hydrate formation in CO\textsubscript{2} + H\textsubscript{2}O system</td>
</tr>
<tr>
<td>1894 and 1897</td>
<td>Villard</td>
<td>Determined CO\textsubscript{2} hydrate composition as CO\textsubscript{2}·6H\textsubscript{2}O and CO\textsubscript{2} hydrate dissociation curve in the range of (267 to 283) K</td>
</tr>
<tr>
<td>1902</td>
<td>de Forcrand</td>
<td>Extensively used Clausius-Claypeyr\textsubscript{on} equation to determine enthalpies of dissociation and compositions of gas hydrates</td>
</tr>
<tr>
<td>1934</td>
<td>Hammerschmidt</td>
<td>Realized that formation of natural gas hydrates was responsible for plugging natural gas pipelines and discovered thermodynamic inhibitors</td>
</tr>
<tr>
<td>1940</td>
<td>Fowler</td>
<td>Identified hydrates of tetra alkylammonium salts (TBAX)</td>
</tr>
<tr>
<td>1946</td>
<td>Deaton and Frost</td>
<td>Measured dissociation pressures of CO\textsubscript{2} hydrates between (273 and 283) K</td>
</tr>
<tr>
<td>1949</td>
<td>Unruh and Katz</td>
<td>Reported (L\textsubscript{W}–H–V) data for CO\textsubscript{2} + CH\textsubscript{4} mixed hydrates</td>
</tr>
<tr>
<td>1954</td>
<td>von Stackelberg and Müller</td>
<td>Determined hydrate crystal structures I and II through X-ray diffraction and classified CO\textsubscript{2} hydrate as a type I</td>
</tr>
<tr>
<td>1959</td>
<td>van der Waals and Platteeuw</td>
<td>Proposed a statistical thermodynamic model for calculating hydrate formation conditions</td>
</tr>
<tr>
<td></td>
<td>(vdWP) McMullan and Jeffrey</td>
<td>Examined hydrates formed by quaternary alkylammonium salts using X-ray diffraction</td>
</tr>
<tr>
<td>1972</td>
<td>Parrish and Prausnitz</td>
<td>Applied vdWP model to natural gases and mixed hydrates</td>
</tr>
<tr>
<td>1984</td>
<td>Dyadin and Udachin</td>
<td>Further investigated TBAX hydrates</td>
</tr>
<tr>
<td>1987</td>
<td>Ripmeester and coworkers</td>
<td>Reported the existence hydrate structure H hydrates</td>
</tr>
<tr>
<td>1997</td>
<td>Spencer</td>
<td>Patented a method of selectively separating CO\textsubscript{2} from multicomponent gaseous streams through CO\textsubscript{2} clathrate formation</td>
</tr>
<tr>
<td>2000</td>
<td>Kang and Lee</td>
<td>Proposed a new hydrate-based gas separation process for recovering &gt; 99 mole % of CO\textsubscript{2} from flue gas using THF as hydrate promoter</td>
</tr>
<tr>
<td>2003</td>
<td>Shimada and coworkers</td>
<td>Found that TBAB hydrate crystals could be used to separate small gas molecules</td>
</tr>
<tr>
<td>2007</td>
<td>Duc and coworkers</td>
<td>Investigated (CO\textsubscript{2} + N\textsubscript{2}) hydrates using TBAB as a thermodynamic promoter</td>
</tr>
</tbody>
</table>
1.2.2 Definition and Crystalline Structures

Gas hydrates or clathrate hydrates are ice-like crystalline compounds, which are formed through a combination of water and guest molecules under suitable conditions of low temperature and high pressures (Sloan & Koh, 2008). In a gas hydrate, hydrogen-bonded ‘host’ water molecules form special cavities and ‘guest’ gas molecules are trapped inside the cavities. The hydrate structure is stabilized by the repulsive interactions between guests and hosts molecules (Sloan & Koh, 2008). The majority of gas hydrates are known three common crystal structures: structure I (sI), structure II (sII) and structure H (sH), where each structure is composed of a certain number of cavities formed by water molecules (Mohammadi & Richon, 2009). Figure 1.3 provides a hydrate structure summary for sI, sII and sH.

As shown in Figure 1.3, all hydrate structures have repetitive crystal units. However, they differ in the number and sizes of the cages and in their unit cells.

![Figure 1.4. Hydrate crystal unit structures: sI, sII and sH (Sloan, 2003). Shaded squares represent the number of cavity types, superscripts indicate the number of faces per cavity type and the shaded rectangles give the number of water molecules per hydrate structure.](image-url)
Hydrate crystal structures I and II were first determined through x-ray diffraction methods by von Stackelberg and Müller (1954). They found that each structure is composed of a certain number of large and small cavities formed by water molecules. For example, structure I clathrate hydrates are composed of two 12-pentagonal ($5^{12}$) cavities and two $5^{12}6^2$ (2-hexagonal face) cavities. The existence of a new hydrate structure, known as sH, was reported by Ripmeester and coworkers (1987). This third structure requires both large ($\sim 6-7$ Å) and small ($\sim 4-5$ Å) molecules, such as light oil fractions and CH$_4$, respectively. Many other structures beyond the scope of this work have been reported afterwards. Extensive reviews on clathrate hydrates crystalline structures are given by Sloan and Koh (2008) and Carroll (2009).

For a guest molecule to enter a cavity, it must meet dimensional, physicochemical and morphological criteria. Typical examples of hydrate forming substances include CH$_4$, ethane (C$_2$H$_6$), propane (C$_3$H$_8$), CO$_2$, N$_2$, H$_2$ and H$_2$S. Of the gases of interest within this work, CO$_2$ and CH$_4$ are known to form sI as simple hydrates, while N$_2$ and H$_2$ have been classified as sII hydrate formers (Sloan & Koh, 2008). This could be explained by the ratios of molecular diameter to cavity diameter listed in Table 1.4. In simple hydrate formers, stable structures occur, as a rule, within the upper and lower limits in diameter ratios of about 1.0 and 0.76, respectively (Sloan & Koh, 2008). For instance, CO$_2$ with a ratio of 1.0 is capable of occupying both the small ($5^{12}$) and large ($5^{12}6^2$) cages of sI. Although the diameter ratio of CH$_4$ to the small cavity of sII is 0.87, it has been determined that CH$_4$ stabilizes the small and large cavities of sI with a diameter ratio of 0.86.

Table 1.4. Molecular diameter to cavity diameter ratio for cavity type for the gases of interest within this research (Sloan & Koh, 2008).

<table>
<thead>
<tr>
<th>Guest hydrate former</th>
<th>Structure I</th>
<th>Structure II</th>
</tr>
</thead>
<tbody>
<tr>
<td>Molecule</td>
<td>$5^{12}$</td>
<td>$5^{12}6^2$</td>
</tr>
<tr>
<td>H$_2$</td>
<td>2.72</td>
<td>0.533</td>
</tr>
<tr>
<td>N$_2$</td>
<td>4.1</td>
<td>0.804</td>
</tr>
<tr>
<td>CH$_4$</td>
<td>4.36</td>
<td>0.855</td>
</tr>
<tr>
<td>CO$_2$</td>
<td>5.12</td>
<td>1.00</td>
</tr>
</tbody>
</table>
In nitrogen hydrates, N\textsubscript{2} stabilizes the small cavities of sII (size ratio of 0.82) and it also occupies in less degree the large (5\textsuperscript{12}6\textsuperscript{4}) sII cavities. At moderate pressures, in all three-hydrate structures, each cavity can contain at most one guest molecule (Englezos, 1993). However, it is interesting to note that since nitrogen is so small (~4 Å), more than one molecule can easily fit the large cavities of sII. Hence, multiple cage occupancy can occur at pressures higher than 30 MPa (Sloan & Koh, 2008).

When two different guests molecules combine in a binary or mixed clathrate hydrate, the situation is quite different. Complex guest size–structural relations and/or transitions may occur and affect the thermodynamic equilibrium between coexisting phases. For example, the addition of 1 mole % C\textsubscript{3}H\textsubscript{8} to pure CH\textsubscript{4} hydrates has been reported to cause a decrease in the hydrate formation pressure of up to 42 % due to a structure change (Sloan & Koh, 2008). Crystalline structures thus play a significant role on the equilibrium state (three-phase temperature, pressure and gas hydrate composition) required for hydrate stability. The microscopic aspects discussed in the preceding paragraphs are meant to provide the basis for better understanding gas hydrates phase equilibria discussed in the following sections.

1.2.3 Phase Diagrams

The phase behavior of gas hydrates considerably changes depending on the size and chemical nature of guest molecules. The relationship between microscopic structure, just described, and macroscopic hydrate phase properties can be better understood through the study of phase diagrams. A brief description of phase diagrams for single-component, two-component, three-component and multicomponent systems is thus provided to gain a fundamental insight into the phase equilibria of hydrate forming systems.

A typical phase diagram for pure water exhibiting gas, liquid, and solid phases is shown in Figure 1.4. In the triple point, found at 273.16 K and 6.117 \cdot 10^{-4} \text{ MPa} (Lide, 2004), all three phases are in equilibrium. The phases are separated by phase boundaries, where phase transitions occur. The phase boundary between liquid and gas ends at the critical point, located at 647.1 K and 22.064 MPa (Wagner et al., 2000). Above this point a single fluid phase referred to as a supercritical fluid is formed.
As an example of the phase behavior for two-component systems, the phase diagram of (CH$_4$ + H$_2$O) binary mixtures is considered. Depending on the pressure and temperature conditions, four stability regions are defined in Figure 1.5, namely: liquid water + methane gas (L$_w$ + V$_{CH4}$) located at high temperatures and moderate pressures; at high pressures crystallization occurs and the liquid water + methane hydrate (L$_w$ + H$_{CH4}$) zone appears; if temperature decreases, water ice + methane hydrate (I + H$_{CH4}$) is formed; finally, a subsequent pressure decrease establishes the water ice + methane gas (I + V$_{CH4}$) zone.

The phase diagram shown in Figure 1.6 is the equivalent of Figure 1.5 for systems containing hydrocarbon (e.g., C$_2$H$_6$, C$_3$H$_8$ or i-C$_4$H$_{10}$) + H$_2$O, CO$_2$ + H$_2$O (Figure 1.1) or hydrogen sulfide (H$_2$S) + H$_2$O. In this diagram a three-phase (L$_w$-V-L$_{HC}$) equilibrium curve at high temperature and high-pressure conditions is depicted. Also, a second quadruple point, Q$_2$, in which L$_w$, H, V and L$_{HC}$ coexist, is formed at the intersection of the L$_w$-V-L$_{HC}$ with the L$_w$-H-V equilibrium curves. Similar to Figure 1.2, for systems with two quadruple points, the hydrate region falls in between the I-H-V curve (at conditions below Q$_1$), the L$_w$-H-V line (between Q$_1$ and Q$_2$), and the L$_w$-H-L$_{HC}$ line at temperatures and pressures above Q$_2$ (Sloan & Koh, 2008).
In Figure 1.7, the lower zone of the pressure-temperature phase diagram for natural gases without liquid hydrocarbon is similar to that shown in Figure 1.6. However, the main differences are that the $L_W$-$H$-$V$ curve occurs at a fixed composition of hydrocarbon mixture, and that the quadruple point ($Q_1$) appears at a lower pressure. In the case in which natural gases contain heavier components, the ($L_W$-$H$-$V$) phase boundary represents the hydrate formation region equivalent to the region between the quadruple point ($Q_1$) and the upper quadruple point ($Q_2$) of Figure 1.6 (Sloan & Koh, 2008).

Figure 1.4. Pressure-temperature diagram for methane + water system in the hydrate region (GasHyDyn Center, ENSMSE).
Figure 1.5. Pressure-temperature phase diagram for hydrocarbon + water systems (Sloan & Koh, 2008).

Figure 1.6. Pressure-temperature phase diagram for multicomponent natural gas systems (Sloan & Koh, 2008).
In addition, the dew and bubble-point curves can be distinguished in the phase envelope region in Figure 1.7. At low pressures and moderate temperatures, the (Lw-H-V) line intersects the phase envelope and a second liquid begins to form (Lw-H-V-Lhc). As pressure continues to raise, more of the second liquid forms as expected, until a point where the amount of the second liquid reaches a maximum. Beyond the critical point, the amount of the second liquid decreases until it totally disappears (Carroll, 2009).

1.2.4 Gibbs’ Phase Rule Consideration

In the above phase diagrams, the equilibrium relationships are established by the equality in all potentials likely to modify the system. Upon equilibrium, no further changes occur in the macroscopic properties of the system with time. Thus, the equilibrium state of a PVT system containing \( N \) chemical species and \( \pi \) phases is function of a certain number of intensive properties, namely: \( T, p, \) and composition of each phase (Smith et al., 2001). These measured quantities are independent of the amount of phase present.

In clathrate hydrates, the number of independent variables needed to specify the system \( (F) \), also called degrees of freedom, is given by the Gibbs’ Phase Rule for non-reacting systems, presented without derivation as (Smith et al., 2001):

\[
F = 2 - \pi + N
\] (1.3)

The application of the Gibbs’ Phase Rule, in the thermodynamic analysis of systems under (hydrate + liquid + vapor) equilibrium, is addressed later in experimental Chapters 4 and 5.

1.2.5 Gas Hydrates Potential in Industry and Process Engineering

Although for many years gas hydrates have been considered an industrial concern, especially in oil and gas production and in processing and transportation facilities (Sloan & Koh, 2008), positive applications of gas hydrates are currently considered a subject of increasing research
interest, based on the number of studies recently published in the literature (Eslamimanesh et al., 2012).

Suitable conditions for clathrate hydrate formation may commonly occur in broad areas including energy and climate subject matters. During hydrocarbon production, gas hydrate formation may affect flow assurance and safety from wells to processing facilities (Sloan, 2003). In the natural environment, hydrates may be found in the sediments of the deep-sea continental margins, the subsurface of Arctic permafrost regions, and in deep glacial ice (Englezos, 1993). Other applications include hydrates as means of gas separation, storage material for H\textsubscript{2}, cool energy storage and recovery, seawater desalination, water removal from industrial effluents, edible products, and bioengineering (Sloan & Koh, 2008).

Domains of gas hydrates application also include power plants, oil and gas refining, hydrogen and ammonia processing, iron and steel manufacturing, cement production, natural gas production with high concentrations of acid gases (H\textsubscript{2}S and CO\textsubscript{2}), coal gasification, shift conversion, etc.

The role of gas hydrates in disasters such as the Macondo well blowout in the Gulf of Mexico in 2010 has been reported in the literature (Koh et al., 2011) and it is not addressed in this work.

### 1.2.6 CO\textsubscript{2} Capture by Gas Hydrate Crystallization

Gas hydrates crystallization is a reversible process that has been proposed as an emerging concept for CO\textsubscript{2} capture (Seo et al., 2000; Linga et al., 2007a). It has been estimated that hydrate-based processes are less energy intensive and thereby are considered a promising alternative for separating CO\textsubscript{2} from industrial gases (Kang & Lee, 2000; Duc et al., 2007).

The approach of gas hydrates as means of separation, especially in CO\textsubscript{2} capture, uses the van der Waals interactions between water molecules to encage gas molecules in the hydrate structure (SECOHYA, 2007). The concept consists in mixing water and a gas mixture containing CO\textsubscript{2} under hydrate-forming conditions, typically (and unless some appropriate additives are used) at low temperatures (< 300 K) and moderate pressures (> 0.6 MPa).
Figure 1.7. Carbon dioxide hydrate phase boundary compared to nitrogen, hydrogen and methane. CO₂, CH₄ and N₂ hydrate phase boundaries were predicted using HWHYD model and the point for H₂ hydrates is the data point reported by Mao and Mao (2004).

Based on the difference in the pressure and temperature conditions required for CO₂ hydrate formation compared to other industrial/flue gases (Figure 1.8), it is expected that CO₂ will preferentially enter the hydrate phase and thereby be separated.

Figure 1.9 shows a schematic flow diagram of the hydrate-based gas separation (HBGS) process suggested by Kang et al. (2000), especially for recovering CO₂ from flue gas. The flue gas from a power plant is first passed through the commercial desulfurization facility for SOₓ removal. The pretreated flue gas goes to the first hydrator charged with an aqueous solution containing thermodynamic additive. However, the next two hydrators contain only water. More than 99
mole % of CO₂ is expected to be removed from the flue gas through this process (Kang et al., 2000).

When gas hydrate crystals are formed the concentration of CO₂ in the hydrate phase is different than that in the original gas mixture. The CO₂-rich phase is then dissociated by depressurization and/or heating at ambient temperature to recover the enriched CO₂ gas. This results in a fractionation similar to that between a gas phase and a liquid phase in a distillation column. The main difference is that the fractionation is between a gas phase and a solid phase (SECOHYA, 2007).

A noticeable progress in processes involving CO₂ gas hydrates can be evidenced through the studies reported in the literature. Among the most recent proposals, Surovtseva et al. (2011) have suggested a CO₂ capture technology incorporating two low-temperature processes, namely cryogenic condensation and hydrate formation. This separation approach, as shown Figure 1.10, can be applied to industrial gasification facilities, where more than 80 mole % of CO₂ is expected to be captured at temperatures around 275 K and pressures above 5 MPa.

In CO₂ recovering from flue gas, pressure, temperature and compositional data are useful for engineering purposes. The isothermal $p$-$x$ diagram given in Figure 1.11 conceptually illustrates the two-stage separation required to achieve the recovery of more than 95 mole % CO₂ from a (CO₂ + N₂ + H₂O) mixture by hydrate crystallization (Kang & Lee, 2000). Because of the importance of such data, simultaneous compositional analysis and hydrate phase equilibria measurements have been considered within the scope of this work.
Figure 1.8. Flow diagram of a hydrate-based CO$_2$ recovery process, as proposed by Kang and Lee (2000). C$_1$: precipitator, C$_2$: condenser, D: dissociation unit, R: reservoir, F$_1$: first hydrator containing thermodynamic additive aqueous solution, F$_2$ and F$_3$: second and third hydrators.

Figure 1.9. Flow diagram of an integrated cryogenic and hydrate CO$_2$ capture process, as suggested by Surovtseva et al. (2011).
As shown in Figure 1.8, high pressure conditions are in theory required to form hydrates from gas mixtures containing N₂ or H₂. However, flue gas emissions are in general close to atmospheric pressure (Table 1.2). Operative costs would significantly increase if compression of these gases is considered in order to satisfy hydrate formation conditions. This is a major drawback of hydrate-based separation processes that reduces its energy efficiency. The impact of such phenomenon could be, however, minimized by using thermodynamic promoters. Consequently, there has been recently an increased interest in some large guest molecules that promote hydrate formation, known as thermodynamic additives. Such chemicals shift the hydrate phase boundary, reducing the pressure and amount of cooling required for gas hydrate formation.

As mentioned earlier, potential domains of application of hydrate crystallization approach include: seawater desalination, wastewater treatment, oil and gas separation, storage and transportation of natural gas, and CO₂ capture. Thus, the study of thermodynamic additives capable of reducing the hydrate formation pressure and increasing the gas hydrate equilibrium temperature and/or formation rate along with possible modification of the selectivity of hydrate...
cages for encaging various gas molecules in the water cages (Mohammadi et al., 2011a) has become an emerging subject of industrial and scientific interest.

1.2.7 Use of Thermodynamic Promoters

Gas hydrate based-separation processes could be improved by looking for appropriate thermodynamic additives to decrease the operative pressure when necessary. Since the presence of thermodynamic additives alters the state of the liquid phase, the pressure-temperature conditions at which hydrates form are consequently shifted to milder conditions. In recent years, considerable efforts have been made to investigate gas hydrate crystallization approach for separating a specific gas constituent from a multi-component gaseous mixture under favorable temperature and pressure conditions.

Table 1.5 provides an overview of the state-of-the-art on hydrate phase equilibrium studies reported in the literature by the time this research began (in 2008). Emphasis is given to gas mixtures containing CO₂, CH₄, N₂ or H₂. Up to date studies are referred in later sections. Furthermore, an exhaustive compilation of hydrate phase equilibrium data is provided by Sloan and Koh (2008). Also, other studies can be found in a comprehensive review by Eslamimanesh and coworkers (2012).

The selection of appropriate thermodynamic additives is subjected to the potential field of application. Various intermediate sized hydrocarbons have been identified as thermodynamic promoters, namely the sII hydrate-formers: cyclopentane, neopentane, benzene, and cyclohexane, and the sH hydrate-formers: methylcyclopentane, methylcyclohexane, neo-hexane, and 2,2,3 trimethylbutane. Such intermediate sized hydrocarbons are known as heavy hydrate formers (HHF). Common for the HHFs is their relatively low solubility in water. This characteristic may be attractive when considering, e.g., desalination or wastewater treatment where the main purpose of hydrate formation is to produce a cleaner water phase (SECOHYA, 2007).
Table 1.5. Literature experimental studies for hydrate phase equilibria of gas mixtures containing CO$_2$ + CH$_4$, N$_2$ and H$_2$.

<table>
<thead>
<tr>
<th>Year</th>
<th>Authors and Coauthors</th>
<th>System</th>
<th>Notes</th>
</tr>
</thead>
<tbody>
<tr>
<td>1949</td>
<td>Unruh and Katz</td>
<td>CO$_2$ + CH$_4$ + H$_2$O</td>
<td>Reported phase equilibrium data and determined vapor phase concentration indirectly</td>
</tr>
<tr>
<td>1971</td>
<td>Robinson and Mehta</td>
<td>CO$_2$ + H$_2$O</td>
<td>Measured CO$_2$ hydrate phase equilibrium at $T = 274$ – 283 K and $p = 1.3$ – 4.5 MPa</td>
</tr>
<tr>
<td>1983</td>
<td>Berecz and Balla-Achs</td>
<td>CO$_2$ + CH$_4$ + H$_2$O</td>
<td>Hydrates exhibited instability at CO$_2$ mole fraction &gt; 50%</td>
</tr>
<tr>
<td>1991</td>
<td>Adisasmito and coworkers</td>
<td>CO$_2$ + CH$_4$ + H$_2$O</td>
<td>Confirmed and extended Unruh and Katz data. Demonstrated feasibility of using gas hydrates as separation method of CO$_2$ from CH$_4$-rich gases.</td>
</tr>
<tr>
<td>1996</td>
<td>Ohgaki and coworkers</td>
<td>CO$_2$ + CH$_4$ + H$_2$O</td>
<td>Measured $P$ and compositional (L$_w$–H–V) equilibrium data at 283 K</td>
</tr>
<tr>
<td>1997</td>
<td>Spencer</td>
<td>CO$_2$ + H$_2$ + H$_2$S + H$_2$O</td>
<td>Patented the principle of CO$_2$ capture by gas hydrate crystallization</td>
</tr>
<tr>
<td>1999</td>
<td>Fan and Guo</td>
<td>CO$_2$ + CH$_4$ + H$_2$O, CO$_2$ + N$_2$ + H$_2$O</td>
<td>Concluded that a 3.48 mole % CH$_4$/CO$_2$ slightly increases the hydrate formation pressure and N$_2$ significantly increases hydrate formation pressure compared to pure CO$_2$ hydrates</td>
</tr>
<tr>
<td>2000</td>
<td>Seo and coworkers</td>
<td>CO$_2$ + CH$_4$ + H$_2$O, CO$_2$ + N$_2$ + H$_2$O</td>
<td>Measured (H-Lw-V) equilibrium dissociation conditions and hydrate and vapor phase compositions</td>
</tr>
<tr>
<td>2001</td>
<td>Kang and coworkers</td>
<td>CO$_2$ + N$_2$ + H$_2$O</td>
<td>Studied $p$-$T$ ranges of hydrate stability with and without hydrate promoter. Demonstrated high pressure requirements in the case without additive</td>
</tr>
<tr>
<td>2002</td>
<td>Hachikubo and coworkers</td>
<td>CO$_2$ + CH$_4$ + H$_2$O</td>
<td>Reported (L$_w$-H-V) equilibrium data</td>
</tr>
<tr>
<td>2004</td>
<td>Tajima and coworkers</td>
<td>CO$_2$ + N$_2$ + O$_2$ + H$_2$O</td>
<td>Compared various CO$_2$ separation processes and showed that gas hydrate technology consumes the largest amount of energy due to the higher pressure conditions required to form hydrates</td>
</tr>
<tr>
<td>2005</td>
<td>Uchida and coworkers</td>
<td>CO$_2$ + CH$_4$ + H$_2$O</td>
<td>Measured the change of vapor-phase composition using gas chromatography and Raman spectroscopy</td>
</tr>
<tr>
<td>2005</td>
<td>Sugahara and coworkers</td>
<td>CO$_2$ + H$_2$ + H$_2$O</td>
<td>Investigated isothermal phase equilibrium (pressure–composition in the gas phase) in the presence of gas hydrate phase</td>
</tr>
<tr>
<td>2006</td>
<td>Kumar and coworkers</td>
<td>CO$_2$ + H$_2$ + H$_2$O</td>
<td>Determined incipient equilibrium hydrate formation conditions</td>
</tr>
<tr>
<td>2007</td>
<td>Duc and coworkers</td>
<td>CO$_2$ + H$_2$O, N$_2$ + H$_2$O, CO$_2$ + N$_2$ + TBAB + H$_2$O</td>
<td>Compared equilibrium pressure of CO$_2$ and N$_2$ pure hydrates with and without TBAB. Concluded hydrate crystallization pressure decreases by a factor from 10 to 50 for both CO$_2$ and N$_2$ hydrates when adding TBAB</td>
</tr>
<tr>
<td>2007</td>
<td>Linga and coworkers</td>
<td>CO$_2$ + N$_2$ + H$_2$O, CO$_2$ + H$_2$ + H$_2$O</td>
<td>Provided basic thermodynamic and kinetic data for conceptual process design</td>
</tr>
<tr>
<td>2008</td>
<td>Beltran and Servio</td>
<td>CO$_2$ + CH$_4$ + H$_2$O</td>
<td>Measured (L$_w$–H–V) equilibrium conditions and gas phase compositions</td>
</tr>
<tr>
<td>2008</td>
<td>Brusgaard and coworkers</td>
<td>CO$_2$ + N$_2$ + H$_2$O</td>
<td>Measured (L$_w$–H–V) equilibrium conditions including gas phase compositions</td>
</tr>
</tbody>
</table>
In oil and gas separation, and storage and transportation applications, where the purpose of the additives is to boost the conversion of gas into hydrates, it may be, however, desirable to be able to separate the hydrate promoters from the remaining hydrate formers under atmospheric pressure. This makes the use of water-soluble hydrate formers as promoters an attractive option. Various organic compounds belong to the group of water-soluble hydrate formers.

Examples are acetone, ethylene oxide, trimethylene oxide, tetrahydrofuran (THF), 1,3-dioxalane, 1,3-dioxane, and 1,4-dioxane (Kang et al., 2001; Seo et al., 2001; Mandal & Laik, 2008). In fact, the hydrate promotion effects of THF have been extensively studied (Kang et al., 2001; Seo et al., 2001; Lee et al., 2005; Delahaye et al., 2006; Sabil, 2010). Especially, since it forms, at atmospheric pressure, the same crystal structure (sII hydrate) as those formed (generally at elevated pressures) by several natural gas hydrate-formers. Nevertheless, most of the above mentioned substances are not suitable for practical purposes because of their high costs, toxicity or volatility.

Among the variety of thermodynamic additives that have been proved to reduce the operative conditions of gas hydrates formation, tetraalkyl ammonium salts, such as Tetra n-Butyl Ammonium Bromide (hereafter, TBAB), have the advantage of being stable at atmospheric pressure (Kamata et al., 2004), more environmentally friendly and easy to handle. Other features of using ammonium salts additives as hydrate promoters include an overall increase in the CO$_2$ capture rate of up to 90 % (Figueroa et al., 2004).

1.2.8 TBAB Semi-Clathrates

A different type of clathrate compound with large organic functional groups, known as ‘semi-clathrates’ (sc), is formed in the presence of tetra-alkylammonium or quaternary ammonium salts (Jeffrey, 1984). The formation of hydrates from such ionic compounds was, perhaps, first studied by Fowler and coworkers in 1940 and further investigated by McMullan and Jeffrey in 1959, Davidson (1973) and later by Dyadin and Udachin in 1984.
A large number of quaternary ammonium salts, generally denoted TBAX (with X being bromide, chloride, fluoride, nitrate etc), are known to form semi-clathrates. For instance, as shown in Figure 1.12, Tetra-n-Butyl Ammonium Fluoride (TBAF) has shown to drastically increase the temperature required for forming CO$_2$ semi-clathrates compared to TBAB and Tetra-n-Butyl Ammonium Chloride (TBAC) hydrate promoters (Li et al., 2010). On the other hand, TBAB is considered a non-volatile, non-flammable and non-toxic compound (Tanasawa & Takao, 2002; Obata et al., 2003; Chatti et al., 2005). Furthermore, TBAB has been suggested in potential alternatives to industrial/flue gas separation (Shimada et al., 2003; Kamata et al., 2004; Duc et al., 2007), H$_2$ storage (Chapoy et al., 2007), transport processes (Fukushima et al., 1999; Hashimoto et al., 2006), etc., with promising results. Therefore, the present investigation focuses on TBAB as thermodynamic hydrate promoter.

Figure 1.11. Promotion effect of various quaternary ammonium salts on the phase equilibrium conditions of CO$_2$ clathrate hydrates, as reported by Li et al. (2010). Symbols represent phase boundaries for (CO$_2$ + TBAC), (CO$_2$ + TBAB), and (CO$_2$ + TBAF) semi-clathrates in 2.93 · $10^{-3}$ mole fraction of thermodynamic additive in aqueous solutions. Solid line represents the phase boundary of CO$_2$ clathrate hydrates without additive (predicted by CSMGem hydrate model).
In TBAB semi-clathrates ((C\(_4\)H\(_9\))\(_4\)N\(^+\)Br\(^-\)\(\cdot\)qH\(_2\)O), the bromide anions (Br\(^-\)) are hydrogen-bonded and selectively incorporated into the water lattices, while the tetra-n-butyl ammonium cations (TBA\(^+\)) behave as guest species (Jeffrey, 1984). As shown in Figure 1.13, in pure TBAB hydrate crystal with water molecules, the Br\(^-\) anion takes part of the crystal framework, while TBA\(^+\) is located in the middle of a tetragonal cage arrangement. The shaded circles illustrate the empty dodecahedral (5\(^12\)) cages available for separating small gas molecules, such as CH\(_4\) (Shimada et al., 2005).

As TBAB forms different hydrate crystal structures depending on the initial concentration of TBAB in aqueous solution and on temperature (Lipkowski et al., 2002), their structural behavior is quite complex and it has not been fully established. The temperature-composition phase diagram given in Figure 1.14, shows the two types of TBAB crystalline structures typically formed at atmospheric pressure, namely type A and type B. Morphologically, type A has been described to have a columnar (tetragonal) shape, while type B has an undefined (orthorhombic) form composed of thin crystals (Dyadin & Udachin, 1984; Oyama et al., 2005). From structural point of view, type B has been reported to have two TBAB cations and 76 H\(_2\)O molecules (Shimada et al., 2005). Furthermore, Oyama et al. (2005) reported a concentration of 18 wt.% as the intersection between the equilibrium curves of these two crystals. A maximum stability is observed at about 40 wt.% for type A (Shimada et al., 2003) and near 32 wt.% (Oyama et al., 2005) for type B. Additionally, the hydration number in TBAB semi-clathrate has been reported to vary from 2.03 to 36.0 (Lipkowski et al., 2002). Other hydration numbers of 26.0 and 38.0
have also been reported for type A and type B, respectively (Oyama et al., 2005), accounting for the number of unique crystal structures formed.

Figure 1.13. Temperature-composition phase diagram of (TBAB + H₂O) semi-clathrates under atmospheric pressure (Jeffrey & McMullan, 1967; Arjmandi and coworkers, 2007). Symbols represent experimental data and figures along the composition lines stand for hydration numbers.

Figure 1.14. Carbon dioxide + TBAB semi-clathrates phase boundary. Symbols represent experimental data at different concentrations of TBAB in aqueous solutions. Solid line is the carbon dioxide hydrate phase boundary predicted by HWHYD model (Arjmandi et al. 2007).
Various gas molecules such as CO$_2$, CH$_4$, N$_2$, H$_2$ and H$_2$S, are likely of being selectively encaged in TBAB sc hydrates (Oyama et al., 2005). Thus, the phase equilibria of TBAB semi-clathrates in the presence of the above gases have been a subject of numerous investigations in the last decade. For instance, Chapoy et al. (2007) measured dissociation conditions for (H$_2$ + TBAB) and (H$_2$ + TBAF) semi-clathrates. They compared the dissociation pressures to those of H$_2$ and (H$_2$ + THF) clathrate hydrates and suggested that H$_2$ is most likely enclathrated in (H$_2$ + TBAB) and (H$_2$ + TBAF) semi-clathrates. In addition, they reported an increased storage capacity in semi-clathrates of one order of magnitude (at 1 MPa), compared to that of (H$_2$ + THF) clathrates.

Duc et al. (2007) demonstrated that the presence of TBAB considerably decreases the formation pressure of simple hydrates (CO$_2$ or N$_2$) and mixed hydrates (CO$_2$ + N$_2$). Their experimental results suggest that CO$_2$ selectivity in the hydrate phase can be increased at least by four times compared to that of the gas phase. Also, a gas storage capacity of 30-35 (volume of gas per volume of hydrate) can be obtained for mixed hydrates (CO$_2$ + N$_2$ + TBAB). A representative phase diagram obtained by Arjmandi et al. (2007) for (CO$_2$ + TBAB) sc at different concentrations of TBAB in aqueous solutions is given in Figure 1.15. In their work, Arjmandi and coworkers concluded that hydrates formed from (CO$_2$ + TBAB) are more stable than (CO$_2$ + H$_2$O) hydrates.

The effect of 0.293 mole % TBAB on CO$_2$ separation efficiency from CO$_2$ (16.60 mole %) + N$_2$ binary mixtures by formation of semi-clathrate hydrates at 277.7 K and feed pressures ranging from 3.36 to 7.31 MPa was studied by Fan et al. (2009). Their results demonstrated that CO$_2$ could be remarkably enriched in the hydrate phase in the presence of TBAB even under lower feed pressure. In the same year, equilibrium formation pressures of CO$_2$ (0.159 mole fraction) + N$_2$ + TBAB were reported by Lu et al. (2009) at (0.05; 0.153; 0.348; 0.407 and 0.457) TBAB mass fraction in the temperature range of (278.05 to 287.85) K.

Deschamps and Dalmazzone (2009) measured hydrate dissociation temperature and pressure conditions for the formation of semi-clathrates from a CO$_2$ (0.249 mole fraction) + N$_2$ gas mixture in the presence of 0.4 mass fraction TBAB in aqueous solution using differential scanning calorimetry (DSC) technique. The effect of TBAB concentration on the dissociation
conditions of sc formed from flue gas mixtures has been recently investigated by Meysel et al. (2011). They reported three-phase (solid + liquid + vapor) equilibrium conditions for semi-clathrate formation from three binary mixtures of (CO$_2$ + N$_2$), with cylinder compositions of (0.20, 0.50 and 0.75 mole fraction of CO$_2$) in solutions of (0.05, 0.10 and 0.20) mass fraction TBAB.

In spite of the increasing number of investigations related to TBAB semi-clathrate, the role of this additive in the selective removal of CO$_2$ from multi-component gas streams is not fully understood. Thermodynamic data available in the literature are rather scarce. In addition, only two thermodynamic predictive approaches (Mohammadi et al., 2010; Paricaud, 2011) have been proposed so far for semi-clathrates of (H$_2$ + TBAB) and (CO$_2$ + TBAB). Thus, there is a significant opportunity for investigating the phase equilibria of CO$_2$ containing gas mixtures in TBAB aqueous mixtures. Especially, as these data are required not only for practical purposes, but also for developing thermodynamic models capable of predicting the phase behavior of semi-clathrates.

1.3 Objective and Scope of the work

This work addresses the previous discussed limiting aspects of hydrate phase equilibria of CO$_2$ containing gas mixtures in the presence of TBAB aqueous solutions.

Provided that gas hydrates offer the possibility for developing a novel technology for CO$_2$ separation from flue and industrial gases, the conceptual design of a separation process based on gas hydrate crystallization requires reliable phase equilibrium data of CO$_2$ gas mixtures under hydrate forming conditions. As indicated earlier, compositional measurements need to be carried out to characterize the involved phases. With this intention, the following gas mixtures: (CO$_2$ + CH$_4$), (CO$_2$ + N$_2$) and (CO$_2$ + H$_2$), relevant to CCS technologies based on gas hydrates are studied. In addition, the phase equilibria of some of these gases are investigated in the presence of TBAB aqueous mixtures. The aim of this thesis is:

*To provide reliable experimental data on the hydrate phase equilibria of gas mixtures containing CO$_2$ in the presence of pure water and TBAB aqueous solutions, as a function of the*
concentration of TBAB and temperature, to enhance the fundamental knowledge of hydrate formation and dissociation from thermodynamics point of view.

The specific objectives and expected contributions of this thesis are as follows:

- To develop a new experimental set-up for gas hydrates phase equilibria studies. A significant outcome is expected in terms of the accuracy of the data measured, the apparatus suitability for (gas-liquid-hydrate) equilibrium measurements at high pressures, and the incorporation of a capillary sampling device coupled with gas chromatography for compositional analysis.

- Determination of the hydrate dissociation conditions and compositional data for: (a) (CO$_2$ + CH$_4$), (CO$_2$ + N$_2$) and (CO$_2$ + H$_2$) hydrates; and (b) CO$_2$, CH$_4$, N$_2$ and (CO$_2$ + N$_2$) semi-clathrates in the presence of TBAB aqueous solutions. Better understanding of the thermodynamic stability of the above systems, along with the most favorable process operating conditions (temperatures and pressures) and separation efficiencies (compositions) are expected to be obtained from these measurements.

- Elucidation of the effect of TBAB on the equilibrium conditions of CO$_2$, CH$_4$, N$_2$ and (CO$_2$ + N$_2$) semi-clathrates, for establishing the role of TBAB as thermodynamic promoter.

- Investigation of the reliability of thermodynamic models predictions for CO$_2$ hydrate-forming systems.

This thesis consists of seven chapters. Having examined the industrial context, along with current state-of-the-art of phase equilibrium studies for CO$_2$ hydrate-forming systems in this introductive chapter and with the objectives of the thesis established; the following chapter covers the theoretical basis for the experimental determination of thermodynamic properties of gas hydrates. The principles and preferred experimental procedures, along with the criteria for establishing equilibrium are also discussed in the 2$^{nd}$ chapter. Besides, other experimental issues, such as the calibration of measuring devices, uncertainties, and the determination of the phase compositions in equilibrium with gas hydrates are addressed as well in the 2$^{nd}$ chapter.
The core of the comprehensive experimental work carried out throughout this thesis is presented in Chapters 3 to 6. Phase equilibrium measurements of gas hydrates of (methane + carbon dioxide), which were performed using an existent apparatus, are the subject of the 3rd chapter. The generated hydrate dissociation data along with literature data are compared with the predictions of a thermodynamic model and a literature empirical equation, discussions are made on the deviations between experimental and predicted data. Comparisons are also presented with literature data. The identification of pertinent experimental difficulties encountered and the need of measuring reliable compositional data for mixed hydrate systems at high pressures and in the presence of corrosive gases provided the justification for developing a new and more versatile experimental set-up.

A combination of new and adopted features from the literature was thus considered in the design of the new apparatus. The development of the new equipment, based on the ‘static-analytic’ technique with capillary gas phase sampling, is detailed in Chapter 4. The apparatus incorporates precise and accurate measuring devices and the visual observation of the presence of gas hydrates and phase behavior, with promising results. As an example, new hydrate dissociation and compositional data measured for (CO\textsubscript{2} + CH\textsubscript{4} + H\textsubscript{2}O) systems are presented in the 4th chapter.

In the 5th chapter, the phase equilibria for gas hydrates of (CO\textsubscript{2} + N\textsubscript{2} + H\textsubscript{2}O) and (CO\textsubscript{2} + H\textsubscript{2} + H\textsubscript{2}O) are investigated. The conditions at which CO\textsubscript{2} separation is thermodynamically favored and the effect of the composition of the feed on the equilibrium dissociation pressures are discussed. Moreover, comparisons with literature data are presented and analyses are provided on the deviations obtained between experimental and predicted data using two thermodynamic literature models for the (CO\textsubscript{2} + N\textsubscript{2} + H\textsubscript{2}O) systems.

The 6th chapter is devoted to experimental measurements of gases in TBAB aqueous mixtures. The promotion effect of TBAB is thoroughly discussed in this chapter. In addition, optimum operating conditions for separating CO\textsubscript{2} from flue gases are proposed based on the experimental data.

In the 7th and final chapter of this thesis, the general concluding remarks are presented together with some directions for further investigating the thermodynamics of semi-clathrates.
Experimental Methods and Analysis Techniques for Gas Hydrates Phase Equilibrium Measurement

“The ultimate goal of phase diagram calculations is the prediction of diagrams within the experimental uncertainty. Evidently, it is advisable to know what the experimental uncertainty is!”

“... there is no experimental method that is always superior to all others; instead, all methods have their merits, but also their blind spots.”

“The choice of the experimental method is one of the factors which determine the accuracy and the reliability of the experimental data.”

Résumé

Dans ce chapitre, nous fournissons les formalismes théoriques pertinents en relation avec la détermination expérimentale des propriétés thermodynamiques de systèmes contenant des hydrates de gaz. L'accent est mis principalement sur les techniques expérimentales concernant les pressions modérées et relativement élevées. Les appareils les plus courants et les procédures expérimentales utilisées y sont décrites. Les principes, le choix des techniques utilisées et les critères en vue d'établir un équilibre sont expliqués. De plus, nous discutons l'étalonnage des différents capteurs et du détecteur du chromatographe en phase gazeuse, les incertitudes expérimentales correspondantes, l'échantillonnage difficile des fluides et la détermination des compositions des phases à l'équilibre pour les mélanges de gaz.

Abstract

In this chapter the theoretical formalisms relevant to the experimental determination of thermodynamic properties of systems containing gas hydrates are provided. Emphasis is given to experimental techniques at pressures ranging from moderate to relatively high pressures. The most common devices and experimental procedures employed are described. The principles, the choice of the techniques used and the criteria for establishing equilibrium are explained. Likewise, the calibration of measuring sensors and gas chromatograph detector, the corresponding experimental uncertainties, and the challenging fluid sampling and determination of the equilibrium phase compositions for gas mixtures are discussed.
2 Experimental Methods and Analysis Techniques for Gas Hydrates Phase Equilibrium Measurement

2.1 Overview

Design, development and operation of chemical processes require a cyclical and interactive strategy involving conceptual, experimental, modeling and simulation stages (Richon, 2009). A proper design process should follow the sequence from conception of ideas through literature review, selection, design and construction of equipment, methods, tests and set up, measurements, data reliability and consistency tests to the final implementation, as depicted in Figure 2.1.

The development of new technologies based on gas hydrates crystallization approach requires specific temperature and pressure conditions and the utilization of complex systems with many components that are beyond usual operations and existing databases. Moreover, industrial design relies on accurate modeling and modeling relies on reliable experimental data (Richon, 2009). Thus, experimental thermodynamics are of industrial significance.

Figure 2.1. Process design strategy (adapted from Richon, 2009 and Soo, 2011). The highlighted blocks indicate the stages addressed in this research.
Suitable combination of temperature and pressures above the gas-hydrate-liquid phase boundary is normally required for hydrate formation. Therefore, phase behavior studies for systems containing gas hydrates are mainly concerned with experimental techniques suited for pressures ranging from moderate to relatively high pressures, so only these types of techniques are concisely discussed.

A variety of methods have been developed for high-pressure fluid phase equilibria measurement. Nonetheless, their suitability will depend on the application, the system under investigation, the properties to be measured and the required accuracy. Several review articles on this subject are available in the literature. For instance, some of the most meaningful contributions possibly are: The Volume VII of The International Union of Pure and Applied Chemistry (IUPAC) monograph series on ‘Experimental Thermodynamics’ (Weir & de Loos, 2005), which contains a valuable state-of-the-art covering thermodynamic measurement techniques for multicomponent mixtures. Also, the series of reviews published by Dohrn and coworkers (1995, 2002, 2010, 2011) that not only provide a compilation of systems for which high-pressure phase-equilibrium data have been investigated over the past three decades, but a classification scheme of experimental methods as well. Moreover, the advancements on accurate and effective experimental equipment for phase equilibrium measurements are examined by Richon (1996) and Richon and de Loos (2005); and the broad range of static and dynamic equipment are reviewed by Raal and Mühlbauer (1998).

Richon (1996) and Dohrn et al. (2010) propose different classifications of experimental methods for the determination of high-pressure phase equilibria. Both classifications share several similarities, however, the one proposed by Richon (1996) is based on the method of equilibration between phases in equilibrium, whereas Dohrn et al. (2010) classify the different experimental methods according to the way compositions of the equilibrium phases are measured and whether the mixture to be investigated is prepared with precisely known composition or not, namely ‘analytical methods and synthetic methods’ (Deiters & Schneider, 1986).

Even if classification of the methods for measuring phase equilibria is not straightforward, returning to the classification proposed by Richon (1996) and Richon and de Loos (2005),
essentially two main categories are distinguished: dynamic (open circuit) methods involve forced circulation of one or more phases, whereas in static methods (closed circuits) equilibrium can be achieved with or without recirculation of fluid phases, generally using an internal stirring mechanism to reduce the time required for reaching equilibrium (Raal & Mühlbauer, 1998). Refined schemes based on this classification can be found in the book of Raal and Mühlbauer (1998) and in the doctoral dissertation of Afzal (2009).

Based on the above classification, this work takes advantage of a combination of features from static, analytical and synthetic methods and the use of modern measuring devices and materials to bring about a new perspective for performing hydrate phase equilibrium measurement. In particular, special attention is given to the precision and accuracy of the results obtained. The principles, the choice of the techniques used and the criteria for equilibrium are presented in this chapter. In addition, the calibration of measuring sensors and gas chromatograph detector, experimental uncertainties and the determination of the equilibrium phase compositions for gas mixtures are discussed.

2.2 Visual versus Non-visual Techniques

A further distinction among the most frequently used experimental methods for determining hydrate equilibrium conditions can be made between those based on visual and non-visual means of hydrate detection. Particularly at low pressures, visual observation of the formation and dissociation of hydrate crystals was successfully implemented in a Pyrex tube flow apparatus by Hammerschmidt in 1934 and in a windowed cell by Deaton and Frost in 1937 (Sloan & Koh, 2008).

As the above method requires the visual observation of hydrate crystals (at constant temperature or pressure) it may only be used at temperatures above the freezing point of water to avoid any confusion with ice crystals (Schroeter et al., 1983). Also time for equilibration might take several hours, thus it may become somewhat time consuming. As an alternative, hydrate phase equilibrium measurement at high and low pressures can be performed in a constant volume
(isochoric) cell without need of visual observation and the intersection point of the cooling and heating isochors is considered the dissociation condition.

Three modes have been thus established for operating a hydrate formation apparatus: isobaric, isothermal and isochoric (Sloan & Koh, 2008). Table 2.1 summarizes the fundamentals of each method. The feasibility of using isothermal method for measuring hydrate dissociation pressures has been recently investigated for \((\text{CO}_2 + \text{H}_2\text{O})\) system in a titanium variable volume cell (Fontalba et al., 1984), with promising results (D. Richon, Personal Communication, March 9, 2012). As equilibrium is reached within 5 minutes, a significant amount of time could be potentially saved using this technique for measuring hydrate dissociation data. The hydrate dissociation pressure is identified by the presence of a plateau in a pressure versus piston-displacement plot. The composition of the hydrate phase can be determined from the PVT data and the amount of gas released during hydrate dissociation (known from the width of the plateau). For multicomponent systems additional calculations are required, possibly compromising the accuracy of the obtained equilibrium data.

The hydrate dissociation point is a repeatable thermodynamic equilibrium point (Tohidi et al., 2000) and is defined as the temperature and pressure condition where the last hydrate crystal melts (Gjertsen & Fadnes, 2006).

Table 2.1. Commonly used experimental procedures for measuring hydrate dissociation conditions (Sloan & Koh, 2008).

<table>
<thead>
<tr>
<th>Method</th>
<th>Principle</th>
<th>Hydrate formation</th>
<th>Hydrate dissociation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Isothermal</td>
<td>Constant temperature</td>
<td>Temperature increase</td>
<td>Visual observation of hydrate crystal disappearance</td>
</tr>
<tr>
<td>Isobaric</td>
<td>Constant pressure</td>
<td>Exchange of gas or liquid from an external reservoir</td>
<td></td>
</tr>
<tr>
<td>Isochoric</td>
<td>Constant volume</td>
<td>Pressure decrease</td>
<td>Intersection point of cooling and heating isochors (nonvisual technique)</td>
</tr>
</tbody>
</table>
Therefore, in all three procedures hydrate dissociation is used to determine the hydrate dissociation \((p, T)\) condition. In the isothermal and isobaric methods, the equilibrium condition is determined (at constant pressure or temperature, respectively) by visual observation of a phase change, e.g. hydrate crystals disappearance. Whereas a corresponding change in pressure as a function of temperature (due to density changes) in a constant volume cell indicates hydrate formation and/or dissociation in the isochoric method described below.

### 2.3 The Isochoric Method

Hydrate dissociation data can be accurately determined using an isochoric apparatus. The technique is based on the classical isochoric procedure developed in Professor Kobayashi’s laboratory (Marshall et al., 1964) and further improved by Tohidi and coworkers (2000), who outlined the impact of measuring techniques, mixing efficiency, heating method and heating rate on the accuracy of hydrate dissociation point measurements.

In a typical isochoric experiment, hydrates are formed by decreasing the system temperature. The differential pressure change \(\partial p\) is measured with respect to the accompanying differential temperature change \(\partial T\) in a constant volume cell. For each load of known composition, pressure is monitored as a function of temperature making possible the determination of a \(p-T\) isochor (Richon & de Loos, 2005). The quantity \((\partial p/\partial T)_V\) represents the slope of an isochoric path in a \(p-T\) phase diagram. Hydrates are then dissociated through stepwise heating. The intersection of the cooling and heating curves represents a phase transition, thereby indicating the hydrate dissociation \((p, T)\) point (Ohmura et al., 2004). By plotting several experimental isochors obtained at different pressures for a given load, the complete hydrate phase boundary of a system is obtained.

In the isochoric method, the equilibrium condition is established through temperature and pressure measurement. No visual observation or complicated calculations are required, allowing a reliable determination of hydrate equilibrium data. Additionally, the technique is suitable over the entire range of hydrate formation temperatures and pressures, and fewer amounts of fluids...
are used, as no volume changes are required. Furthermore, it is suited to automated control of experiments (Rivollet, 2005; Khalil, 2006). Thus, isochoric methods are considered rather advantageous to investigate the phase behavior of multicomponent mixtures, compared to isobaric and isothermal approaches with visual observation requirement. For the above reasons, the isochoric method combined with stepwise heating and efficient mixing (Tohidi et al., 2000) is applied in the present investigation.

2.4 Apparatuses for the Determination of Hydrate Phase Equilibria

It is beyond the scope of this work to provide an exhaustive review of the experimental equipment that have been employed for measuring hydrate phase equilibria. The features of the most commonly used apparatus and experimental techniques considered in this section have been mainly derived from the excellent review of Sloan and Koh (2008), with the addition of representative examples from the literature in order to illustrate their main advantages, but also some of the experimental difficulties typically encountered. Three proven experimental approaches representative of current developments are mentioned in the following paragraphs.

The static technique is one of the classical procedures for measuring hydrate phase equilibrium data, especially at high pressures. The starting point of contemporary experimental studies carried out in static apparatuses is that of Deaton and Frost (1937). In their apparatus, a glass windowed equilibrium cell, shown in Figure 2.2, was placed in a thermo-regulated bath. The cell was equipped with a valve system to allow for inlet and outlet gas flow regulation. The use of thermocouples and pressure transducers enabled measurement of temperatures and pressures. The protocol in obtaining phase equilibrium data involved visual confirmation of hydrate formation and disappearance. The above basic principles have not significantly changed over the past decades. Indeed, recent advances in the design of hydrate phase equilibria static equipment incorporate modern measuring instruments that improve experimental uncertainties; designs and materials that extend the operating ranges, careful construction and operation to investigate unusual conditions and systems; improvements in the data acquisition and minimization of monotony.
Although accurate and thermodynamically consistent data can be obtained through static and dynamic approaches, static methods are generally preferred for the determination of phase equilibrium data (Oellrich, 2004). Some of the main advantages of static devices include:

- The simplicity of the technique and experimental set-up
- It can be applied at any temperature and over a wide pressure range
- Suitable for single and multiple component systems, allowing reliable evaluation of industrial systems
- Easy modification of total compositions and quantities of fluid samples
- Small amount of material needed
- Possibility of observing the phase behavior at high pressures

Time required to ensure that the system has achieved thermodynamic equilibrium remains still a major drawback for the determination of hydrate phase equilibria under static conditions, making it a quite time consuming method, especially when long metastable periods occur.

The Quartz Crystal Microbalance (QCM) exploited by Tohidi and coworkers (Burgass et al., 2002; Mohammadi et al., 2003) is an example of an alternative experimental approach suitable for measuring equilibrium data of gas hydrates (Figure 2.3). The QCM consists of a thin disk of quartz placed between two electrodes. Crystal oscillation at a particular resonant frequency is activated when an electric current passes across the electrodes. Hydrate formation is then detected by a change in the resonance frequency once hydrates have adhered to the surface of the

Figure 2.2. Detail of Deaton and Frost’s hydrate formation equilibrium cell (as cited by Sloan & Koh, 2008).
quartz crystal. Pressure and temperature of the system are measured using a pressure transducer and a thermocouple in a high pressure cell (Sloan & Koh, 2008).

The main advantage of QCM method is that it uses small amounts of samples (~ one droplet of water), resulting in a significant reduction in the time required for each experiment (Mohammadi et al., 2003). Although the QCM method has been considered unfeasible (Sloan & Koh, 2008) due to good contact requirement between the surface of the quartz crystal and hydrates, Lee et al., (2012) have recently demonstrated that by modifying the droplet size, this method yields acceptable results, especially, for rapid and practical gas hydrate application purposes, i.e. selecting a hydrate promoter from among various candidates.

Figure 2.3. (a) Schematic diagram of the QCM, and (b) the QCM mounted within a high pressure cell (Burgass et al., 2002 and Mohammadi et al., 2003, as cited by Sloan & Koh, 2008).
Figure 2.4. High-pressure micro DSC VII measurement device (Deschamps & Dalmazzone, 2009).

Most recently the use of calorimetric methods such as DSC has been extended to the determination of hydrate phase equilibria data and thermal property data for gas hydrates. A micro-DSC analyzer coupled with special high-pressure vessels, namely High Pressure Differential Scanning Calorimetry (HP-DSC) technique was introduced by Dalmazzone et al. (2002) to characterize the thermodynamic stability boundaries of methane and natural gas hydrates in solutions of inhibitors. The same technique has been applied to investigate dissociation enthalpies and the phase equilibria of TBAB semi-clathrates with gases (Deschamps & Dalmazzone, 2009). The device, as shown in Figure 2.4, consists of a microDSC VII, which measures the difference in heat flow between the sample and reference material. It can operate at temperatures between (228.15 and 393.15) K and up to 40 MPa coupled to a pressure multiplicator.

The main advantage of the micro-DSC technique is that it provides thermodynamic and thermal data simultaneously. Compared to PVT techniques, microcalorimetry has been reported (Le Parlouër et al., 2004) to be relatively faster and to require smaller sample amounts (~ 5 mg). However, differences in thermodynamic properties measured through similar calorimetric
techniques can be significantly larger than stated experimental uncertainties. For instance, considerable scatter has been recently reported for the equilibrium temperatures of tetrabutylphosphonium bromide semi-clathrates, measured through DSC by different laboratories (Suginaka et al., 2012).

The above descriptions of selected devices and experimental procedures are meant to provide the underlying principles for investigating the phase behavior of gas hydrates. Each method has its own advantages and limitations. However, the one based on the static apparatus, potentially one of the simplest and most accurate approaches, is selected for this work. The apparatus is operated following a combination of static, analytic and synthetic procedures. Such approach allows simultaneous determination of the \((p-T)\) hydrate dissociation conditions and compositional: liquid \((x)\), gas \((y)\) and hydrate \((z)\), phase equilibrium data for the gas hydrate systems of interest in this investigation.

2.5 Static-Analytic-Synthetic Measurements

There is no universal experimental technique capable of fully characterizing the phase behavior of multicomponent systems over the whole range of temperature and pressures. For mixtures with more than two components the information obtainable by non-analytical methods is limited (Raal & Mühlbauer, 1998). Thus, a combined “static-analytic” and synthetic approach is applied for obtaining reliable hydrate phase equilibrium data of \(\text{CO}_2\) containing gas mixtures.

The hydrate dissociation conditions and the composition of the gas phase in equilibrium with the hydrate and liquid phases are determined via the so-called “static-analytic” technique, whereas a synthetic method is used to estimate the liquid and hydrate phase compositions (for systems containing pure water). Because sampling and analyzing liquid and hydrate phases is much more challenging, the combination of the above two methods in one set-up leads to the possibility of obtaining thermodynamic data of multiple phases simultaneously. An experimental set-up combining the above mentioned techniques has been developed within this research and it is fully described in Chapter 4.
The experimental procedure is as follows: a mixture of known composition is prepared in the equilibrium cell by introducing one component after the other. By accurately knowing the volume of the cell and the pressure and temperature of the mixture, the total number of moles and the composition of the feed can be precisely determined. Furthermore, the amount of liquid supplied to the cell is also precisely known. During the experiment temperature is varied following the isochoric pressure search method with stepwise heating and efficient mixing (Tohidi et al., 2000; Rovetto et al., 2006). After equilibrium has been obtained, small representative gas phase samples are withdrawn in situ without disturbing the equilibrium condition at each temperature step via an electromagnetic rapid online sampler-injector (ROLSI™) presented in detail in Chapter 4.

Compositional analysis is carried out through gas chromatography for the gas phase, whereas the liquid phase is analyzed at the reference temperature 293 K using a calibrated refractometer only for semi-clathrates formed from (CO₂ + N₂ + TBAB + H₂O). For systems investigated in the absence of TBAB, the compositions of the hydrate and aqueous phases are precisely calculated applying a material balance approach adopted from Ohgaki et al. (1996) in combination with the experimental data and volumetric properties, outlined in Chapter 4.

A pressure-temperature plot, as shown in Figure 2.5, is obtained from each experimental run. The intersection between the cooling and heating curves indicates the equilibrium transition from (hydrate + liquid + gas) to (liquid + gas) and hence is reported as the hydrate dissociation point. The procedure is repeated at different pressures in order to determine the hydrate phase boundaries over a wide temperature range.
Chapter 2 - Ph.D. Dissertation V. BELANDRIA

Figure 2.5. Hydrate dissociation conditions (HDC) determination following the isochoric pressure-search method and hydrate phase boundary (model predictions, HWHYD 2000) for the (0.748 mole fraction CO₂ + 0.252 mole fraction N₂ + water) system.

2.6 Gas Chromatography

Since the invention of the first gas chromatograph detector by British chemists James and Martin (1952) more than half a century ago, this instrumental technique also referred to as ‘gas-liquid partition chromatography’, has become widespread adopted for analyzing complex multi-component gas mixtures by industry and researchers. Up to 30 % of global gas chromatograph (GC) systems are currently implemented in Europe alone. The share is followed by United States and Japan.

Gas chromatography is a practical method of separation for analytical purposes. The type of GC used in this work involves separating the compounds of a gas mixture carried by the flow of an inert gaseous mobile phase (carrier gas), which are adsorbed onto the surface of an inert solid stationary phase. Figure 2.6 is a picture of the (Varian, CP3800) gas chromatograph used in this
work, with its main components: the injection system, the oven, the column (placed inside the oven) and the detector.

The gas sample is introduced, through the injector port, into the chromatographic column where separation takes place. The column is placed in the thermostated oven. The compounds of the mixture are separated throughout the column based on their affinity and interaction with the stationary phase, which translates into a characteristic gas chromatographic retention time. The thermal conductivity detector used in this work measures the heat conductivity of each separated compound that flows through the column, resulting in a peak area signal. The area of a peak in the chromatogram is proportional to the amount of each compound in the gas mixture. It must be noted that retention times in GC are extremely sensible to the column temperature and the carrier gas flow rate, which must be kept constant. The theoretical and practical aspects of this technique are treated in detail by Tranchant (1995).

Figure 2.6. Front view of the gas chromatograph used in this work and main components.
2.6.1 Chromatographic Conditions

Several tests were performed to find the best chromatographic conditions to achieve favorable response times and peak resolution (difference in the retention times) in the separation of (CO$_2$ and CH$_4$), (CO$_2$ and N$_2$) and (CO$_2$ and H$_2$) gas mixtures. Four main factors contribute to achieve this separation: column packing type, column temperature, carrier gas flow rate and physical properties of components (Raal & Mühlbauer, 1998). Thus, different columns with different lengths and different temperature programming conditions were tested. A good separation of components is found via a 4 m long column packed with 80-100 mesh Porapak Q. It was noticed that increasing the oven temperature, with the aim of reducing the retention times for these components, leads to difficulties in CO$_2$ and CH$_4$ separations.

The oven temperature was thus set to 323 K and the carrier gas used was helium (He) with a 25 ml/min flow rate, except for the compositional analysis of (CO$_2$ + H$_2$) gas mixtures, where N$_2$ was used as a carrier gas because of the proximity in the thermal conductivities of He and H$_2$. Proper GC operating conditions used in this work are given in Chapter 3. A typical chromatogram showing two peaks each with a different retention time ($t_{R1}$ and $t_{R2}$) for CO$_2$ and N$_2$ is presented in Figure 2.7.

![Gas chromatogram](image)

Figure 2.7. Gas chromatogram exhibiting an effective separation of a (0.748 mole fraction CO$_2$ + 0.252 mole fraction N$_2$) gas mixture.
2.7 Calibrating Measuring Devices and Experimental Accuracies

As hydrate phase equilibrium data with the highest possible accuracy are needed for developing reliable thermodynamic predictive tools and hydrate-based industrial processes, calibration of measuring instruments is a key concern in this work. The accuracy of the results depends to a large extent on the accuracy of measuring instruments. Thus, careful calibration of all measuring devices, *i.e.*, temperature probes, pressure transducers, gas chromatograph detectors and *etc.* was performed against reference instruments (Figure 2.8) prior to performing the experimental work and periodically checked to determine the accuracy with which data are measured.

Figure 2.8. Calibration equipment used in this work: Dead weight balance device, temperature bath with reference platinum resistance thermometer probe, variable volume cell with displacement transducer for volumetric calibrations and gas chromatograph with a gas tight calibration syringe (clockwise).
2.7.1 Pressure Sensors Calibration

Pressure inside the equilibrium cell is directly measured by calibrated capacitance pressure transducers. Druck™ (type PTX611) pressure transducers are maintained at a constant temperature higher than the highest temperature of the study to avoid any possible condensation on the pressure measuring system. Calibration is carried out against a dead weight balance (Desgranges & Huot 5202S CP, Aubervilliers, France) for ranges from (0.3 to 40) MPa.

Pressure calibration is performed by connecting the reference instrument to a source of pressure (often nitrogen) and to the inlet of the equilibrium cell. The calibration procedure consists on counter-balancing the total downward forces (i.e. gravitational force of a central piston with added weights, as well as the atmospheric pressure measured via a Druck (model DPI 141) digital barometer with that of the pressure exercised by nitrogen gas loaded into the cell. Once this is achieved, pressure readings from the cell pressure transducers are allowed to stabilize and are recorded against the real pressure, which is calculated from the weights added to the piston.

Figure 2.9. Relative uncertainty on pressure transducers calibration from (0.6 to 10.6) MPa. LPT: ▲, increasing pressure; △, decreasing pressure. HPT: ●, increasing pressure; ○, decreasing pressure; calibration uncertainty is the deviation between measured and calculated pressure.
Table 2.2. Pressure transducers calibration coefficients.

<table>
<thead>
<tr>
<th>Pressure Transducer</th>
<th>Calibration range / MPa</th>
<th>( p_{\text{cal}} = a p_{\text{read}}^2 + b p_{\text{read}} + c )</th>
</tr>
</thead>
<tbody>
<tr>
<td>LPT</td>
<td>0.3 - 6.1</td>
<td>( a = -2.064 \times 10^{-6} ) ( \text{MPa}^{-1} ) ( b = 0.1002 ) ( c = -4.340 \times 10^{-3} ) ( \text{MPa} )</td>
</tr>
<tr>
<td>HPT</td>
<td>0.3 - 10.6</td>
<td>( a = -6.218 \times 10^{-7} ) ( \text{MPa}^{-1} ) ( b = 0.1006 ) ( c = 2.667 \times 10^{-4} ) ( \text{MPa} )</td>
</tr>
</tbody>
</table>

Pressures read through the instrument and from the reference are fitted to a second order polynomial correlation, allowing true pressure values to be found. Table 2.2 gives the obtained calibration coefficients for low and high-pressure transducers (LPT and HPT, respectively). As an example, typical deviations observed through pressure transducer calibration are presented in Figure 2.9. Pressure measurement uncertainty is estimated to be within ± 0.002 MPa from the relative deviations shown in the latter experimental curve.

2.7.2 Temperature Probe Calibration

Temperature is measured via Pt-100 Platinum Resistance Thermometer (PRT) probes, which are calibrated against a 25 Ω PRT reference probe (TINSLEY type 5187 SA) with a certified calibration from the Laboratoire National d’Essais (LNE, Paris). Pt-100 sensors and the reference probe are submerged in a temperature bath (Lauda Ultra-Kryomat, Ruk 50) with ethanol and water (for low and higher temperature ranges, respectively).

The temperature of the bath is increased and decreased at uniform intervals from (210 to 360) K in order to detect any hysteresis within the sensors. Temperature signals are allowed to stabilize at each temperature step and are read out, within 0.01 K, on a micro-ohmmeter data Acquisition/Switch Unit (Hewlett-Packard, model 34420A). Similar to the procedure described above for the determination of equilibrium pressures, a plot of \( T_{\text{true}} \) against \( T_{\text{read}} \) results in a second order polynomial relation (Figure 2.10). The equation of this line is subsequently used to determine true temperature values. The maximum uncertainty on temperature measurement resulting from this calibration is within ± 0.02 K.
2.7.3 Volumetric Calibrations

As it is discussed later in Chapter 4, precise knowledge of the total volume of the equilibrium cell is crucial for the accurate determination of the compositions of the liquid and hydrate phases by mass balance approach. The internal volume of the cell is thus determined by using a variable volume cell (VVC) assembly, as shown in Figure 2.8. The VVC consists of a void cylinder of known internal diameter, a piston with appropriate O-ring and a displacement transducer fitted to the piston to record the variation on the linear displacement inside the cylinder. The VVC is connected to the equilibrium cell. All transfer lines; the equilibrium cell and the VVC assembly are evacuated. The VVC is filled with a pure liquid; ethanol is used for this purpose and the assembly is connected to a pressurizing fluid (i.e. nitrogen) to move the piston. The equilibrium cell and transfer lines are filled with ethanol. Pressure is monitored until an abrupt pressure increase is detected inside the cell. At this point, the length travelled by the piston is registered. The volume of the equilibrium cell is equivalent to the volume of liquid loaded into the cell, which is geometrically determined from the displacement of the piston and the cylinder internal diameter. The procedure is repeated at least three times to ensure reproducibility of the results and an average value is reported. The maximum uncertainty on the internal volumes obtained through this procedure are expected to be within $\pm 0.5 \text{ cm}^3$. 

Figure 2.10. Pt-100 Platinum resistance thermometer probe calibration.
2.7.4 GC Detector Calibration for Gas Mixtures

In order to determine a quantitative relationship between the response of the detector and the composition of gas mixtures separated by gas chromatography, a calibration of the Thermal Conductivity Detector (TCD) for each compound is performed. A direct injection calibration method (Raal & Mühlbauer, 1998) is used to achieve the accuracy of results required within the project. In this method, known volumes of pure components are directly injected into the GC via the injector port by using precision chromatography syringes (SGE Analytical Science; 50μL, 100μL, 250μL and 500μL Gas Tight Syringes) for preparing calibration standards and GC injections. TCD calibration is conducted once all analytical conditions (see section 2.6.1) of the chromatograph have been optimized to achieve satisfactory separation of (CO₂ and CH₄), (CO₂ and N₂) and (CO₂ and H₂) gas mixtures.

The TCD was calibrated for carbon dioxide, methane, nitrogen and hydrogen. The calibration curves were fitted to second-order polynomial equations relating the number of moles and area under the peaks from the chromatogram. The composition of the gas phase at a given \((p,T)\) condition is thus determined from the peak area ratio of the unknown sample and the coefficients of the corresponding polynomial equation for each compound. A typical calibration curve and the corresponding deviation results for CO₂ are shown in Figure 2.11. Similar deviations are obtained for CH₄, N₂ and H₂. Therefore, the uncertainty in measuring compositions of the gas phase through gas chromatography is estimated to be within ±1 - 2%.

Using the experimental procedure described earlier to measure hydrate equilibrium data for gas mixtures with and without TBAB, and assuming the corresponding standard uncertainties have a normal distribution, it is estimated that maximum overall uncertainty for pressure and temperature measurements, derived from isochoric plots, is within ± 0.05 MPa and ± 0.2 K, respectively. The maximum uncertainty in all measurements is attributed to the deviations in measuring compositions of the gas phase by gas chromatography. Such deviations are estimated to be within ± 1 – 2 % as explained above. Other uncertainties for the liquid and hydrate phases are expected to be better than 1 %. Therefore the overall uncertainty for compositional measurements is expected to be less than 2 %.
Figure 2.11. Thermal conductivity detector calibration for CO$_2$ using a 100 µl gas calibration syringe: second order calibration curve (left), calibration deviation (right).

2.7.5 Refractometer Calibration

A refractometer calibration was performed in order to determine the composition of the liquid phase at equilibrium with semi-clathrates formed from CO$_2$ + N$_2$ + TBAB aqueous solutions. Samples of (TBAB + water) mixtures were prepared in the concentration range from (0 to 0.50) mass fractions TBAB following the gravimetric method detailed in Chapter 6. Refractive index measurements were carried out at 293.15 K using an ABBE refractive index instrument, previously calibrated with deionized water and ethanol with accuracy greater than 2·10$^{-4}$.

Refractive indices ($n_D$) for the (TBAB + water) binary mixtures as function of compositions are plotted in Figure 2.12. It can be observed from the experimental results that $n_D$ exhibit a linear behavior over the investigated concentration range. The maximum accuracy on refractive index measurement are thus expected to be better than 0.1%.
2.8 Criteria for Equilibrium

The state for equilibrium, as previously discussed, implies a condition in which thermodynamic properties do not change over time. Since hydrates are slow to form near the dissociation point, relatively long periods are required for the pressure to come to equilibrium after a temperature change (Marshall et al., 1964). In order to ensure a true thermal equilibrium state while decreasing the time required to achieving this condition, especially in static methods, thorough mixing of the cell contents is essential. It has been demonstrated that step heating combined with adequate time at each temperature interval results in generating reliable experimental data (Tohidi et al., 2000). Moreover, as the heating rate has a strong impact on the accuracy of hydrate dissociation measurements (Tohidi et al. 2000; Rovetto et al. 2006), the dissociation part of the isochoric loop must be performed at a sufficiently slow heating rate of about 0.12 K/h to allow the system to reach equilibrium (Sloan & Koh, 2008).

Once the above conditions have been satisfied, stability in pressure, temperature, gas phase composition and refractive index are monitored to establish the attainment of equilibrium. Several gas phase samples are taken through ROLSI™ sampler and are analyzed by gas
chromatography at each temperature interval during hydrate dissociation. It is considered that equilibrium has been reached when the composition of the gas phase of at least five samples agree to within 0.001 molar fractions. At this point, average concentrations are registered as the gas phase composition at the corresponding temperature and pressure condition. An actual example of compositional analysis carried out to establish the attainment of equilibrium is given in Figure 2.13. A consistent detector response is exhibited throughout the entire temperature interval.

Figure 2.13. Chromatogram profile for a (0.151 mole fraction CO$_2$ + 0.849 mole fraction N$_2$) gas mixture in the presence of TBAB aqueous solution (mass fraction, $w = 0.05$) at $T = 287.0$ K and $p = 14.525$ MPa.
Phase Equilibria of Clathrate Hydrates of Methane + Carbon dioxide: New Experimental Data and Predictions†

† Content published in Fluid Phase Equilib. 2010, 296, 60-65.
Chapter 3 - Ph.D. Dissertation V. BELANDRIA

3

Résumé

Ce chapitre fournit des conditions de dissociation d'hydrates de gaz de (méthane + dioxyde de carbone) à des concentrations faibles, moyennes et élevées en dioxyde de carbone. Les mesures d'équilibres de phases ont été réalisées entre 279 et 290 K à pressions jusqu'à 13 MPa. Une méthode isochore dite "isochoric pressure-search method" a été utilisée pour effectuer les mesures. Les données de dissociation générées par cette étude ainsi que celles disponibles dans la littérature sont comparées aux prédictions via un modèle thermodynamique et via l'équation empirique décrite dans le chapitre précédent. Une discussion est faite au sujet des écarts entre données expérimentales et données prédites.

Abstract

This chapter provides dissociation conditions of gas hydrates of (methane + carbon dioxide) at low, medium and high concentrations of carbon dioxide. The phase equilibrium measurements were conducted in the temperature ranges from (279 to 290) K and pressures up to 13 MPa. An isochoric pressure-search method was used to perform the measurements. The dissociation data generated in this study along with the experimental data available in the literature are compared with the predictions of a thermodynamic model and a previously reported empirical equation. A discussion is made on the deviations between the experimental and predicted data.
3 Phase Equilibria of Clathrate Hydrates of Methane + Carbon dioxide: New Experimental Data and Predictions

3.1 Introduction

Because gas or clathrate hydrates have the capability to store/separate gases (Englezos, 1993, Sloan & Koh, 2008), the development of alternative technologies based on this concept has gained much attention in exploration and production activities within the oil and gas industry. Examples are carbon dioxide (CO$_2$) sequestration and methane (CH$_4$) recovery from natural gas hydrates in deep sea sediments (Oghaki et al., 1994), transport of natural gas as frozen hydrate (Gudmundsson et al., 1995), removal of high CO$_2$ content in natural gas by formation of gas hydrates (Azmi et al., 2010), etc. As methane is the predominant component of natural gas, reliable experimental data on the phase behavior of (CO$_2$ + CH$_4$) gas mixtures under hydrate forming conditions are thus required to enhance the understanding of natural gas hydrates and for process development purposes.

The first experimental study of (CH$_4$ + CO$_2$) hydrates was reported by Unruh and Katz (1949). Two decades later, Berecz and Balla-Achs (1983) reported that hydrates of (CO$_2$ and CH$_4$) exhibited a maximum and a minimum in the hydrate isotherms and isobars at 0.50 CO$_2$ mole fractions and higher. Then, Adisasmito et al. (1991) confirmed and extended the measurements done by Unruh and Katz (1949). Their data did not show the unusual hydrate instability reported by Berecz and Balla-Achs (1983). Meanwhile, Ohgaki et al. (1996) reported phase equilibrium data for the (CH$_4$ + CO$_2$) clathrate hydrates at 280 K. Later, Fan and Guo (1999), Seo et al. (2000) and Hachikubo et al. (2002) reported few hydrate dissociation data for (CH$_4$ + CO$_2$) gas mixtures. Among the aforementioned equilibrium data, the experimental data of Unruh and Katz (1949), Berecz and Balla-Achs (1983), Adisasmito et al. (1991), Fan and Guo (1999) and Hachikubo et al. (2002) apparently represent hydrate dissociation conditions. However, Fan and Guo (1999) reported few hydrate dissociation data for a 0.0348 mole fraction of carbon dioxide containing gas. Hachikubo et al. (2002) reported three hydrate dissociation data for 0.25, 0.50 and 0.77 mole fractions of carbon dioxide containing gases.
Moreover, Unruh and Katz (1949) and Adisasmito et al. (1991) reported their hydrate dissociation data generally at temperatures near the ice point though some of their data are at higher temperatures. No discussions were made on possible hydrate structure change(s) or comparison with any thermodynamic model. This literature review indicates a need for generating more dissociation data for the \((\text{CH}_4 + \text{CO}_2)\) clathrate hydrates, studying the stable hydrate structure and also investigating the reliability of the thermodynamic models predictions for the aforementioned clathrate hydrate systems.

In this chapter, the dissociation conditions of the \((\text{CO}_2 + \text{CH}_4)\) clathrate hydrates at low, medium and high concentrations of \text{CO}_2 investigated in the temperature range from \((279\text{ to } 290)\ \text{K}\) and up to \(13\ \text{MPa}\), are presented. An isochoric pressure-search method (Tohidi et al., 2000; Afzal et al., 2007; Mohammadi et al., 2008) was used to estimate the dissociation conditions. The dissociation data generated along with the literature data are compared with the predictions of a thermodynamic model and a previously reported empirical equation (Adisasmito et al., 1991).

### 3.2 Experimental setup and method

Purities and suppliers of the chemicals used in this work are given in Table 3.1. A detailed description of the apparatus used in this study is provided in the literature (Afzal et al., 2007; Mohammadi et al., 2008). A simplified flow diagram of the experimental setup is shown in Figure 3.1 and partial pictures of its main components are shown in Figure 3.2. Briefly, the apparatus is based on the “static–analytic” method (Richon, 1996) with capillary fluid phase sampling (Laugier & Richon, 1986). The heart of this apparatus is an equilibrium cell made of 316 stainless steel and suitable for measurements at pressures up to 40 MPa. The cell has a volume of \((57.5 \pm 0.5)\ \text{cm}^3\) and two sapphire windows. A magnetic stirrer ensures agitation to facilitate reaching equilibrium.

<table>
<thead>
<tr>
<th>Chemical</th>
<th>Supplier</th>
<th>Purity (volume %)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Methane</td>
<td>Messer Griesheim</td>
<td>99.995</td>
</tr>
<tr>
<td>Carbon dioxide</td>
<td>Air Liquide</td>
<td>99.995</td>
</tr>
</tbody>
</table>

\(a\) Deionized water was used in all experiments.
Two platinum resistance thermometers (Pt100) inserted into the vessel were used to measure temperatures and check for equality of temperatures within temperature measurement uncertainty, which is estimated to be less than 0.1 K. This temperature uncertainty estimation results from calibration against a 25-Ω reference platinum resistance thermometer. The pressure in the cell was measured using the low pressure transducer (Druck, type PTX611 for pressures up to 20 MPa). Pressure measurement accuracies are estimated to be better than 2 kPa.

Figure 3.1. Flow diagram of the experimental setup. DAS: degassed aqueous solution; DAU: data acquisition unit; DT: displacement transducer; EC: equilibrium cell; FV: feeding valve; GC: gas chromatograph; HPT: high pressure transducer; LB: liquid bath; LPT: low pressure transducer; PF: pressurizing fluid; PP: platinum probes; RS: ROLSI™ sampler; SD: stirring device; SW: sapphire windows, TR: temperature regulator; VP: vacuum pump; Vs: isolation valve of LPT; VVC: variable volume cell.
Table 3.2. Operating conditions of the gas chromatograph.

<table>
<thead>
<tr>
<th></th>
<th>Carrier gas</th>
<th>Helium</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gas flow rate (ml/min)</td>
<td>25</td>
<td></td>
</tr>
<tr>
<td>Detector</td>
<td>TCD</td>
<td></td>
</tr>
<tr>
<td>Detector temperature (K)</td>
<td>393</td>
<td></td>
</tr>
<tr>
<td>TCD wire temperature (K)</td>
<td>448</td>
<td></td>
</tr>
<tr>
<td>Oven temperature (K)</td>
<td>323</td>
<td></td>
</tr>
</tbody>
</table>
3.2.1 General hydrate formation and dissociation procedure

The isochoric pressure-search method (Tohidi et al., 2000; Afzal et al., 2007; Mohammadi et al., 2008) was followed to determine the hydrate dissociation pressures and temperatures. The reliability of the experimental method used has been demonstrated in the literature (Afzal et al., 2007; Mohammadi et al., 2008; Mohammadi et al., 2009). Before starting the experiment, the cell was evacuated to eliminate the presence of air. The gas mixture was prepared in the cell by introducing first a certain amount of CO$_2$, and then CH$_4$ from the corresponding cylinders through a pressure-regulating valve. After temperature and pressure were stabilized, the valve in the line connecting the vessel and the gas cylinder was closed. The composition of the gas mixture was analyzed and confirmed using a gas chromatograph (Varian, CP3800) coupled with a pneumatic ROLSi™ sampler (Guilbot et al., 2000). The gas chromatograph (GC) equipped with a thermal conductivity detector (TCD) was appropriately programmed with proper flow rates, oven and detector temperatures for the compounds studied, which are given in Table 3.2. A packed analytical column in stainless steel tubing (Agilent J&W, Porapak Q) with 1.83 m length, 2 mm inner diameter and 0.177 mm mesh opening size was used for all the systems measured.

Subsequently, about 10% (by volume) of the cell was filled with water using the volumetric press shown in Figure 3.2. The cell was immersed into the temperature-controlled bath and the temperature was slowly decreased to form the hydrate. Hydrate formation in the cell was detected by a noticeable pressure drop. The temperature was then increased in steps of 0.1 K. At every temperature step, the temperature was kept constant with sufficient time to achieve an equilibrium state in the cell. As implemented by Ohmura and coworkers (2004), a pressure-temperature diagram was obtained for each experimental run from which the hydrate dissociation point was found (Figure 3.3). The point at which the slope ($\partial p/\partial T$) of pressure-temperature data plots changes sharply is considered to be the point at which all hydrate crystals have dissociated and, hence, is reported as the equilibrium condition (Ohmura et al., 2004). As mentioned earlier, the procedure is repeated at different pressures in order to determine the hydrate phase boundaries over the studied temperature range.
Figure 3.3. Representative isochoric curve and pressure and temperature plots obtained during a hydrate formation/dissociation experiment, showing characteristic times for reaching equilibrium and overall behavior for CO\textsubscript{2} + CH\textsubscript{4} systems: pressure vs. temperature (top), pressure (bottom left) and temperature (bottom right) as a function of time. CO\textsubscript{2} molar composition in gas feed was 0.272.

3.3 Results and discussion

The dissociation data for methane and carbon dioxide simple hydrates were first measured. These data along with some selected literature data are illustrated in Figures 3.4 and 3.5. The good agreement demonstrates the reliability of the isochoric pressure-search method (Tohidi \textit{et al.}, 2000; Afzal \textit{et al.}, 2007; Mohammadi \textit{et al.}, 2008) used in this work. Figures 3.4 and 3.5 also show the predictions of a thermodynamic model (HWHYD, 2000). A detailed description of this model is given elsewhere (Tohidi \textit{et al.}, 1993). Briefly, it is based on the equality of fugacity concept, which uses the Valderrama modification of the Patel-Teja equation of state (Valderrama, 1990) and non-density dependent mixing rules (Avlonitis \textit{et al.}, 1994) for modeling the fluid phases while the van der Waals and Platteeuw (1959) theory is used for modeling the hydrate phase.
Figure 3.4. Experimental (literature and this work) dissociation pressures for methane simple hydrates, together with thermodynamic model (HWHYD, 2000) predictions assuming sI and calculated values using eq. (3.2).

Figure 3.5. Experimental (literature and this work) dissociation pressures for carbon dioxide simple hydrates, together with thermodynamic model (HWHYD, 2000) predictions assuming sI and calculated values using eq. (3.2).
The hydrate dissociation conditions for the (methane + carbon dioxide + water) systems were investigated at different concentrations of carbon dioxide to study the effect of carbon dioxide composition in the mixture. The composition of the (methane + carbon dioxide) gas mixtures along with the experimental hydrate dissociation conditions in the presence of pure water are given in Table A.1 (Appendix A) and are shown in Figure 3.6. Initial gas compositions are expressed in mole fractions in the gas phase. Because the equilibrium pressure of CO$_2$ hydrates is lower than that of CH$_4$ hydrates (Figures 3.4 and 3.5), it is noted, as expected, that mixed (CO$_2$ + CH$_4$) hydrates are thermodynamically more stable as the concentration of CO$_2$ in the feed gas decreases. For example, at 289.2 K the dissociation pressures for gas mixtures of 0.730, 0.490 and 0.264 molar concentration of CO$_2$ are 13.06, 12.41 and 11.62 MPa, respectively.

![Figure 3.6](image-url)

Figure 3.6. Experimental dissociation pressures from this work for various (methane + carbon dioxide) gas hydrates at different CO$_2$ load mole fractions: 0.264 (●); 0.272 (■); 0.490 (▲); 0.500 (*); 0.504 (—); 0.730 (●).
Chapter 3 - Ph.D. Dissertation V. BELANDRIA

The predictions of the thermodynamic model (HWHYD, 2000) are also reported in Table A.1. The experimental and predicted dissociation conditions are shown in Figures 3.7 and 3.8. As can be observed in these figures and also in Table A.1, the thermodynamic model (HWHYD, 2000) generally overestimates the dissociation pressures for the (carbon dioxide + methane) clathrate hydrates studied in this work. Both structures I and II have been assumed for predicting the dissociation conditions. Assuming structure I, however, leads to lower deviations between the predicted and experimental data suggesting the stable structure for the (carbon dioxide + methane) clathrate hydrates studied in this work is likely structure I.

The relative deviation ($RD$) given in Table A.1 was calculated using the following equation:

$$RD(\%) = \frac{p_{\text{exp}} - p_{\text{pred}}}{p_{\text{exp}}} \times 100$$  (3.1)

where $p_{\text{exp}}$ and $p_{\text{pred}}$ represent experimental and predicted dissociation pressures, respectively.

Table A.1 and Figure 3.7 also include the predictions using the correlation proposed by Adisasmito and coworkers (1991):

$$\ln \left( \frac{p_{\text{calc}}}{\text{MPa}} \right) = A + B(T/\text{K})^{-1} + C y + D(T/\text{K})^{2} + E y(T/\text{K})^{-1} + F y^{2}$$  (3.2)

where $p_{\text{calc}}$ = calculated pressure, $T$ = temperature, $y$ = mole per cent of carbon dioxide in the vapor phase (water-free basis), and the values for the constants are: $A=175.3$, $B=-89009$, $C=0.07392$, $D=1.1307 \times 10^{7}$, $E=-23.392$, and $F=3.9566 \times 10^{-5}$.

An acceptable agreement is generally observed between the predicted values using eq. (3.2) and the experimental data generated in this work.
Figure 3.7. Relative deviation ($RD$) of experimental dissociation pressures ($p_{exp}$) for ($CO_2 + CH_4$) clathrate hydrates and predictions of the thermodynamic model (HWHYD, 2000). $RD$ assuming sI: 0.264 (◊); 0.272 (□); 0.490 (△); 0.500 (*) 0.504 (x); 0.730 (◦). $RD$ assuming sII: 0.264 (●); 0.272 (■); 0.490 (▲); 0.500 (* shadow); 0.504 (x shadow); 0.730 (●).
Figure 3.8. Experimental, calculated using (eq. 3.2) and predicted dissociation pressures for (CO$_2$ + CH$_4$) clathrate hydrates. This work at different CO$_2$ mole fractions loaded: 0.264 (♦); 0.272 (■); 0.490 (▲); 0.500 (*); 0.504 (●); 0.730 (●). Calculated pressures using eq. (3.2) proposed by Adisasmito and coworkers (1991): (+). Thermodynamic model (HWHYD, 2000) predictions assuming sI at different CO$_2$ mole fractions loaded: 0.264 (◊); 0.272 (□); 0.490 (△); 0.500 (+); 0.504 (×); 0.730 (○). Thermodynamic model (HWHYD, 2000) predictions assuming sII at different CO$_2$ mole fractions loaded: 0.264 (◊ shadow); 0.272 (□ shadow); 0.490 (△ shadow); 0.500 (* shadow); 0.504 (× shadow); 0.730 (○ shadow).
Figure 3.9. Relative deviation ($RD$) of the experimental and predicted (HWHYD model, 2000) dissociation pressures ($p_{exp}$) for various ($CO_2 + CH_4$) clathrate hydrates at different $CO_2$ mole fractions loaded. $RD$ (%) assuming sI: This work (◊); Hachikubo et al., 2002 (□); Adisasmito et al., 1991 (○); Unruh and Katz, 1949 (△); Fan and Guo, 1999 (x). $RD$ (%) assuming sII: This work (♦); Hachikubo et al., 2002 (■); Adisasmito et al., 1991 (●); Unruh and Katz, 1949 (▲); Fan and Guo, 1999 (x shadow).
Figure 3.10. Relative deviation (RD) of experimental dissociation pressures ($p_{exp}$) for (CO$_2$ + CH$_4$) clathrate hydrates and calculated pressures using eq. (3.2) proposed by Adisasmito and coworkers (1991): This work (◊); Hachikubo et al., 2002 (□); Adisasmito et al., 1991 (○); Unruh and Katz, 1949 (△); Fan and Guo, 1999 (x).

Figures 3.9 and 3.11 compare the experimental dissociation data reported in the literature for various (methane + carbon dioxide) clathrate hydrates with the predictions of the thermodynamic model (HWHYD, 2000). These figures also show that the model (HWHYD, 2000) over predicts the dissociation conditions of the experimental dissociation data reported in the literature for (methane + carbon dioxide) clathrate hydrates. Again, both structures I and II for the predictions of the dissociation conditions were assumed and lower deviations between the predicted and experimental data by assuming structure I are observed suggesting the stable hydrate structure for the (carbon dioxide + methane) clathrate hydrates reported in the literature is likely structure I. However, the final proof for the stable structure of the (methane + carbon dioxide) clathrate
hydrates requires direct measurements by suitable physical techniques (e.g., NMR, X-ray, or Raman spectroscopy).

Figure 3.11. Experimental dissociation conditions for various (CO$_2$ + CH$_4$) clathrate hydrates and predictions of the thermodynamic model (HWHYD, 2000), at different CO$_2$ mole fractions loaded: This work (○). Literature: Hachikubo et al., 2002 (■); Adisasmito et al., 1991 (○); Unruh and Katz, 1949 (x); Fan and Guo, 1999 (△). Thermodynamic model (HWHYD, 2000) predictions assuming sI: This work (�行). Literature: Hachikubo et al., 2002 (■); Adisasmito et al., 1991 (○); Unruh and Katz, 1949 (●); Fan and Guo, 1999 (△). Thermodynamic model (HWHYD, 2000) predictions assuming sII: This work (○ shadow). Literature: Hachikubo et al., 2002 (square shadow); Adisasmito et al., 1991 (○ shadow); Unruh and Katz, 1949 (x shadow); Fan and Guo, 1999 (△ shadow).
Figure 3.12. Comparison of experimental dissociation pressures for various (CO$_2$ + CH$_4$) clathrate hydrates with the calculated values using eq. (3.2). Experimental dissociation pressures at different CO$_2$ mole fractions loaded: This work (○); Hachikubo et al., 2002 (□); Adisasmito et al., 1991 (❖); Unruh and Katz, 1949 (χ); Fan and Guo, 1999 (△). Calculated dissociation pressures with eq. (3.2): This work (●); Hachikubo et al., 2002 (●); Adisasmito et al., 1991 (●); Unruh and Katz, 1949 (x shadow); Fan and Guo, 1999 (▲).

The experimental dissociation data reported in the literature have also been compared with the calculated pressures using the equation proposed by Adisasmito and coworkers (1991) in Figures 3.10 and 3.12. As can be seen, the agreement between the calculated values and experimental data using eq. (3.2) is acceptable. In overall, as shown earlier, the model (HWHYD, 2000) unreliably predicts the dissociation conditions for (methane + carbon dioxide) clathrate hydrates in the presence of pure water. Similar results are expected from other thermodynamic models. This suggests that reconsideration of thermodynamic models for predicting dissociation
conditions of (methane + carbon dioxide) clathrate hydrates is necessary. These models have generally been developed for hydrocarbon systems. For the systems containing carbon dioxide, model parameters likely require readjustments using reliable experimental data.

In addition, a number of technical difficulties (e.g. plugging of capillary sampler, long metastable periods, unsuitability for investigating corrosive gases, etc.) were encountered for measuring compositional equilibrium data. Because such measurements have been considered within the scope of this research, it was decided to develop a new apparatus suitable for generating accurate hydrate phase equilibria and compositional data simultaneously, which is the subject of the next chapter.
Development of a New Apparatus for Simultaneous Measurements of Gas Hydrate Dissociation Conditions and Compositional Analysis†

Ce chapitre est consacré à la description d'un nouvel outil expérimental basé sur la technique «statique-analytique» avec échantillonnage en phase gazeuse au moyen d'un capillaire, spécialement conçu, construit et amélioré pour mesurer avec précision les équilibres de phases : pression, température et compositions en présence d'hydrates de gaz. Cet appareil est adapté à des mesures entre 233 et 373 K, pour des pressions pouvant atteindre 60 MPa et il est compatible avec l'utilisation de gaz corrosifs. La procédure expérimentale développée pour mesurer les conditions de dissociation des hydrates est similaire à celle décrite dans le chapitre 3. En outre, les compositions de la phase gazeuse en équilibre avec l'hydrate de gaz et de la phase aqueuse sont mesurées par chromatographie en phase gazeuse. Une approche basée sur une étude des bilans de matière est utilisée pour estimer les compositions des phases hydrates et aqueuse. Afin de définir les capacités réelles et la fiabilité de l'appareillage et de la méthode utilisée, de nouveaux équilibres de phases du système (dioxyde de carbone + eau + méthane) ont été mesurés dans des conditions de formation d'hydrates et les résultats comparés aux données de la littérature. Ce chapitre se termine par une discussion basée sur la comparaison entre les prédicitions des modèles thermodynamiques et les données obtenues dans ce travail.

Résumé

Abstract

This chapter is devoted to the description of a new experimental set-up based on the “static-analytic” technique with gas phase capillary sampling, specially designed, built, and improved to accurately measure phase equilibrium pressure, temperature, and compositions under gas hydrate formation conditions. The apparatus is suitable for measurements at temperatures ranging from (233 to 373) K, pressures up to 60 MPa and it is compatible with corrosive gases. The experimental procedure used to measure the hydrate dissociation conditions is similar to the one described in Chapter 3. In addition, the compositions of the gas phase in equilibrium with gas hydrate and aqueous phase are measured through gas chromatography technique. A material balance based approach is used for estimating the compositions of the hydrate and aqueous phases. In order to determine the capabilities and reliability of the apparatus and method used, new phase equilibrium data in the (carbon dioxide + methane + water) system under hydrate formation conditions were measured and compared with literature data. A discussion based on the comparison between the predictions of thermodynamic models and the data measured in this work is also given.
4 Development of a New Apparatus for Simultaneous Measurements of Gas Hydrate Dissociation Conditions and Compositional Analysis

4.1 Introduction

Considerable research has been devoted in the last decades to examine potential industrial applications of gas hydrate technology (Adisasmito et al., 1991; Ohgaki et al., 1996; Hachikubo et al., 2002; Sloan & Koh, 2008). Thermodynamic models based on accurate experimental equilibrium data are needed to reliably predict hydrate thermodynamic properties for potential industrial applications. As most of the existing models have been developed for hydrocarbon systems, model parameters must be re-considered for hydrates containing carbon dioxide using reliable phase equilibrium data (Adisasmito et al., 1991; Ohgaki et al., 1996; Hachikubo et al., 2002; Sloan & Koh, 2008, Belandria et al., 2010). In addition, any error in the measurement of hydrate phase equilibrium properties will lead to significant errors in model’s predictions. Consequently, accurate measurement of the phase behavior of mixed clathrate hydrates containing CO₂ is necessary.

A number of experimental devices and methods for measuring hydrate phase equilibrium of gas mixtures reported in the literature have been reviewed by Sloan and Koh (2008). Experimental determination of the composition of the existing phases in equilibrium with gas hydrate by “static-analytic” method is generally not easy. Some of the most common technical difficulties are: long metastable periods, ineffective agitation, difficulties to sample the phases without disturbing the thermodynamic equilibrium, lack of visibility inside the equilibrium cell, plugging of sampling valves, etc.

All of the above are to be considered in the design of an experimental apparatus for hydrate phase equilibrium measurements. Traditionally the experimental methods involve measuring hydrate phase boundaries, compositional data are scarcely measured (Sloan & Koh, 2008).
Table 4.1. Experimental data reported in the literature for the dissociation conditions of the binary gas hydrates of (carbon dioxide + methane).

<table>
<thead>
<tr>
<th>Authors</th>
<th>Dissociation conditions ranges (T and p)</th>
<th>Range of CO₂ mole fraction in gaseous mixture</th>
<th>Number of experimental data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Adisasmito et al. (1991)</td>
<td>273.7 - 287.6 K 2.52 - 10.95 MPa 271.0 K 1.27 - 2.02 MPa</td>
<td>0.08 - 0.85 0.25 - 0.77</td>
<td>41 3</td>
</tr>
<tr>
<td>Hachikubo et al. (2002)</td>
<td>279.1 - 289.9 K 2.96 - 13.06 MPa</td>
<td>0.264 - 0.730</td>
<td>11</td>
</tr>
<tr>
<td>Belandria et al. (2010)</td>
<td>275.5 - 285.7 K 1.99 - 7.0 MPa</td>
<td>0.055 - 0.71</td>
<td>17</td>
</tr>
<tr>
<td>Unruh and Katz (1949)</td>
<td>273.5 - 282.3 K 1.10 - 4.80 MPa</td>
<td>0.9652</td>
<td>9</td>
</tr>
<tr>
<td>Fan and Guo (1999)</td>
<td>272.66 - 283.56 K 1.5 - 5.0 MPa</td>
<td>0 - 1.0</td>
<td>17</td>
</tr>
<tr>
<td>Seo et al. (2000)</td>
<td>277.9 - 285.5 K 2.72 - 8.27 MPa</td>
<td>0.206 - 0.744</td>
<td>9</td>
</tr>
<tr>
<td>This work</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 4.2. Experimental data reported in the literature for the p, T, and composition of the gas and hydrate phases at (L_w-H-G) equilibrium conditions for the binary clathrate hydrates of (carbon dioxide + methane).

<table>
<thead>
<tr>
<th>Authors</th>
<th>T and p ranges</th>
<th>Mole fraction of CO₂ in the gas (y), hydrate (z) and/or aqueous phases</th>
<th>Number of experimental data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ohgaki et al. (1996)</td>
<td>280.3 K 3.04 - 5.46 MPa</td>
<td>y, z</td>
<td>31</td>
</tr>
<tr>
<td>Seo et al. (2000)</td>
<td>274.36 - 283.56 K 1.5 - 5.0 MPa</td>
<td>y, z</td>
<td>26</td>
</tr>
<tr>
<td>Uchida et al. (2005)</td>
<td>258-274.1 K and 190 K 0.5-3 MPa and 0.1 MPa</td>
<td>y, z</td>
<td>-</td>
</tr>
<tr>
<td>Beltran and Servio (2008)</td>
<td>275.14 - 285.34 K 2.36 - 7.47 MPa</td>
<td>y</td>
<td>22</td>
</tr>
<tr>
<td>Bruusgaard et al. (2010)</td>
<td>274.02 - 280.05 K 1.66 - 4.03 MPa</td>
<td>y</td>
<td>12</td>
</tr>
<tr>
<td>This work</td>
<td>273.6 - 284.2 K 1.510 - 7.190 MPa</td>
<td>y, x, z</td>
<td>41</td>
</tr>
</tbody>
</table>
Although a significant amount of research has been carried out for mixed hydrates of carbon dioxide and methane (Unruh & Katz, 1949; Ohgaki et al., 1996; Fan & Guo, 1999; Seo et al., 2000; Hachikubo et al., 2002; Beltran & Servio, 2008; Belandria et al., 2010; Bruusgaard et al., 2010), the compositions of the gas, hydrate, and liquid phases reported in the literature are still limited. A summary of the experimental conditions at which literature data (including this work) have been reported is given in Tables 4.1 and 4.2.

In the previous chapter a small (~57.5 cm$^3$) equilibrium cell was used for measuring the hydrate dissociation conditions of (CO$_2$ + CH$_4$) gas mixtures in the presence of pure water. Based on the limitations of the latter apparatus and the current needs for gas hydrate investigations, an alternative and possibly more efficient way to simultaneously measure the boundary of gas hydrate formation and the compositions of the existing phases in equilibrium with mixed hydrates is presented in this chapter. The main features of both apparatuses are quickly reviewed in Table 4.3.

Table 4.3. Main characteristics of previous and new experimental setups.

<table>
<thead>
<tr>
<th>Feature</th>
<th>Previous</th>
<th>New</th>
</tr>
</thead>
<tbody>
<tr>
<td>Volume of the cell</td>
<td>~ 60 cm$^3$</td>
<td>~ 200 cm$^3$</td>
</tr>
<tr>
<td>Agitation system</td>
<td>Magnetic rod</td>
<td>Magnetically driven Rushton turbine</td>
</tr>
<tr>
<td>Liquid bath / visibility</td>
<td>Huber (CC40) T range ~ (233 to 473) K</td>
<td>Tamson Instruments (TV4000LT) T range ~ (233 to 373) K</td>
</tr>
<tr>
<td></td>
<td>No visual observation during the course of an experiment</td>
<td>Sight windows</td>
</tr>
<tr>
<td>Equilibrium cell</td>
<td>316 stainless steel p ~ 40 MPa</td>
<td>Alloy A286 (High temperature stainless steel, XN26TW) p ~ 60 MPa</td>
</tr>
<tr>
<td>Gas mixture preparation</td>
<td>In the equilibrium cell</td>
<td></td>
</tr>
<tr>
<td>ROLSI$^\text{TM}$ sampler</td>
<td>Pneumatic (movable)</td>
<td>Electromagnetic</td>
</tr>
<tr>
<td>Temperature measurement</td>
<td>Indirectly (in the body of the cell)</td>
<td>$In situ$ (in the cell interior)</td>
</tr>
</tbody>
</table>
Chapter 4 - Ph.D. Dissertation V. BELANDRIA

The new approach is based on the “static-analytical” method (Richon, 1996) and capillary sampling technique (Laugier & Richon, 1986). For this purpose, an experimental set-up suitable for measurements in the temperature range of (233 to 373) K and compatible with corrosive fluids was designed, constructed and validated. The core of the apparatus is an equilibrium cell entirely designed, built, and improved “in house’, which can withstand pressures up to 60 MPa. A major advantage of this apparatus is the combination of precise and accurate measuring devices and the visual observation of the presence of gas hydrates and phase behavior. The isochoric technique (Tohidi et al., 2000; Afzal et al., 2007; Mohammadi et al., 2008) earlier described is used to determine the hydrate temperature and pressure dissociation conditions. For composition measurement of the gas phase under hydrate formation conditions, an electromagnetic ROLSI™ sampler (Guilbot et al., 2000) was installed and connected online to a gas chromatograph.

The compositions of the liquid and hydrate phases are calculated using the material balance approach proposed by Ohgaki et al. (1996) in combination with the experimental data and the volumetric properties evaluated from equations of state for gas mixtures. A suitable mathematical approach is used to solve the non-linear material balance equations. This chapter describes the characteristics of the aforementioned unique measurement system and demonstrates its effectiveness and capabilities.

4.2 Apparatus

With the aim of developing a flexible apparatus suitable for gas hydrate phase equilibrium measurements, a combination of new and adopted features from the literature were considered. The main characteristics of this set-up are: suitability for corrosive fluids (high pressures), strong agitation, precise and accurate measuring devices, gas phase compositional analysis and visual observation inside the equilibrium cell during the course of the experiment. A schematic diagram of this apparatus is shown in Figure 4.1. The experimental setup consists of four major sections: an equilibrium cell, a sample supplying system, a composition analyzing system, and a pressure-temperature measurement system. Partial pictures of the main components are shown in Figure 4.2.
Figure 4.1. Schematic flow diagram of the new apparatus. DAS: degassed aqueous solution; DAU: data acquisition unit; EC: equilibrium cell; G: Gas cylinder; GC: gas chromatograph; HPT: high pressure transducer; LB: liquid bath; LPT: low pressure transducer; PP: platinum probe; RS: ROLSI™ sampler; RT: Rushton turbine; SD: stirring device; SW: sapphire windows, TR: temperature regulator; V₁, V₂, V₄, V₅: feeding valves; V₃, V₆: purge valves; VP: vacuum pump; Vs: isolation valve for LPT; WP: high pressure pump.

Figure 4.2. Partial pictures of the main components of the new apparatus (From left to right: Equilibrium cell, ROLSI™ sampler, pressure transducers, valve arrangement and agitation device, windowed bath).
4.2.1 Equilibrium cell

The core of the apparatus, the equilibrium cell, was entirely designed, built and improved by the workshop of CEP-TEP (MINES ParisTech, France). It was made of a high temperature stainless steel material (Type X6NiCrTiMoVB25-15-2 / Alloy 286) to withstand hydrogen embrittlement and pressures up to 60 MPa. The internal volume of the cell of \((201.0 \pm 0.5 \text{ cm}^3\), including transfer lines\) is known from careful calibration using a variable volume cell coupled to a displacement transducer. The cell is suitable for measurements within temperatures ranging from (233 to 373) K.

The cell is cylindrical in shape and it consists of two major parts: (1) a main body and (2) two sapphire windows. The 166 mm long, 83 mm diameter main body is horizontally placed on an aluminum support (Figure 4.3). Two sapphire windows are located in the front and the back of the cell enabling the visual observation of the presence of gas hydrates and phase behavior occurring inside the equilibrium cell. All pieces of the cell are tightened by sixteen bolts and the seal between the main body and the sapphire windows is achieved with polytetrafluoroethylene (PTFE) O-rings which sit in circular channels on both sides. Three inlet/outlet ports suitable for pressure and temperature sensors have been drilled in the main body of the cell (Figure 4.3).

Figure 4.3. Cross section of the equilibrium cell with stirring and measurement arrangement (left). Photograph of equilibrium cell on its aluminum support (right).
Figure 4.4. (a) Lateral section of the equilibrium cell showing the position of the protection grid. B: tightening bolts; MB: main body; PG: protection grid; RT: Rushton turbine; SW: sapphire windows; \( V_1 \) and \( V_2 \): feeding valves. (b) Detail of the protection grid for the capillary sampler. SD: stirring device.
A stainless steel (316) grid support horizontally placed inside the cell was installed to protect the capillary sampler from plugging by hydrate particles. The protecting framework was fixed by a PTFE support at approximately 20 mm from the top. Such arrangement as shown in Figures 4.4 and 4.5, allows sampling and analyzing the gas phase in equilibrium with the hydrate and liquid phases, in a way that hydrate particles do not enter or plug the capillary. Plugging of capillary sampler by hydrate crystals can seriously compromise the reliability of vapor phase composition measurements during hydrate formation (Ruffine et al., 2010). The arrangement just described can be used to overcome this experimental difficulty. As shown in Fig. 4.6, a remarkable sampling repeatability is obtained for nitrogen gas samples taken under gas-hydrate-liquid equilibrium, demonstrating the value of the latter capillary protection arrangement.

A motor-driven turbine agitation system (Top Industrie, France) enables to stir the cell contents at a speed up to 2000 rpm to increase the fluids contact and enhance water conversion into hydrate.
4.2.2 Sample supplying system

The sample supplying system consists of gas cylinders, a vacuum pump with an electronic manostat (Leybold, model Trivac D) and a high-pressure syringe pump (Teledyne Isco, model 260D), which allows measuring the amount of liquid supplied to the system.

4.2.3 Composition analyzing system

The composition analyzing system consists of an electromagnetic online micro sampler (rapid on-line sampler-injector: ROLSI™) developed at the Ecole des Mines de Paris (Laugier & Richon, 1986; Guilbot et al., 2000). The small size of the samples (1-5 µL) compared to the volume of the cell (~ 201 cm³), ensures thermodynamic equilibrium is not disturbed during sampling.
Over the years, many modifications have been carried out to the original ROLSI™. The electromagnetic version used in this apparatus (ROLSI™ evolution IV) shown in Figure 4.2, is smaller than the one described by Guilbot et al. (2000) and entirely automatable, it is actuated by an electromagnet allowing significant new features, more robustness and increased operational life (Afzal et al. 2008a). Figure 4.7 gives a flow diagram of the latest version of this sampler-injector. The micro sampler is a compact device with no dead volumes and it consists of a Monel 400 capillary tube with internal diameter of less than 0.15 mm. Reliable and representative samples may be obtained by adjusting the sample size through the valve’s opening time (between 10 milliseconds and approximately one second) and frequency, with an outstanding repeatability. It allows samplings from (0.3 to 80 MPa) and temperatures from cryogenic up to 523 K.

Samples are swept along the carrier gas (outlet) heated transfer line, ensuring direct injection into the GC column. Sampling can be carried out only through electric power, thus the capillary is normally closed for highest safety. The materials of construction (Monel 400 or Inox 316L) enable to extend its applicability to corrosive and viscous systems (ROLSI™).

Figure 4.7. Flow diagram of the electromagnetic rapid on-line sampler-injector: ROLSI™ (Afzal et al., 2008b).
Chapter 4 - Ph.D. Dissertation V. BELANDRIA

The ROLSI\textsuperscript{TM} was vertically installed in the equilibrium cell and connected to a gas chromatograph (GC) on-line. The micro sampler and the lines connecting to the GC are independently heated to a temperature well above that of the equilibrium cell to avoid any condensation or adsorption of the components. The temperature of the sampling valve and transfer lines are set through the ROLSI\textsuperscript{TM} control unit. To make sampling possible, the pressure inside the cell must be higher than the pressure of the carrier gas stream from the GC. The ROLSI\textsuperscript{TM} is actuated using the control unit, which allows setting the valve’s opening time with a resolution of 0.01 s. Thus, for a given pressure in the cell, the frequency and the amount of sample withdrawn can be adjusted.

The analysis work was carried out using a gas chromatograph (Varian, CP3800) equipped with a thermal conductivity detector (TCD). The GC was connected to a computer fitted with the Perichrom Winilab III software (Figure 4.8). The characteristics of the chromatographic column are described in section 2.6.1 and the chromatographic conditions were similar to those given in Chapter 3. The composition of the gas phase is determined by gas chromatography, as explained in Chapter 2, while the composition of water in the gas phase is considered negligible in the experimental conditions investigated in this study (Mohammadi & Richon, 2009b). However, other methods as “dilutor technique” may be used if necessary to measure the water content of the gas phase (Mohammadi \textit{et al.}, 2004).

Figure 4.8. Layout for chromatograms acquisition using Winilab III software.
4.2.4 Measurement, control and acquisition of temperature and pressure

Temperature is controlled using a thermostatic ethanol bath (Tamson Instruments, TV4000LT). The thermostatic bath is equipped with a glass window, which allows the visual observation of the cell content throughout the experiments. One platinum temperature probe (Pt100) inserted in the cell interior was used to measure the temperature inside the cell within measurement uncertainties, which are estimated to be less than 0.02 K with a second order polynomial calibration equation, as mentioned in Chapter 2. The temperature probe was carefully calibrated against a reference platinum resistance thermometer, as indicated also in Chapter 2.

The equilibrium pressure was measured using two calibrated pressure transducers (Druck™, type PTX611). Pressure ratings for low (LPT) and high (HPT) pressure transducers are 8 and 40 MPa, respectively. Both pressure transducers are maintained at constant temperature (temperature higher than the highest temperature of the study) using an air-thermostat thermally regulated by a proportional–integral–derivative controller (WEST instrument, model 6100).

Figure 4.9. Layout for temperature and pressure data acquisition through AOIP Ltc10 software.
After calibrating the pressure transducers against a dead weight balance (Desgranges & Huot 5202S CP, Aubervilliers, France), pressure accuracy was estimated to be better than 0.002 MPa using a second order polynomial calibration equation, as described in Chapter 2. A major advantage of this apparatus is the combination of precise and accurate measuring devices and the visual observation of the presence of gas hydrates and phase behavior. The apparatus is also equipped with a safety pressure relief valve.

The data acquisition unit (AOIP, PC10) was coupled with a personal computer to measure and automatically register pressure, temperature and time data. The data acquisition software (AOIP, Ltc10) also allows adjusting the rate of data acquisition. Continuous recording of pressures and temperatures allows detecting any subtle changes in the system and true equilibrium conditions. A representative view of the temperature and pressure data acquisition software is shown in Figure 4.9.

### 4.3 Experimental Procedure

Phase equilibrium measurements \((p, T, y)\) under hydrate formation conditions were carried out using the apparatus described in the previous section and the experimental procedure as follows.

#### 4.3.1 Preparation of the feed

Research grade carbon dioxide (99.995 mole% purity) supplied by Air Liquide and \(\text{CH}_4\) (99.995 mole % purity) supplied by Messer Griesheim, were used without further purification. Gas mixtures composed of \(\text{CO}_2\) and \(\text{CH}_4\) were prepared in the equilibrium cell. After the equilibrium cell was well cleaned and evacuated with vacuum pump, a specified amount of each gas (through pressure measurement) was introduced at ambient temperature into the volume-calibrated cell from the corresponding gas cylinders through a pressure-regulating valve. Once temperature and pressure were stabilized, the on-line valve connecting the vessel and the gas cylinder was closed. As pressure, temperature and the total volume of the equilibrium cell are known, the total number of moles loaded to the cell is easily calculated by applying an appropriate \(p-V-T\) relation, such as the ideal gas law. The initial composition of the gas mixture is determined by gas chromatography (GC). Several samples are taken through ROLSI™ sampler and analyzed by
GC. Agreement between the overall compositions obtained by PVT and chromatographic methods assures this approach as a highly reliable one. Molar concentrations of CH₄ and CO₂ are measured within an experimental uncertainty of ± 1-2 %.

4.3.2 Fluids supply to the equilibrium cell

An amount of typically 10 % (by volume) of the equilibrium cell was subsequently filled with distilled and deionized water using a high-pressure syringe pump. All amounts of substances supplied to the cell were quantified.

4.3.3 Isochoric Pressure Search Method

Hydrate dissociation conditions were measured according to the isochoric pressure search method (Tohidi et al., 2000; Afzal et al., 2007; Mohammadi et al., 2008), as described in Chapter 3. Briefly, the cell was immersed into the temperature-controlled bath and the temperature was decreased to form hydrate, while agitating at a constant speed of 1500 rpm. The temperature of the system was kept constant for at least 24 hours to overcome the metastable period and allow complete hydrate formation. Hydrate formation in the cell was detected by a noticeable pressure drop. Once hydrate formation was completed and equilibrium conditions were reached, at least seven samples of the gas phase were taken through the ROLSi™ sampler at a given temperature and pressure for repeatability checks. The composition of the gas phase at equilibrium with the hydrate and liquid phases was determined through GC analysis.

Temperature was then increased in steps at sufficiently slow rate of about 0.1 K/h (Tohidi et al., 2000; Rovetto et al., 2006). At every temperature step, temperature was kept constant and the composition of the gas phase was successively analyzed, until meeting the criteria for equilibrium described in Chapter 2. At this point (typically reached within four hours), it was assumed that equilibrium had been reached and average concentrations were registered as the composition of the gas phase at the corresponding temperature and pressure condition.
Variables measured:
- Total volume ($V$)
- Total quantities of gases and liquid ($n_1$, $n_2$, $n_3$, respectively)
- Mole fractions of gas phase ($y_1$ and $y_2$)
- Equilibrium $T$ and $p$

Figure 4.10. Hydrate formation/dissociation process inside the high-pressure visual cell (left), cooling and heating isochors and determination of hydrate phase boundaries and composition of the equilibrium phases (right).

Temperature and pressure data were collected twice per minute throughout the experiment. As implemented by Ohmura and coworkers (2004), a pressure-temperature diagram was obtained for each experimental run, from which the hydrate dissociation condition (HDC) was determined. The point at which the slope of pressure-temperature data plots changes sharply was considered to be the point at which all hydrate crystals have dissociated and, hence, it is reported as the hydrate dissociation point (Ohmura et al., 2004). Figure 4.10 illustrates the typical course of a gas hydrate formation-dissociation experiment.

There is a fundamental difference between hydrate formation and dissociation conditions, since the gas and aqueous phases are initially disordered on a molecular level, the initial hydrate formation is affected by a metastability period, while hydrate crystals are ordered structures in nature and they are quickly dissociated when taken out of their $p$-$T$ stability region (Sloan & Koh, 2008).
For measuring an equilibrium condition at a higher pressure, the pressure of the system was increased by successively supplying water to the equilibrium cell until achieving the desired pressure. In this way, several $p$, $T$ and gas phase composition equilibrium data were obtained in parallel to the hydrate dissociation conditions from each experimental run. Maximum uncertainties in the pressure and temperature measurements are expected to be within $\pm 0.05$ MPa and $\pm 0.2$ K, respectively. The maximum overall uncertainty is attributed to the uncertainty in measuring compositions of the gas phase by gas chromatography, which is estimated to be less than 1% as explained in Chapter 2.

The experimental quantities measured in every hydrate formation and dissociation experiment are as follows: total volume ($V$), each total quantity of CO$_2$, methane and water ($n_1^t$, $n_2^t$, $n_3^t$, respectively), mole fractions of gas phase ($y_1$ and $y_2$) and the equilibrium temperature ($T$) and pressure ($p$). Starting from the ($p$, $T$, $y$) data for the three-phase equilibrium, the compositions of the hydrate and aqueous phases are calculated using a material balance approach proposed by Ohgaki and coworkers (1996) in combination with the Peng-Robinson (1976) equation of state for gas mixtures. Assuming the perfect gas law is valid throughout the studied pressure range and considering that all types of molecules have the same gaseous molar volume, $v_i^G$ may be replaced by $v_m^G$ and the volume-balance in the equilibrium cell is given as:

$$V = \sum n_i^G v_m^G + \sum n_i^L v_i^L + n^H v^H$$  \hfill (4.1)

where the subscript $m$ denotes the gas mixture and the superscripts $H$, $L$, and $G$ represent the hydrate, liquid, and gas phases, respectively. The volumetric properties for the gas mixture ($v_m^G$), liquid ($v_i^L$) and the molar volume of ideal hydrate ($v^H$) were calculated using the CSMGem thermodynamic model (CSMGem, 2008).

In addition, equations (4.2) to (4.4) are derived according to the material balances for the three present components in the system as follows:

$$n_i^t = n_i^G + n_i^L + zn^n$$  \hfill (4.2)

$$n_i^t = n_i^G + n_i^L + (1 - z)n^n$$  \hfill (4.3)

$$n_i^t = n_i^G + qn^n$$  \hfill (4.4)
where the total amount of each component once measured, can be partitioned into gas, liquid (aqueous phase), and hydrate (z) phases for CO$_2$ and CH$_4$ ($n_1^G$, $n_2^G$, respectively), and liquid and hydrate phases for water ($n_3^L$).

The expressions for mole fractions of CO$_2$ in the gas phase ($y_1$) and CO$_2$ ($x_1$) and CH$_4$ ($x_2$) in the liquid phase are given by equations (4.5) to (4.7):

$$y_1 = \frac{n_1^G}{\sum n_i^G}$$  

(4.5)

$$x_1 = \frac{n_1^L}{\sum n_i^L}$$  

(4.6)

$$x_2 = \frac{n_2^L}{\sum n_i^L}$$  

(4.7)

The values of $x_1$ and $x_2$ can be estimated from a suitable thermodynamic model. For this purpose, the CSMGem thermodynamic model, which is based on the Gibbs energy minimization (CSMGem, 2008) was used. In the cases where the model did not converge, these values were evaluated applying the apparent Henry’s constants of each pure gas system:

$$x_i = f_i(T, P) / H_i(T, P)$$  

(4.8)

where $f_i(T, P)$ is the fugacity coefficient, $H_i(T, P)$ is the apparent Henry’s constant, and subscript $i$ refers to the $i^{th}$ component in the mixture. A mathematical approach based on the Newton’s numerical method (Constantinides & Moustofì, 1999) coupled with the Differential Evolution optimization strategy (Price & Storn, 1997) was used to solve Equations (4.1) to (4.7) for the seven unknown variables ($n_1^G$, $n_2^G$, $n_1^L$, $n_2^L$, $n_3^L$, $n_H^L$, and $z$). As hydrate composition is variable with temperature, pressure, and the composition of associated fluid phases (Sloan & Koh, 2008), an approximate value of $q$, based on the ($p$, $T$, $y$) conditions under which hydrates are formed and assuming clathrate hydrate structure I, is first anticipated. A more accurate value is then obtained by iteration. The solving procedure is described in detail elsewhere (Belandria et al., 2011).
4.4 Results and discussion

Hydrate dissociation conditions ($T$ and $p$) for the (CO$_2$ + CH$_4$ + H$_2$O) systems were measured at different compositions of CO$_2$ in the gas feed. The compositions of the (methane + carbon dioxide) gas mixtures along with the experimental hydrate dissociation conditions in the presence of pure water are presented in Table A.2 (Appendix A) and Figure 4.11. In addition, the hydrate dissociation pressures were predicted at the corresponding equilibrium temperature, CO$_2$ mole fraction in the gas feed, and water mole fraction introduced to the system using two hydrate thermodynamic models: CSMGem and HWHYD, which is based on fugacity equalities of each component throughout all present phases (HWHYD, 2000).

![Figure 4.11](image_url)

Figure 4.11. Hydrate dissociation conditions measured in this work for (methane + carbon dioxide) clathrate hydrates at various CO$_2$ load mole fractions: 0.206 (♦); 0.476 (▲) and 0.744 (●).
Figure 4.12. Hydrate dissociation conditions (literature and this work) for (methane + carbon dioxide) clathrate hydrates at selected CO2 load mole fractions. (a): ♦, 0.206 (This work); ◊, 0.210-0.250 (Adisasmito et al., 1991); □, 0.264 (Belandria et al., 2010); x, 0.274 (Unruh & Katz, 1949); △, 0.200 (Seo et al., 2000); (b): ♦, 0.476 (This work); ◊, 0.390-0.500 (Adisasmito et al., 1991); □, 0.490-0.504 (Belandria et al., 2010); x, 0.539-0.545 (Unruh & Katz, 1949); Δ, 0.600 (Seo et al., 2000); (c): ♦, 0.744 (This work); ◊, 0.670-0.850 (Adisasmito et al., 1991); □, 0.730 (Belandria et al., 2010); x, 0.777 (Unruh & Katz, 1949). Dashed line, pure CO2 hydrates and solid line, pure CH4 hydrates (Adisasmito et al., 1991).
The predicted hydrate dissociation pressures are also listed in Table A.2 along with the absolute relative deviation (ARD) from the obtained experimental values. As can be seen, the ARD of the predicted hydrate dissociation conditions by HWHYD and CSMGem models are in average 9.7% and 5.1%, respectively, which are considered to be in acceptable agreement with the data measured in this work.

For comparison purposes, Figures 4.12a, 4.12b, and 4.12c show the hydrate dissociation conditions measured in this work along with some selected experimental data from the literature (Unruh & Katz, 1949; Adisasmito et al., 1991; Seo et al., 2000; Hachikubo et al., 2002; Belandria et al., 2010). The obtained results generally indicate that the hydrate dissociation pressures of the CO₂ containing gas mixtures are greater than those of pure CO₂ hydrates. It is also observed that as the relative amount of CH₄ to CO₂ increases in the feed gas at a given temperature, the equilibrium pressure conditions shift to higher pressures. As can be seen, the agreement between these data and the experimental data reported in the literature is generally acceptable, demonstrating the reliability of the new apparatus and method used in this work.

To the best knowledge of the author, no hydrate structural transition has been reported in the literature for (CO₂ + CH₄) hydrates. Therefore, considering that the (CO₂ + CH₄ + H₂O) system likely forms structure I hydrates (Takeya et al., 2005; Uchida et al., 2005; Sloan & Koh, 2008; Belandria et al., 2010) similar to pure CH₄ or CO₂ hydrates, and applying Gibbs phase rule, there are two degrees of freedom at liquid water-hydrate-gas (Lw-H-G) equilibrium conditions for this system (Bruusgaard et al., 2010). Therefore, two intensive variables can be changed independently without disturbing the thermodynamic equilibrium.

In this work, temperature and pressure were controlled while the compositions of CH₄ and CO₂ in the gas phase under (Lw-H-G) equilibrium were measured and compared with available literature data (Ohgaki et al., 1996; Beltran & Servio, 2008; Bruusgaard et al., 2010). As shown in Figures 4.13a and 4.13b, the molar fractions of CO₂ in the gas and hydrate phases are found to agree with the experimental data reported in the literature within experimental uncertainties. Furthermore, it is observed that the mole fractions of CO₂ in the gas and hydrate phases generally decrease as pressure increases.
Figure 4.13.  

a) $p$-$y$ phase diagram of (methane + carbon dioxide) clathrate hydrates at different equilibrium temperatures: This work: ■, 273.6 K; ●, 275.2 K; ★, 276.1 K; ▲, 278.1 K and +, 280.2 K. Literature: ○, 275.2 K; □, 277.2 K; △, 279.2 K; □, 281.2 K; ×, 283.2 K; —, 285.2 K (Beltran & Servio, 2008); solid line, 274.2 K; ---, 276.2 K; ——, 278.2 K; (Bruusgaard et al., 2010); ⋆, 280.3 K (Ohgaki et al., 1996).

b) $p$-$z$ phase diagram of methane + carbon dioxide clathrate hydrates at 280.2 K: This work: ●, 280.2 K. Literature: ○, 280.3 K (Ohgaki et al., 1996).
This suggests that considerable enrichment of CO₂ in the hydrate phase takes place in the studied systems. It is also observed that the composition of CO₂ in the gas phase increases as temperature increases, which translate in less amount of CO₂ trapped in the hydrate phase at high temperatures. Compositional analysis of the hydrate and liquid phases for the ternary (CO₂ + CH₄ + H₂O) system was determined using the material balance approach described in the experimental section. The non-linear mass balance equations were solved using a suitable mathematical approach, as mentioned earlier. The measured data, results of solving the material balance equations, and the predictions of CSMGem thermodynamic model are summarized in Table A.2 (Appendix A) and illustrated in Figures 4.14a through 4.14e at selected isothermal conditions.

It should be noted that such pressure-gas phase composition (p-y) phase diagrams are essential for designing a (multi-stage operation) CO₂ capture process based on gas hydrates concept. As can be seen in these figures, the predictions of the CSMGem model for the mole fraction of CO₂ in the gas phase are in consistent agreement with the experimental data. However, the thermodynamic model (CSMGem, 2008) shows considerable deviations when predicting the molar compositions of CO₂ in the hydrate phase. This suggests that the parameters of the thermodynamic model may require readjustment using fully compositional analysis + hydrate dissociation experimental data, as such models have generally been developed for hydrates of hydrocarbons using mainly experimental hydrate dissociation data.

As for the unspecified points shown in Table A.2 related to the predictions of the CSMGem model, the model is not able to predict the three-phase equilibrium (Lw-H-G) behavior at the studied conditions. The HWHYD model did not converge at all at the studied experimental conditions.
Figure 4.14. Pressure-composition phase diagram of the (methane + carbon dioxide) clathrate hydrates: This work: $y_{CO_2}$ (▲); $z_{CO_2}$ (●). CSMGem model predictions: $y_{CO_2}$ (Δ); $z_{CO_2}$ (○). a) 273.6 K; b) 275.2 K; c) 276.1 K; d) 278.1 K; e) 280.2 K.
Thermodynamic Stability of Hydrates from Gas Mixtures Containing CO$_2$†

• Flue gas : N$_2$ + CO$_2$
• Fuel Gas : H$_2$ + CO$_2$

N$_2$ or H$_2$
Separation
Hydrate crystals rich in CO$_2$

$p$, $T$
Hydrate Formation

Résumé

Ce chapitre présente des équilibres de phases des systèmes: "dioxyde de carbone + azote + eau" et "dioxyde de carbone + hydrogène + eau" en présence d’hydrates de gaz. Les équilibres à trois phases (Lw-H-G) sont mesurés en suivant les procédures expérimentales décrites dans le chapitre précédent. Des teneurs moyennes à hautes de CO₂ en mélanges de gaz sont étudiées sur une large plage de températures. Des résultats on déduit que les pressions d’équilibre de dissociation sont dépendantes de la composition de la charge et sont décalées vers des valeurs d’autant plus faibles que la fraction molaire en CO₂ de la charge est élevée. Les données de dissociation générées ici, ainsi que les données expérimentales disponibles dans la littérature pour le mélange : "dioxyde de carbone + azote" sont comparées avec les prédictions de deux modèles thermodynamiques. Les écarts observés entre valeurs expérimentales et valeurs prédites sont discutés. Les compositions mesurées sont comparées à celles de la littérature et l’accord est généralement acceptable prenant en compte les incertitudes expérimentales. Les analyses thermodynamiques présentées fournissent la base pour une conception de procédés de séparation impliquant des hydrates en vue de la capture du CO₂ dans le cadre de la pré-combustion ou de la post-combustion.

Abstract

This chapter presents the phase equilibria of (carbon dioxide + nitrogen + water) and (carbon dioxide + hydrogen + water) systems containing gas hydrates. The three-phase (Lw-H-G) equilibrium data are measured following the experimental procedures described in the previous Chapter. Medium to high content CO₂ gas mixtures are investigated over a wide temperature range. The equilibrium dissociation pressures are found to be dependent on the composition of the feed and are shifted to lower values as the mole fraction of CO₂ increases in the feed gas. The dissociation data generated along with the experimental data reported in the literature for (carbon dioxide + nitrogen) are compared with the predictions of two thermodynamic literature models. A discussion is made about the deviations observed between experimental and predicted data. The measured compositional data are compared with the literature data and the agreement is found generally acceptable within experimental uncertainties. The thermodynamic analyses presented provide the basis for a conceptual design of hydrate-based schemes for pre-combustion or post-combustion CO₂ capture.
5 Thermodynamic Stability of Hydrates from Gas Mixtures Containing CO₂

5.1 Introduction

Over 60% of carbon dioxide (CO₂) emission sources come from power plants activity, in which the main constituents are nitrogen (N₂) and CO₂ (IPCC, 2005). Conventional strategies established to capture CO₂ from industrial/flue gases, essentially involve nitrogen-carbon dioxide, hydrogen-carbon dioxide and oxygen-nitrogen separation tasks. Since such separation is the most expensive step of CCS, the challenge is to evaluate and develop energy efficient and environmental friendly technologies to capture the CO₂ produced in large-scale power plants.

Extremely high pressures [100-360 MPa] are required to stabilize structure-II N₂ (Marshall et al. 1964) or H₂ gas hydrates (Mao & Mao, 2004) at ambient temperatures. However, CO₂ is enclathrated in hydrate cages at moderate pressure conditions (Sloan & Koh, 2008). Such preferential formation of CO₂ hydrates over N₂ or H₂ hydrates determine the potential of application of the gas hydrate approach for separating CO₂ from treated flue gas, considered a (CO₂ + N₂) gas mixture, or fuel / synthesis gas, mainly composed of (CO₂ + H₂).

Despite the potential use of gas hydrate approach to capture CO₂ from combustion flue gases, the hydrate phase equilibria of the ternary systems including (carbon dioxide + nitrogen or hydrogen + water) have been scarcely studied. To analyze the complex thermodynamic phenomena involved in hydrate-based crystallization processes, above all, the phase behavior of gas hydrates containing CO₂ as a guest molecule should be investigated. In this respect, several related studies have been performed. The experimental phase equilibrium data on the dissociation conditions and compositions of the gas and hydrate phases reported in the literature for the (carbon dioxide + nitrogen + water) and (carbon dioxide + hydrogen + water) ternary systems are summarized in Tables 5.1 and 5.3, respectively.

Literature studies are mainly focused on the determination of equilibrium conditions. Until now, few experimental works report compositional data of the equilibrium phases (Tables 5.2 and 5.5), although they are fundamental for designing separation processes.
Table 5.1. Literature phase equilibrium data of the \((\text{carbon dioxide} + \text{nitrogen} + \text{water})\) ternary hydrate system.

<table>
<thead>
<tr>
<th>Authors</th>
<th>CO(_2) molar composition in the gas feed</th>
<th>(T) and (p) ranges</th>
<th>Type of data</th>
<th>Number of experimental data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fan and Guo (1999)</td>
<td>0.9099 and 0.9652</td>
<td>273.1 - 280.2 K 1.22 - 3.09 MPa</td>
<td>HDC ((p,T))</td>
<td>9</td>
</tr>
<tr>
<td>Seo et al. (2000)</td>
<td></td>
<td></td>
<td>GHE ((p,T,y,z))</td>
<td>26</td>
</tr>
<tr>
<td>Kang et al. (2001)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Kang et al. (2001)</td>
<td>0.0663 - 0.9659</td>
<td>272.9 - 284.3 K 1.57 - 24.12 MPa</td>
<td>HDC ((p,T))</td>
<td>28</td>
</tr>
<tr>
<td>Seo and Lee (2004)</td>
<td>0.10 and 0.20</td>
<td>272.1 K 3.20 - 14.50 MPa</td>
<td>GHE ((p,T,y,z))</td>
<td>8</td>
</tr>
<tr>
<td>Linga et al. (2007b)</td>
<td>0.169, 0.570, 0.830</td>
<td>273.7 K 1.60 - 7.70 MPa</td>
<td>HDC ((p,T))</td>
<td>3</td>
</tr>
<tr>
<td>Bruusgaard et al. (2008)</td>
<td>0 - 1</td>
<td>275.3 - 283.0 K 1.60 - 22.40 MPa</td>
<td>HDC ((p,T,y))</td>
<td>26</td>
</tr>
<tr>
<td>Herri et al. (2011)</td>
<td>0.16 - 0.59</td>
<td>274.4 - 282.1 K 5.30 - 6.60 MPa</td>
<td>GHLE ((p,T,y,z))</td>
<td>16</td>
</tr>
</tbody>
</table>

Table 5.2. Review of the compositions of the gas and hydrate phases at hydrate equilibrium conditions reported in the literature for \((\text{carbon dioxide} + \text{nitrogen} + \text{water})\) ternary system.

<table>
<thead>
<tr>
<th>Authors</th>
<th>(T) / K and (p) / MPa ranges</th>
<th>Measurement of mole fraction of CO(_2) in the gas ((y)) and hydrate ((z)) phases</th>
<th>Number of experimental data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Seo et al. (2000)</td>
<td>271.75-284.25 1.2-23.5 272-282 1.5-30</td>
<td>(y, z)</td>
<td>26</td>
</tr>
<tr>
<td>Kang et al. (2001)</td>
<td></td>
<td></td>
<td>26</td>
</tr>
<tr>
<td>Seo and Lee (2004)</td>
<td>272.1 3.2 - 14.05</td>
<td>(y, z)</td>
<td>8</td>
</tr>
<tr>
<td>Bruusgaard et al. (2008)</td>
<td>275.3 - 283.0 1.6 - 22.4</td>
<td>(y)</td>
<td>26</td>
</tr>
</tbody>
</table>
Table 5.3. Literature review of the experimental data on compositions of the gas and hydrate phases for the (carbon dioxide + hydrogen + water) systems.

<table>
<thead>
<tr>
<th>Authors</th>
<th>CO₂ molar composition in the gas feed</th>
<th>T and p ranges</th>
<th>Type of data</th>
<th>Number of experimental data</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sugahara et al. (2005)</td>
<td>Not reported</td>
<td>274.3 - 281.9 K 1.42 - 9.13 MPa</td>
<td>GHLE (p,T,y)</td>
<td>43</td>
</tr>
<tr>
<td>Kumar et al. (2006)</td>
<td>0.392, 0.579, 0.833</td>
<td>273.9 - 281.6 K 1.58 - 10.74 MPa</td>
<td>HDC (p,T,y)</td>
<td>20</td>
</tr>
<tr>
<td>Linga et al. (2007a and 2007b)</td>
<td>0.392 and 0.850</td>
<td>273.7 K 1.40 and 5.10 MPa</td>
<td>HDC (p,T)</td>
<td>2</td>
</tr>
<tr>
<td>Li et al. (2010)</td>
<td>0.392</td>
<td>274.1 - 278.8 K 5.75 - 11.01 MPa</td>
<td>HDC (p,T,)</td>
<td>5</td>
</tr>
<tr>
<td>Seo and Kang (2010)</td>
<td>0.41</td>
<td>274.15 K 6.50 - 8.90 MPa</td>
<td>GHLE (p,T,y,z)</td>
<td>3</td>
</tr>
</tbody>
</table>

This literature review indicates that generating accurate experimental thermodynamic data, elucidating the phase behavior under three-phase equilibrium conditions, and also investigating the reliability of the thermodynamic models predictions for the aforementioned clathrate hydrate system are still needed.

In this chapter, basic phase equilibrium data are provided for the (carbon dioxide + nitrogen + water) and (carbon dioxide + hydrogen + water) hydrates and a thermodynamic analysis is presented to establish the stability region of both systems under hydrate formation conditions. The experimental data are compared with the corresponding data available in the literature and also with the predictions of CSMGem and HWHYD thermodynamic models (for carbon dioxide + nitrogen + water systems).

5.2 Gas Hydrate Formation in Carbon Dioxide + Nitrogen + Water Systems

In this section, dissociation and compositional equilibrium properties under hydrate formation conditions for the (carbon dioxide + nitrogen + water) systems are studied at various concentrations of CO₂ in the feed gas in the temperature range of (273.6 to 285.3) K and
pressures up to about 30 MPa. The studied gas mixtures composed of high purity grade CO\textsubscript{2} (99.995 mole\%, supplied by Air Liquide) and N\textsubscript{2} (over 99.99 mole\%, supplied by Air Liquide) were prepared in the equilibrium cell and analyzed by gas chromatography. The resultant compositions are given in Table A.4 (Appendix A).

The experimental procedures described in the previous Chapter were followed to simultaneously measure the dissociation conditions (section 5.2.1) and the molar compositions of CO\textsubscript{2} and N\textsubscript{2} in the gas phase at different equilibrium conditions (section 5.5.2). All experimental data are tabulated in Tables A.4 and A.5 (Appendix A). The phase equilibrium data generated in this work are compared with the literature data. Predictions through CSMGem and HWHYD models are also reported for comparisons purposes. Regarding the uncertainty of measurements discussed in this section, ± 0.2 K and ± 0.05 MPa are the maximum expected uncertainties in the dissociation data (section 5.2.1), derived from the isochoric plots as explained in Chapter 2. For compositional equilibrium data (section 5.2.2), maximum uncertainties in molar concentrations in the gas phase are estimated to be within ±1-2\%, from TCD calibrations, while measurement uncertainty in the hydrate equilibrium temperature and pressures is estimated to be within ± 0.02 K and ± 0.002 MPa, respectively, from instrument calibrations (Chapter 2). Uncertainties in the amount of liquid supplied to the system are expected to be within ± 0.5\%.

5.2.1 Equilibrium Dissociation Conditions

The hydrate dissociation conditions were investigated at five different composition ratios of CO\textsubscript{2} in the feed gas in the presence of water. The compositions of the (CO\textsubscript{2} + N\textsubscript{2}) gas mixtures are given in the first column of Table A.4 (Appendix A). Average value of at least seven analyses is reported as the composition of the feed for each gas mixture. The measured hydrate dissociation data reported in Table A.4 are plotted in Figure 5.1. The hydrate phase boundaries of pure carbon dioxide and nitrogen hydrates are also shown. As can be observed in Figure 5.1, the experimental data show that the hydrate dissociation pressures of (CO\textsubscript{2} + N\textsubscript{2}) gas mixtures fall in between those of pure CO\textsubscript{2} and N\textsubscript{2} hydrates. It can also be seen from this plot that the hydrate dissociation conditions shift to higher pressures when increasing the N\textsubscript{2}/CO\textsubscript{2} ratio in the feed gas.
Figure 5.1. Experimental dissociation conditions for (nitrogen + carbon dioxide) clathrate hydrates at different CO$_2$ load mole fractions. This work: 0.271 (●); 0.476 (♦); 0.748 (◊); 0.773 (▲); 0.812 (△). HWHYD model: N$_2$ hydrates (solid line); CO$_2$ hydrates (dashed line).
Chapter 5 - Ph.D. Dissertation V. BELANDRIA

Figure 5.2. Experimental dissociation conditions for (nitrogen + carbon dioxide) clathrate hydrates at different CO₂ load mole fractions. This work: 0.271 (●); 0.476 (♦); 0.748 (■); 0.773 (▲); 0.812 (+). Literature: —, 0.9652 (Fan & Guo, 1999); x shadow, 0.830 (Linga et al., 2007b); ◻, 0.778 (Kang et al., 2001); + shadow, 0.570 (Linga et al., 2007b); ◊, 0.4815 (Kang et al., 2001); ○, 0.1761 (Kang et al., 2001); *, 0.169 (Linga et al., 2007b); *, 0.1159 (Kang et al., 2001); x, 0.0063 (Kang et al., 2001). HWHYD model: N₂ hydrates (solid line); CO₂ hydrates (dashed line).

The hydrate dissociation conditions measured in this work and the corresponding literature data are compared in Figure 5.2. The equilibrium data obtained generally agree with the experimental data reported in the literature within stated experimental uncertainties. However, considerable deviation was observed for the dissociation pressures measured at 0.476 and 0.773 mole fraction of CO₂ and 280.7 and 280 K, respectively.
As indicated in section 1.2.2, carbon dioxide and nitrogen are known to form sI and sII hydrates, respectively (Kang & Lee, 2000; Linga et al. 2007a). Literature data reveal that depending on the relative amount of CO\textsubscript{2} and N\textsubscript{2} gas molecules occupied in the small and large cavities, the structure of mixed (CO\textsubscript{2} + N\textsubscript{2}) hydrates can be considered to be either sI or sII (Kang & Lee, 2000). For instance, Kang et al. (2001) have reported a sII transition on hydrates formed at concentrations of 6.63 and 11.59 mole % CO\textsubscript{2} (feed gas) based on the slopes of the equilibrium lines of various (CO\textsubscript{2} + N\textsubscript{2}) hydrates. Motivated by this controversy, possible structural transitions of mixed (CO\textsubscript{2} + N\textsubscript{2}) hydrates were investigated. Nevertheless, based on the slopes of the equilibrium lines no hydrate structural transitions were observed in the concentration range of 0.271 to 0.812 mole fractions CO\textsubscript{2} (in the feed gas). This fact was expected as structural transitions are reported to occur when the CO\textsubscript{2} molar concentration of the feed gas is near 15 mole %. Furthermore, the obtained equilibrium data suggest that the stable hydrate structure for the (CO\textsubscript{2} + N\textsubscript{2}) composition ratio studied in this work is likely structure I. \textit{In situ} Raman spectroscopy measurements carried out by Chazallon (2010) confirm these expectations. Moreover, the results of the latter study indicate that structure II clathrate hydrates of (CO\textsubscript{2} + N\textsubscript{2} + H\textsubscript{2}O) are only formed at low (< 0.019) CO\textsubscript{2} mole fractions (in the gaseous feed).

The reliability of two hydrate thermodynamic models: CSMGem (based on the Gibbs energy minimization) and HWHYD (based on the equality of fugacity of each component throughout all phases) was studied by predicting the hydrate dissociation pressures for the studied (CO\textsubscript{2} + N\textsubscript{2}) gas mixtures. The predictions were obtained at the corresponding equilibrium temperature, CO\textsubscript{2} mole fraction in the feed gas, and water mole fraction introduced to the system. The obtained values are given in Table A.4 (Appendix A). As can be seen, the absolute relative deviation (ARD) of the predicted hydrate dissociation conditions by HWHYD and CSMGem thermodynamic models are in average 3.4 % and 10.3 %, respectively.

Figure 5.3 shows the ARD from the obtained experimental values. The scattering in the predicted values suggest that the parameters of both thermodynamic models may require readjustment using reliable hydrate dissociation experimental data; as such models have generally been developed for hydrates of hydrocarbons.
5.2.2 Compositional Analysis of Equilibrium Phases

All experimental data measured in this study are reported in Table A.5 (Appendix A) and are plotted in Figures 5.4 to 5.7. The compositions of N\textsubscript{2} and CO\textsubscript{2} in the gas phase, under liquid water-hydrate-gas (L\textsubscript{w}-H-G) equilibrium, at different temperatures were experimentally determined for various (CO\textsubscript{2} + N\textsubscript{2}) gas mixtures in the presence of water. It is evident from these measurements that the amount of CO\textsubscript{2} in the gas phase generally decreases, as expected, when pressure increases at a given temperature. This suggests that considerable enrichment of CO\textsubscript{2} in the hydrate phase takes place for the mixed (carbon dioxide + nitrogen) gas hydrates at the temperatures and pressures studied in this work.
Figure 5.4. Pressure - composition phase diagram for (nitrogen + carbon dioxide + water) systems under (L_w-H-G) equilibrium at different temperatures. This work: 273.6 K (■); 275.2 K (♦); 276.1 K (●); 277.2 K (—); 278.1 K (+); 279.7 K (▲).

It is also observed that the composition of CO_2 in the gas phase increases as temperature increases, which translates in less amount of CO_2 trapped in the hydrate phase at high temperatures. The experimental data measured in this work along with the corresponding literature data at selected temperatures are separately shown in Figures 5.5, 5.6a, 5.6b and 5.6c. As it can be seen, the mole fractions of CO_2 in the gas phase compare well with those reported by Seo et al. (2000) and Bruusgaard et al. (2008) at temperatures between 274 and 280 K. However, considerable deviation is observed for the mole fraction of CO_2 in the hydrate phase at high temperatures (e.g. 277 and 280 K).
The molar compositions of the aqueous and hydrate phases are determined by solving a system of non-linear material balance equations. As mentioned earlier, a mathematical algorithm based on Newton’s numerical method (Constantinides & Moustofi, 1999) and coupled with the differential evaluation (DE) optimization strategy (Price & Storn, 1997) is applied. The latter mathematical approach is detailed elsewhere (Belandria et al., 2011). The experimentally measured data, results of solving the material balance equations, and comparison with the predictions of CSMGem thermodynamic model are summarized in Table A.5 (Appendix A) and illustrated in Figures 5.7a-e at selected temperatures. As can be expected, the molar composition of carbon dioxide in the hydrate phase generally decreases as pressure increases for a given temperature, which is physically correct considering that competition for cage occupancy between \( \text{N}_2 \) and \( \text{CO}_2 \) increases at higher pressures. Also, as seen in these figures the predictions of the CSMGem model for the mole fraction of \( \text{CO}_2 \) in the gas phase generally agree with the experimental data. However, this thermodynamic model shows considerable deviations when predicting the molar compositions of \( \text{CO}_2 \) in the hydrate phase. Even much larger deviations (~43 \%) have been recently reported between hydrate phase compositional measurements through Raman spectroscopy and predictions from the same thermodynamic model (Chazallon, 2010). This suggests that parameters of the latter thermodynamic model may require readjustment using three-phase (Lw-H-G) compositional experimental data, as most of these models have been developed for gas hydrates of hydrocarbons using experimental hydrate dissociation data. As for the undetermined values of some of the points shown in Table A.5 related to the predictions of the CSMGem model, the model is not capable of predicting the three-phase equilibrium (Lw-H-G) behavior at the studied conditions. It should be noted that the predictions of HWHYD model are not reported in this work as this model considers that \( \text{N}_2 \) forms structure I clathrate hydrates.

The number of hydrate phase equilibrium data measured in this work for (\( \text{CO}_2 + \text{N}_2 + \text{H}_2\text{O} \)) systems, along with the experimental conditions (\( \text{CO}_2/\text{N}_2 \) feed compositions, equilibrium temperature and pressures) is summarized in Table 5.4. The thermodynamic stability and compositions of the gas, liquid, and hydrate phases of mixed (carbon dioxide + nitrogen) hydrates has been examined at a useful range of temperatures and pressures. These data provide valuable guidelines for the design; selection and adjustment of the parameters of \( \text{CO}_2 \) capture processes based on gas hydrate crystallization concept.
Figure 5.5. Pressure - composition phase diagram for (nitrogen + carbon dioxide + water) systems under (L_w-H-G) equilibrium at selected temperatures.

Table 5.4. Summary of the hydrate phase equilibrium data measured in this work for (CO_2 + N_2 + H_2O) systems.

<table>
<thead>
<tr>
<th>CO_2 molar composition in the feed</th>
<th>Type of data</th>
<th>T Range / K</th>
<th>p Range / MPa</th>
<th>Number of experimental data</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.271 - 0.812</td>
<td>HDC (p,T)</td>
<td>279.2 - 285.3</td>
<td>3.24 - 29.92</td>
<td>9</td>
</tr>
<tr>
<td></td>
<td>GHLE (p,T,x,y,z)</td>
<td>273.6 - 281.7</td>
<td>2.03 - 17.63</td>
<td>35</td>
</tr>
</tbody>
</table>
Figure 5.6. Pressure - composition phase diagram for the (nitrogen + carbon dioxide + water) systems under (L-n-H-G) equilibrium: Experimental and literature data. 
a) This work, 273.6 K: $y_{CO2}$ (■); $z_{CO2}$ (●); Seo et al. (2000), 274 K: $y_{CO2}$ (□); $z_{CO2}$ (○); 
b) This work, 277.2 K: $y_{CO2}$ (■); $z_{CO2}$ (●); Seo et al. (2000), 277 K: $y_{CO2}$ (□); $z_{CO2}$ (○); 
c) This work, 279.7 K: $y_{CO2}$ (■); $z_{CO2}$ (●); Seo et al. (2000), 280 K: $y_{CO2}$ (□); $z_{CO2}$ (○).
Figure 5.7. Pressure-composition phase diagram for the (nitrogen + carbon dioxide + water) systems under (L_w-H-G) equilibrium at selected temperatures. This work (experimental): $y_{CO_2}$ (▲); $z_{CO_2}$ (●). CSMGem model predictions: $y_{CO_2}$ (Δ); $z_{CO_2}$ (○). a) 273.6 K, b) 275.2 K, c) 276.1 K, d) 278.1 K, e) 279.7 K.
5.3 Study of Gas Hydrate Formation in (Carbon Dioxide + Hydrogen + Water) Systems

In this study, the equilibrium dissociation pressures and compositions of the gas phase for (CO$_2$ + H$_2$) hydrates are measured in the CO$_2$ concentration range from (0.508 to 0.829) mole fraction and in the temperature range of (273.6 to 283.0) K at pressures up to about 25 MPa. The studied gas mixtures composed of high purity grade CO$_2$ (99.995 mole %, supplied by Air Liquide) and H$_2$ (over 99.99 mole %, supplied by Air Liquide) were prepared in the equilibrium cell and analyzed by gas chromatography. The resultant compositions are reported in Tables A.6 and A.7 (Appendix A).

The experimental procedures described in the previous chapter were followed to simultaneously measure the dissociation conditions and the molar compositions of CO$_2$ and H$_2$ in the gas phase at different equilibrium pressures and temperatures. The typical uncertainty in these measurements is similar to that reported in the preceding section. All experimental data are tabulated in the Appendix A. The phase equilibrium data generated in this work are at last compared with the literature data.

5.3.1 Equilibrium Dissociation Conditions

The effect of the molar concentration of CO$_2$ was investigated for ternary (CO$_2$ + H$_2$ + H$_2$O) systems at various mole fractions of CO$_2$ to confirm the thermodynamic validity of CO$_2$ hydrate-based separation from fuel gas mixtures. The three-phase (L$_w$-H-G) equilibrium measurements were carried out following the experimental procedure described in Chapter 4. The (CO$_2$ + H$_2$) gas mixtures were investigated in the (0.508, 0.709, and 0.829) relative molar fractions of CO$_2$, with an estimated experimental uncertainty of $\pm$ 1-2 % on molar compositions, derived from gas chromatograph detector calibration.

The experimental dissociation conditions of (CO$_2$ + H$_2$) gas hydrates are given in Table A.6 (Appendix A). Figure 5.8 shows the semi-logarithm plot of the dissociation pressure as a function of temperature. Literature data are given in Table 5.3 and are also shown in Figure 5.8. A consistent agreement with the dissociation conditions measured in this work is generally found. The dissociation pressures generally shift to higher values as the molar concentration of
CO₂ decreases in the feed in the temperature range of (277.2 to 283.0) K. A drastic increase in the dissociation pressure is particularly observed at high temperatures for hydrates formed from the 0.508 CO₂ mole fraction gas mixtures. As can be noted, the dissociation pressure rapidly increases from 8.53 MPa (at 280.5 K) to 24.76 MPa at the equilibrium temperature of 283.0 K. Such behavior could be attributed to the fact that H₂ begins to compete with CO₂ for hydrate cage occupancy with the increase in the H₂ mole fraction within the (CO₂ + H₂) gas mixture (Kumar et al., 2009 and Li et al., 2010).

Figure 5.8. Experimental (literature and this work) dissociation conditions for gas hydrates of (CO₂ + H₂) formed in the presence water at various feed gas compositions.
Linga and coworkers (2007b) stated that “hydrate formation pressure increases with temperature and in order to minimize compression costs the smallest possible pressure is desired”. Thus, based on the obtained results and considering the relative concentration of CO$_2$ in flue gas or synthesis gas is approximately 40 mole% (Klara & Srivastava, 2002), it is expected that high energy requirements may be necessary for separating CO$_2$ from H$_2$ through hydrate formation at relatively high temperatures. However, no hydrate dissociation data are available in the literature at temperatures above the value of 281.4 K reported by Kumar et al. (2006) for a CO$_2$ mole fraction of 0.579. Further phase behavior studies are therefore required at higher temperatures for H$_2$-rich binary gas mixtures for better assessing the strong dependency of the dissociation pressures on the molar concentration of CO$_2$ in (CO$_2$ + H$_2$ + H$_2$O) ternary hydrates.

5.3.2 Compositional Analysis of Equilibrium Phases

Compositional data for the gas phase in equilibrium with the hydrate and aqueous phases were measured at different pressures and temperatures for various (CO$_2$ + H$_2$) gas mixtures in the presence of water. The molar compositions of CO$_2$ in the feed gas along with the temperature, pressure and compositions of the gas phase are given in Table A.7 (Appendix A) and shown in Figure 5.9 (water concentration is assumed negligible in the gas phase). The experimental results indicate that as pressure increases, the composition of CO$_2$ in the gas phase decreases. This may suggest that considerable enrichment of CO$_2$ in the hydrate phase takes place in the studied systems. However, it should be noted that in (CO$_2$ + H$_2$) mixed hydrates, H$_2$ is assumed to be not enclathrated in the hydrate cages and to behave as a diluent gas towards the formation of CO$_2$ hydrate (Sugahara et al., 2005).

Table 5.5 summarizes the experimental conditions at which compositional data for the gas and hydrate phases have been reported in the literature for the (carbon dioxide + hydrogen + water) ternary systems. In Figure 5.10, the experimental data measured in this work and literature data are compared. As can be seen, a consistent agreement is generally found with the experimental data reported by Sugahara et al. (2005) and Kumar et al. (2006) within experimental
uncertainties. However, considerable deviation is observed for the composition of CO$_2$ in the gas phase reported by Seo and Kang (2010) at 274.15 K.

The molar compositions of the gaseous components in the hydrate phase for the (CO$_2$ + H$_2$ + H$_2$O) systems have been subject of few studies in the literature. Table 5.5 summarizes the main findings reported in those studies. It is clear that the contradictory results are mainly due to three factors: a) Temperature and pressure conditions, b) Molar compositions of the introduced gaseous feed to the system, and c) The experimental techniques. Those who have claimed that H$_2$ can be trapped into the hydrate cages generally conducted their experiments at very low temperatures. Another factor to consider is that high ratios of H$_2$ to CO$_2$ in the gaseous feed were used. As this composition is increased, the possibility of H$_2$ enclathration into the hydrate cages can be intrinsically increased. Different experimental techniques used for studying the molar compositions of the hydrate phase may also affect the obtained results. Considering the above facts, it is considered that at the experimental conditions investigated in this study only CO$_2$ is trapped inside gas hydrate cavities. However, as previously mentioned, further experimental works using suitable physical techniques (e.g., NMR, X-ray, or Raman spectroscopy) are recommended for further examining the latter assumption.

The number of hydrate phase equilibrium data measured in this work for (CO$_2$ + H$_2$ + H$_2$O) systems, along with the experimental conditions (CO$_2$/H$_2$ feed compositions and equilibrium temperatures and pressures) is summarized in Table 5.56. These experimental data provide valuable information on the thermodynamic stability and gas phase compositions of mixed (carbon dioxide + hydrogen) gas hydrates at useful temperatures and pressures, which can be taken into account in the design of CO$_2$ pre-combustion processes based on gas hydrate crystallization concept.
Figure 5.9. Pressure - gas phase composition phase diagram for (hydrogen + carbon dioxide + water) systems under (L,\textsubscript{w}-H-G) equilibrium at different temperatures. This work: 273.6 K (■); 275.2 K (●); 276.2 K (●); 277.1 K (-); 278.1 K (+); 279.1 K (▲); 280.1 K (x); 281.2 K (▬).
Table 5.5. Experimental studies on molar compositions of gas hydrates formed in the (CO\(_2\) + H\(_2\) + H\(_2\)O) ternary systems.

<table>
<thead>
<tr>
<th>Authors</th>
<th>Gaseous feed compositions introduced to the system / CO(_2) mole fraction</th>
<th>(T / K)</th>
<th>(p / MPa)</th>
<th>Experimental technique</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sugahara et al.</td>
<td>Not reported</td>
<td>274.3-281.9</td>
<td>1.42-10</td>
<td>Raman micro-spectroscopy</td>
<td>No H(_2) cage occupancy was observed</td>
</tr>
<tr>
<td>(2005)</td>
<td></td>
<td></td>
<td></td>
<td>Raman spectroscopy using quartz windows</td>
<td>No H(_2) cage occupancy was observed</td>
</tr>
<tr>
<td>Sugahara et al.</td>
<td>Not reported</td>
<td>274.3-281.9</td>
<td>1.42-10</td>
<td>Direct gas release method</td>
<td>H(_2) molecules adsorb on the hydrate structure (0.007 water-free base mole fraction in the hydrate phase )</td>
</tr>
<tr>
<td>Kumar et al.</td>
<td>0.4</td>
<td>163 to 278</td>
<td>8</td>
<td>Gas chromatography of released gas from hydrate</td>
<td>92 mole % CO(_2) and 8 mole % H(_2) were trapped in the hydrate phase</td>
</tr>
<tr>
<td>(2009)</td>
<td></td>
<td></td>
<td></td>
<td>C NMR</td>
<td>sI hydride formed, 100 % of the large cages were occupied by CO(_2)</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Raman spectroscopy</td>
<td>sI hydride formed</td>
</tr>
<tr>
<td>Seo and Kang</td>
<td>0.41</td>
<td>274.15</td>
<td>6.5-8.9</td>
<td>C NMR</td>
<td>If silica gel is used to form hydrate, 93 % of small cages and 100 % of large cases are occupied by CO(_2)</td>
</tr>
<tr>
<td>(2010)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Molar composition of CO(_2) in the hydrate phase in the range of (96.5 to 98.7)</td>
</tr>
<tr>
<td>Kim and Lee</td>
<td>0.2</td>
<td>123.15</td>
<td>0.1</td>
<td>H MAS NMR</td>
<td>H(_2) was entrapped in hydrate</td>
</tr>
<tr>
<td>(2005)</td>
<td></td>
<td></td>
<td></td>
<td>Gas chromatography of released gas from hydrate</td>
<td>92.5 % CO(_2), 7.5 % H(_2)</td>
</tr>
</tbody>
</table>
Figure 5.10. Pressure - gas phase composition phase diagram for (hydrogen + carbon dioxide + water) systems under \((L_w-H-G)\) equilibrium at different temperatures. This work: (■) 273.6 K; (♦) 275.2 K; (●) 276.2 K; (-) 277.1 K; (+) 278.1 K; (▲) 279.1 K; 280.1 K (●); 281.2 K (* shadow). Literature data: Sugahara et al. (2005): (□) 274.3 K; (◊) 276.5 K; (○) 280.1 K; (▲) 281.9 K; Kumar et al. (2006): (x) 273.9 K; (+ shadow) 277 K; Seo and Kang (2010): (*) 274.15 K.

Table 5.6. Summary of the hydrate phase equilibrium data measured in this work for the \((\text{CO}_2 + \text{H}_2 + \text{H}_2\text{O})\) systems.

<table>
<thead>
<tr>
<th>Feed Composition</th>
<th>Type of data</th>
<th>(T) Range / K</th>
<th>(p) Range / MPa</th>
<th>Number of experimental data</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.508 - 0.829</td>
<td>HDC ((p,T))</td>
<td>277.0 - 283.0</td>
<td>2.44 - 24.76</td>
<td>8</td>
</tr>
<tr>
<td></td>
<td>GHLE ((p,T,y))</td>
<td>273.6 - 281.2</td>
<td>1.75 - 8.57</td>
<td>32</td>
</tr>
</tbody>
</table>
Thermodynamic Stability of Semi-Clathrate Hydrates

6

Résumé

Dans ce chapitre, nous étudions la stabilité thermodynamique des semi-clathrates de TBAB avec des gaz purs et des mélanges de gaz. En premier lieu, nous présentons les résultats des mesures d'équilibres de phases réalisées sur les semi-clathrates formés à partir de : (CO₂, CH₄ ou N₂ + TBAB + H₂O). Ensuite, les variables fondamentales du processus telles que conditions de dissociation et composition des phases font l'objet d'une enquête approfondie pour déterminer les régions de stabilité et les conditions de formation des semi-clathrates dans le mélange : (CO₂ + N₂ + TBAB + H₂O). Les conditions de dissociation sont mesurées en utilisant la méthode isochorique avec variation de la pression en fonction de la température décrite au chapitre 4. Les changements, à différentes températures, des compositions des phases gazeuse et liquide pour les équilibres à trois phases sont mesurés par chromatographie en phase gazeuse et réfractométrie, respectivement. L'effet de promotion thermodynamique dû au TBAB en solutions aqueuses est étudié en termes de pressions et de températures de dissociation. Les conditions d'exploitation les plus favorables pour un procédé de séparation du CO₂ basé sur l'utilisation des hydrates sont alors proposées. Les prédicitions par des modèles thermodynamiques issus de la littérature sont également utilisées pour examiner l'effet promoteur d'hydrate du TBAB. Les résultats complets de l'étude permettent de montrer que le CO₂ peut être séparé des gaz industriels / de combustion qu'il soit à très faibles ou très haute concentrations, et ce, à des températures douces et des pressions basses pourvu que des solutions aqueuses de TBAB soient utilisées.

Abstract

In this chapter, the thermodynamic stability of TBAB semi-clathrates with pure and mixed gases is studied. First, phase equilibrium measurements carried out for semi-clathrates formed from (CO₂, CH₄ or N₂ + TBAB + H₂O) are presented. Then, fundamental process variables such as dissociation conditions and phase compositional data are thoroughly investigated to determine the stability regions and formation conditions of (CO₂ + N₂ + TBAB + H₂O) semi-clathrates. The dissociation data are measured using the isochoric pressure search method described in Chapter 4. The compositional changes in the gas and liquid phases at different temperatures under three-phase equilibrium are measured by gas chromatography and refractometry technique, respectively. The thermodynamic promotion effect of TBAB in aqueous solutions is studied in terms of dissociation pressures and temperatures and the most favorable operating conditions for a hydrate-based CO₂ separation process are proposed. The predictions of literature thermodynamic models are also used to examine the hydrate promotion effect of TBAB. The measured data suggest that CO₂ can be separated from highly to low concentrated industrial / flue gas mixtures at mild temperatures and low pressures in the presence of TBAB aqueous solutions.
Thermodynamic Stability of Semi-Clathrate Hydrates

Introduction

Gas hydrates formation under low temperature and high pressure conditions has been experimentally established in Chapters 3 through 5 for gas mixtures containing CO₂ in the absence of thermodynamic promoter.

As it has been previously discussed, besides pressure, temperature, and composition of the gas mixture, the formation and dissociation of gas hydrates may be also affected by the use of chemical additives with inhibition or promotion effect (Mandal & Laik, 2008). Moreover, the use of hydrate promoters has proven to reduce the pressures required for hydrate stability and increasing the gas hydrate equilibrium temperature. In addition, considerable efforts are currently undergoing to investigate the gas hydrate crystallization approach for separating a specific gas constituent from a multi-component gaseous mixture under favorable temperature and pressure conditions. Therefore, in this chapter the hydrate promotion effect of TBAB aqueous mixtures is investigated.

Relevant experimental literature data (from thermodynamic point of view) in the systems including CH₄, CO₂, N₂ and (CO₂ + N₂) gas mixtures in the presence of TBAB aqueous solutions are provided in Tables 6.1 to 6.4. In spite of the increasing amount of experimental studies reported in the literature in recent years, the role of TBAB in the selective removal of CO₂ from multi-component gas streams is still not clearly understood. Therefore, further experimental phase equilibrium data in the above systems are required for practical purposes and also for tuning predictive thermodynamic models for semi-clathrate systems.

In this study, an attempt has been made to generate in addition to the commonly reported pressure and temperature equilibrium data, reliable compositional equilibrium data for TBAB semi-clathrate hydrates of pure and mixed gases. Such data are normally difficult to measure, time consuming, expensive, and thus rare in the literature. The typical cost of a week effort for obtaining one equilibrium data point is estimated to be about US$2000 (Sloan & Koh, 2008).
### Table 6.1. Experimental data available in the literature for (CH<sub>4</sub> + TBAB) semi-clathrates.

<table>
<thead>
<tr>
<th>Reference</th>
<th>TBAB concentration (mass fraction)</th>
<th>T range / K</th>
<th>p range / MPa</th>
<th>Number of data points</th>
</tr>
</thead>
<tbody>
<tr>
<td>Arjmandi et al. (2007)</td>
<td>0.05, 0.10, 0.20, 0.30</td>
<td>(287.15-298.15)</td>
<td>(1.421-41.369)</td>
<td>24</td>
</tr>
<tr>
<td>Oyama et al. (2008)</td>
<td>0.10</td>
<td>(282.15-287.95)</td>
<td>(0.510-3.650)</td>
<td>7</td>
</tr>
<tr>
<td>Li et al. (2010)</td>
<td>0.05, 0.099, 0.197, 0.385</td>
<td>(281.15-295.15)</td>
<td>(0.460-10.640)</td>
<td>40</td>
</tr>
<tr>
<td>Mohammadi and Richon (2010)</td>
<td>0.05</td>
<td>(283.6-290.1)</td>
<td>(1.310-11.080)</td>
<td>10</td>
</tr>
<tr>
<td>Sun and Sun (2010)</td>
<td>0.05, 0.10, 0.20, 0.2818, 0.45</td>
<td>(281.75-292.35)</td>
<td>(0.508-7.042)</td>
<td>40</td>
</tr>
</tbody>
</table>

### Table 6.2. Experimental data available in the literature for (CO<sub>2</sub> + TBAB) semi-clathrates.

<table>
<thead>
<tr>
<th>Reference</th>
<th>TBAB concentration (mass fraction)</th>
<th>T range / K</th>
<th>p range / MPa</th>
<th>Number of data points</th>
</tr>
</thead>
<tbody>
<tr>
<td>Duc et al. (2007)</td>
<td>0.05, 0.10, 0.40, 0.65</td>
<td>(279.3-290.9)</td>
<td>(0.273-3.320)</td>
<td>8</td>
</tr>
<tr>
<td>Arjmandi et al. (2007)</td>
<td>0.10, 0.427</td>
<td>(285.6-291.2)</td>
<td>(1.250-4.090)</td>
<td>7</td>
</tr>
<tr>
<td>Oyama et al. (2008)</td>
<td>0.01, 0.02, 0.03, 0.045, 0.10</td>
<td>(276.7-289.6)</td>
<td>(0.560-4.530)</td>
<td>44</td>
</tr>
<tr>
<td>Lin et al. (2008)</td>
<td>0.901, 0.702, 0.443</td>
<td>(279.4-288.1)</td>
<td>(0.344-2.274)</td>
<td>24</td>
</tr>
<tr>
<td>Deschamps and Dalmazzone (2009)</td>
<td>0.40</td>
<td>(286.5-288.6)</td>
<td>(0.830-2.250)</td>
<td>4</td>
</tr>
<tr>
<td>Li et al. (2010)</td>
<td>0.05, 0.10</td>
<td>(280.2-288.8)</td>
<td>(0.400-3.210)</td>
<td>11</td>
</tr>
</tbody>
</table>

### Table 6.3. Experimental data available in the literature for (N<sub>2</sub> + TBAB) semi-clathrates.

<table>
<thead>
<tr>
<th>Reference</th>
<th>TBAB concentration (mass fraction)</th>
<th>T range / K</th>
<th>p range / MPa</th>
<th>Number of data points</th>
</tr>
</thead>
<tbody>
<tr>
<td>Arjmandi et al. (2007)</td>
<td>0.10</td>
<td>(285.15-292.95)</td>
<td>(4.688-33.503)</td>
<td>7</td>
</tr>
<tr>
<td>Duc et al. (2007)</td>
<td>0.05, 0.10</td>
<td>(279.3-284.0)</td>
<td>(2.900-10.850)</td>
<td>3</td>
</tr>
<tr>
<td>Deschamps and Dalmazzone (2009)</td>
<td>0.40</td>
<td>(286.0-291.6)</td>
<td>(6.27-20.5)</td>
<td>5</td>
</tr>
<tr>
<td>Lee et al. (2010)</td>
<td>0.50, 0.20, 0.40, 0.60</td>
<td>(81.3-289.4)</td>
<td>(4.040-9.490)</td>
<td>19</td>
</tr>
</tbody>
</table>
This chapter is divided in two parts. In the first part, the thermodynamic stability of semi-clathrates of \((\text{CO}_2, \text{CH}_4 \text{ or } \text{N}_2 + \text{TBAB})\) in non-stoichiometric aqueous solutions is examined. The second part deals with measurements of equilibrium and compositional properties for \((\text{CO}_2 + \text{N}_2)\) gas mixtures in TBAB aqueous mixtures.

Table 6.4. Experimental data available in the literature for \((\text{CO}_2 + \text{N}_2 + \text{TBAB})\) semi-clathrates.

<table>
<thead>
<tr>
<th>Reference</th>
<th>Feed Gas Composition</th>
<th>TBAB mass fraction</th>
<th>Range of experiments</th>
<th>Number of experimental points</th>
<th>Type of data*</th>
</tr>
</thead>
</table>
| Duc et al. (2007)          | \(
\begin{align*}
\text{CO}_2 \ (0.155 \text{ mole}) \\
+ \text{N}_2 \ (0.845 \text{ mole})
\end{align*}
\) | 0.05               | 287.15 - 289.75 K 5.00 - 5.32 MPa | 4 | GHLE \((p,T)\) and GHLE \((p,y,z)\) at 285.15 and 286.15 K |
|                           | \(
\begin{align*}
\text{CO}_2 \ (0.192 \text{ mole}) \\
+ \text{N}_2 \ (0.808 \text{ mole})
\end{align*}
\) |                    | 286.25 - 295.25 K 3.63 - 4.43 MPa | 6 |  |
|                           | \(
\begin{align*}
\text{CO}_2 \ (0.215 \text{ mole}) \\
+ \text{N}_2 \ (0.785 \text{ mole})
\end{align*}
\) |                    | 282.25 - 286.95 K 0.55 - 1.92 MPa | 4 |  |
|                           | \(
\begin{align*}
\text{CO}_2 \ (0.234 \text{ mole}) \\
+ \text{N}_2 \ (0.766 \text{ mole})
\end{align*}
\) |                    | 285.75 - 286.75 K 3.12 - 3.23 MPa | 3 |  |
| Fan et al. (2009)          | \(
\begin{align*}
\text{CO}_2 \ (0.166 \text{ mole}) \\
+ \text{N}_2 \ (0.834 \text{ mole})
\end{align*}
\) | 0.05               | 277.65 K 3.36 - 7.31 MPa | 7 | VHE \((p,T,y,z)\) |
| Deschamps and Dalmazzone (2009) | \(
\begin{align*}
\text{CO}_2 \ (0.249 \text{ mole}) \\
+ \text{N}_2 \ (0.751 \text{ mole})
\end{align*}
\) | 0.40               | 284.8 - 293.3 K up to 9.180 MPa | 5 | HDC \((p,T)\) |
| Lu et al. (2009)           | \(
\begin{align*}
\text{CO}_2 \ (0.159 \text{ mole}) \\
+ \text{N}_2 \ (0.841 \text{ mole})
\end{align*}
\) | 0.05, 0.153, 0.348, 0.407, 0.457 | 278.05 - 287.85 K 1.17 - 5.84 MPa | 12 | HDC \((p,T)\) |
| Meysel et al. (2011)       | \(
\begin{align*}
\text{CO}_2 \ (0.75 \text{ mole}) \\
+ \text{N}_2 \ (0.25 \text{ mole})
\end{align*}
\) | 0.05, 0.1, 0.2     | 284.1 - 290.0 MPa 1.964 - 3.822 MPa | 14 |  |
|                           | \(
\begin{align*}
\text{CO}_2 \ (0.50 \text{ mole}) \\
+ \text{N}_2 \ (0.50 \text{ mole})
\end{align*}
\) |                    | 282.3 - 290.4 K 1.956 - 5.754 MPa | 16 | HDC \((p,T,y)\) |
|                           | \(
\begin{align*}
\text{CO}_2 \ (0.20 \text{ mole}) \\
+ \text{N}_2 \ (0.80 \text{ mole})
\end{align*}
\) |                    | 281.8 - 288.3 K 2.976 - 5.901 MPa | 12 |  |

6.1 Phase Equilibria of Semi-Clathrate Hydrates of Carbon Dioxide, Methane and Nitrogen in Non-Stoichiometric TBAB Aqueous Solutions

In spite of the number of experimental studies dedicated to understanding the phase behavior of TBAB sc hydrates, the thermodynamic properties of TBAB semi-clathrates with carbon dioxide, methane or nitrogen have been scarcely studied above the TBAB stoichiometric composition, namely 0.4 and 0.32 mass fraction, for type A and B hydrates, respectively (Lin *et al.*, 2008). The equilibrium temperature for the pure TBAB hydrate of stoichiometric composition at atmospheric pressure is 285.15 K (Shimada *et al.*, 2003). Therefore, it is expected that the use of TBAB with gases like CO$_2$, CH$_4$ or N$_2$ yields a reduction in the equilibrium pressure and thereby extend the hydrate stability region to higher temperatures. At the time of writing, the only experimental dissociation data available in the literature in a non-stoichiometric concentration of TBAB aqueous solution are those reported by Duc *et al.* (2007) for sc of (TBAB + CO$_2$) at 0.65 mass fraction TBAB in aqueous solution, and by Hashimoto and coworkers (2008) for (hydrogen + TBAB) semi-clathrates.

In the present work, dissociation pressures of (CO$_2$, CH$_4$ or N$_2$ + TBAB) sc hydrate systems are investigated at 0.25 and 0.50 mass fraction of TBAB in aqueous solution in the temperature ranges of (282.6 to 287.9), (285.6 to 292.8), and (286.1 to 289.1) K, respectively. Purities and suppliers of the chemicals used are given in Table 6.5. Solutions with mass fractions of 0.25 were prepared by gravimetric method using an accurate analytical balance (Mettler, AT200), with mass uncertainty of ± 0.0001 g. Consequently, uncertainties on the basis of mole fraction are estimated to be less than 0.01. Double-distilled and deionized water from Direct-Q5 Ultrapure Water Systems (Millipore™), with a resistivity of 18.2 MΩ cm at 298 K, was used in all experiments.

The dissociation measurements were carried out following the isochoric pressure search method described in Chapter 4. The measured data are given in Tables A.8 and A.9 (Appendix A) and are plotted in Figures 6.1 to 6.3. The uncertainties for the hydrate dissociation temperatures and pressures are expected to be within ± 0.2 K and ± 0.05 MPa, as indicated in Chapter 2.
also shown in Figures 6.1 to 6.3 to study the hydrate promotion effect of TBAB above its stoichiometric concentration.

A semi-logarithmic scale is used to better study the hydrate promotion effects of TBAB aqueous solutions and also the consistency of the experimental data. It should be emphasized that hydrate promotion effect means shifting to low pressures / high temperatures the dissociation conditions of gas hydrates due to the presence of TBAB in the aqueous solution (Sloan & Koh, 2008). As observed in Figures 6.1 to 6.3, the data measured in this work are in consistent agreement with literature data in the whole region where a comparison could be made.

Many experimental dissociation data have been reported for (methane + TBAB) and (carbon dioxide + TBAB) semi-clathrates at concentrations below 0.40 (mass fraction TBAB). Figures 6.1 and 6.2 show as expected, that a concentration of 0.25 mass fraction TBAB shifts the three-phase equilibrium curves to the lower pressures / higher temperatures region when compared to the corresponding gas hydrates systems (without TBAB). A comprehensive phase equilibrium study at additional TBAB concentrations in its aqueous solutions can be found in the paper of Mohammadi et al. (2011a). Interestingly, the addition of 0.50 mass fraction TBAB in aqueous solution generally weakens its pressure-reducing effect in the temperature ranges studied in this work, in comparison to lower concentrations relative to water (i.e. 0.25 mass fraction TBAB) that significantly decrease the dissociation pressure at a given temperature. However, this effect depends on pressure and can vary for each semi-clathrate system. The promotion effect is indeed considerable for the nitrogen containing systems.

### Table 6.5. Purities and suppliers of materials.

<table>
<thead>
<tr>
<th>Chemical</th>
<th>Supplier</th>
<th>Purity</th>
</tr>
</thead>
<tbody>
<tr>
<td>Carbon dioxide</td>
<td>Air Liquide</td>
<td>0.99 (mole fraction)</td>
</tr>
<tr>
<td>Nitrogen</td>
<td>Air Liquide</td>
<td>0.99 (mole fraction)</td>
</tr>
<tr>
<td>Methane</td>
<td>Air Liquide</td>
<td>0.99 (mole fraction)</td>
</tr>
<tr>
<td>TBAB aqueous solution,</td>
<td>Sigma-Aldrich</td>
<td>0.99 (mass fraction)</td>
</tr>
<tr>
<td>50.00 ±0.01 (mass %)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
For (TBAB + nitrogen) semi-clathrates, the addition of 0.50 mass fraction TBAB aqueous solutions (*i.e.* non-stoichiometric aqueous solution) unexpectedly causes a continued decrease in the equilibrium pressure at a given temperature. Furthermore, an unusual behavior is particularly observed in Figure 6.3 at temperatures below 286.5 K with the addition of 0.25 and 0.50 mass fraction of TBAB in aqueous solutions. Oyama *et al.* (2005) demonstrated that two types of TBAB hydrates, namely type A and type B, are formed over the concentration range from 0 to 45 wt.%. Possible structural transitions from type A to type B and/or coexistence of both crystal structures could cause such an abrupt pressure decrease, compared to smaller concentrations (*i.e.* 0.05 and 0.10 mass fraction TBAB) which display rather parallel straight lines.

As the crystal structure of semi-clathrates typically depends on the hydration number, it is not possible to withdraw any conclusion regarding semi-clathrates structural transitions from phase equilibrium measurements by PVT studies alone (as performed in this work). The use of suitable physical techniques (*e.g.* NMR, Raman spectroscopy, *etc.*) is therefore recommended to further investigate such phenomena, especially for studying compositional changes in (TBAB + N₂) semi-clathrates. The dissociation data presented in this section are of scientific interest, since they are the first to show the thermodynamic stability of (CH₄ or N₂ + TBAB) semi-clathrates in non-stoichiometric aqueous solutions.
Figure 6.1. Experimental dissociation conditions (literature and this work) for (methane + TBAB) semi-clathrates.
Figure 6.2. Experimental dissociation conditions (literature and this work) for (carbon dioxide + TBAB) semi-clathrates.
Figure 6.3. Experimental hydrate dissociation conditions (literature and this work) for (nitrogen + TBAB) semi-clathrates.
6.2 Thermodynamic Properties of Semi-Clathrate Hydrates of (Carbon Dioxide + Nitrogen) Gas Mixtures in TBAB Aqueous Mixtures

This section is devoted to further investigate the thermodynamic validity of a hydrate-based CO₂ separation process from industrial/flue gases by using TBAB as thermodynamic promoter. Dissociation and compositional data for the (CO₂ + N₂ + TBAB + water) systems with various CO₂ feed gas molar compositions were experimentally measured in the (275.2 to 291.0) K and (0.58 to 19.09) MPa ranges, using the methodologies described in Chapter 4. In addition, the refractive index of the liquid phase was measured under three-phase equilibrium to determine its composition at each temperature step (during dissociation). With respect to the accuracy of the experimental data, ± 0.2 K and ± 0.05 MPa are the maximum expected uncertainties, derived from the isochoric plots, in the dissociation measurements (section 6.2.1). For compositional data (section 6.2.2), maximum uncertainties in molar concentrations in the gas phase are estimated to be within ± 1-2%, from TCD calibrations, while measurement uncertainty in the equilibrium temperature and pressures is estimated to be better than ± 0.02 K and ± 0.002 MPa, respectively, from instrument calibrations (Chapter 2). The maximum deviations on refractive index measurement are expected to be about ± 0.1%. Uncertainties in the amount of TBAB aqueous solution supplied to the system are expected to be lower than ± 0.5%, in both studies presented in sections 6.2.1 and 6.2.2.

The three gas mixtures used in this work were supplied by Air Liquide and their compositions were chosen to cover a wide range of CO₂ and N₂ ratios. The relative molar fractions of CO₂ were (0.151, 0.399, and 0.749) with 2% of relative uncertainty on the molar composition stated by the supplier. TBAB with 99 wt. % purity was purchased from Sigma-Aldrich. Double-distilled and deionized water from Direct-Q5 Ultrapure Water Systems (Millipore™), with a resistivity of 18.2 MΩ cm at 298 K, was used in all experiments. TBAB aqueous mixtures with mass fractions of (0.05 and 0.30) were prepared following the gravimetric method described in section 6.1. Thus, uncertainties on the basis of mole fraction are estimated to be less than 0.01.

Semi-clathrates were formed with the addition of TBAB aqueous solutions with mass fractions of (0.05 and 0.30). The measured dissociation data are discussed and compared with literature
data. The promotion effect of TBAB under different conditions (temperature, pressures and gas phase compositions) is studied to determine the stability region of the \((\text{CO}_2 + \text{N}_2)\) semi-clathrates and the most favorable operating conditions for separating \(\text{CO}_2\) from flue gases through sc hydrate formation.

### 6.2.1 Phase Equilibrium Measurements for Semi-Clathrate Hydrates of the \(\text{CO}_2 + \text{N}_2 + \text{Tetra-n-Butylammonium Bromide Aqueous Solution Systems}

Depending on the industrial application, the concentration of \(\text{CO}_2\) in the gas mixture to be treated can significantly vary over the whole composition range. For instance, in large-scale power plants, flue gas typically contains mostly \(\text{N}_2\) and usually low to medium \(\text{CO}_2\) fractions. Three different molar concentrations of \(\text{CO}_2\) (0.151, 0.399 and 0.749) in the feed gas are studied to cover a large range of industrial interest. The dissociation conditions for \((\text{CO}_2 + \text{N}_2)\) semi-clathrates from TBAB aqueous solutions with mass fractions of (0.05 and 0.30) were experimentally measured to confirm the thermodynamic feasibility of the separation process.

The equilibrium dissociation measurements were carried out in the (281.0 to 291.0) K and (0.67 to 19.07) MPa ranges. A summary of the experimental conditions at which the equilibrium data were measured is provided in Table 6.6. The results are shown in the pressure-temperature phase diagrams of Figures 6.4 to 6.7. All equilibrium data along with the corresponding feed gas compositions and mass fractions of TBAB in aqueous solutions are given in Table A.10 (Appendix A).

The phase boundaries shown in Figures 6.4 \((a\ and\ b)\) define the pressure and temperature region at which \((\text{CO}_2 + \text{N}_2 + \text{TBAB})\) semi-clathrates are thermodynamically stable. Typical flue gas mixtures (0.151 mole fraction \(\text{CO}_2\)) can form hydrates with water at 275.2 K and pressures above 10.103 MPa (Belandria et al., 2011). However, such a high pressure requirement may be considered as a major drawback of the hydrate-based separation process because of the high energy costs implicated (Spencer, 1997). As mentioned earlier, most favorable operating conditions are expected to be achieved in the presence of TBAB (Shimada et al., 2003; Duc et
al., 2007; Fan et al., 2009). Therefore, the promotion effect of TBAB is investigated at two different salt concentrations in aqueous solutions.

As expected, by adding 0.05 mass fractions TBAB in aqueous solutions (Figure 6.4a), CO₂ can be separated from a typical flue gas mixture at 282.6 K and 3.157 MPa. The minimum equilibrium dissociation condition is shifted to 285.7 K and 1.568 when 0.30 mass fraction TBAB aqueous solutions are added (Figure 6.4b). A significant decrease in the equilibrium dissociation pressure is observed for all studied gas mixtures in the presence of TBAB. Although the experimental determination of the dissociation data for the (CO₂ + N₂ + TBAB + water) systems was restricted to three-phase (gas-hydrate-liquid) equilibrium, the upper phase boundaries (0.151 and 0.399 mole fraction CO₂) intersect at temperatures below 282.7 K (Figure 6.4a). Thus, the data measured below this temperature most likely represent dissociation conditions for TBAB semi-clathrates (without gas).

As can be expected from the equilibrium pressure-temperature diagrams of Figures 6.4 to 6.7, semi-clathrates of (CO₂ + N₂ + TBAB) form at lower pressures than gas hydrates of (CO₂ + N₂) at a given temperature. Similar findings on the thermodynamic promotion effect of TBAB semi-clathrate hydrates of (CO₂ + N₂) have been reported in the literature (Meysel et al., 2011; Mohammadi et al., 2011b). In sum, it can be observed that increasing the concentration of TBAB (at constant temperature) decreases the pressure required for semi-clathrate hydrate formation. In contrast, the required pressure for forming semi-clathrates is increased as the concentration of nitrogen in the feed gas increases under the same concentration of TBAB and temperature. Comparable results on the dependency of the required pressure for semi-clathrate formation with the feed gas composition and TBAB concentration are reported in the work of Meysel et al. (2011).
Figure 6.4. Dissociation conditions for semi-clathrates of (CO$_2$ + N$_2$) formed at various CO$_2$ feed gas compositions in the presence of TBAB aqueous solutions: a) 0.05 mass fraction TBAB; b) 0.30 mass fraction TBAB. This work: ♦, 0.151 mole fraction; ●, 0.399 mole fraction; ▲, 0.749 mole fraction. Literature: ◊, 0.151 mole fraction (Mohammadi et al., 2011b); ○, 0.399 mole fraction (Mohammadi et al., 2011b); Δ, 0.75 mole fraction (Meysel et al., 2011).
Table 6.6. Semi-clathrate hydrate phase equilibrium data (this work) for the (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems.

<table>
<thead>
<tr>
<th>Feed Composition</th>
<th>TBAB mass fraction</th>
<th>Type of data</th>
<th>$T$ Range / K</th>
<th>$p$ Range / MPa</th>
<th>Number of experimental points</th>
</tr>
</thead>
<tbody>
<tr>
<td>CO$_2$ (0.151 mole) + N$_2$ (0.849 mole)</td>
<td>0.05, 0.15, 0.30</td>
<td>HDC ($p,T$)</td>
<td>282.4 - 285.7</td>
<td>1.55 - 19.07</td>
<td>7</td>
</tr>
<tr>
<td></td>
<td>0.05</td>
<td>GHLE ($p,T,x,y$)</td>
<td>275.2 - 289.2</td>
<td>12.254 - 19.085</td>
<td>17</td>
</tr>
<tr>
<td>CO$_2$ (0.399 mole) + N$_2$ (0.601 mole)</td>
<td>0.05, 0.15, 0.30</td>
<td>HDC ($p,T$)</td>
<td>283.6 - 287.1</td>
<td>1.78 - 6.58</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>0.05, 0.30</td>
<td>GHLE ($p,T,x,y$)</td>
<td>275.2 - 287.2</td>
<td>1.633 - 6.575</td>
<td>28</td>
</tr>
<tr>
<td>CO$_2$ (0.749 mole) + N$_2$ (0.251 mole)</td>
<td>0.05, 0.30</td>
<td>HDC ($p,T$)</td>
<td>281.0 - 291.0</td>
<td>0.67 - 3.70</td>
<td>10</td>
</tr>
<tr>
<td></td>
<td>0.05, 0.30</td>
<td>GHLE ($p,T,x,y$)</td>
<td>275.2 - 285.7</td>
<td>0.581 - 0.942</td>
<td>17</td>
</tr>
</tbody>
</table>
Comparing phase equilibrium data from different sources on the same basis is generally not easy. Thus, a direct comparison of the experimental data obtained in this work with those reported in the literature was only possible under similar feed gas compositions and TBAB concentrations. The only other experimental study reporting three-phase equilibrium measurements for TBAB semi-clathrate hydrates of \((\text{CO}_2 + \text{N}_2)\) with a composition of (0.75 mole fraction of \(\text{CO}_2\)) in 0.05 mass fraction aqueous solutions of TBAB is that of Meysel et al. (2011). As shown in Figures 6.4a and 6.5, their equilibrium data are in generally good agreement with the results of the present study within experimental error over (284.1 and 286.2) K. Likewise, the agreement between the dissociation temperature measured at 0.151 mole fraction of \(\text{CO}_2\) and 0.30 mass fraction of TBAB aqueous solutions with the previously reported value by Mohammadi and coworkers (2011b) at 1.5 MPa is remarkably good (Figures 6.4b and 6.7). However, at 0.399 mole fraction of \(\text{CO}_2\) (Figures 6.4b and 6.6) the dissociation temperature resulted about 0.7 K higher than the value reported by Mohammadi et al. (2011b) at 1.7 MPa. The observed deviation can be attributed to multiple causes. For instance, calibration of measuring devices, heating rate applied during hydrate dissociation and/or the interpretation of the measured data could be some of the sources of the above difference. Nevertheless, experimental uncertainties of up to 1 K in hydrate dissociation temperatures have already been reported in the literature (Beltran & Servio, 2008).

To the best knowledge of the author, this is the first study to report the effect of 0.30 mass fraction TBAB aqueous solutions on semi-clathrates of \((\text{CO}_2 + \text{N}_2)\) at 0.749 mole fraction of \(\text{CO}_2\) in the feed gas. In consequence, no comparison of the hydrate dissociation conditions at such \(\text{CO}_2\) gaseous feed composition can be done.
Figure 6.5. Experimental dissociation conditions for semi-clathrates of (0.749 mole fraction CO\textsubscript{2} + 0.251 mole fraction N\textsubscript{2}) formed in the presence of TBAB aqueous solutions and predictions of CSMGem and HWHYD thermodynamic models in the absence of thermodynamic promoter.
Figure 6.6. Experimental dissociation conditions for semi-clathrates of (0.399 mole fraction CO$_2$ + 0.601 mole fraction N$_2$) formed in the presence of TBAB aqueous solutions and predictions of CSMGem and HWHYD thermodynamic models in the absence of thermodynamic promoter.
Figure 6.7. Experimental dissociation conditions for semi-clathrates of (0.151 mole fraction CO\textsubscript{2} + 0.849 mole fraction N\textsubscript{2}) formed in the presence of TBAB aqueous solutions and predictions of CSMGem and HWHYD thermodynamic models in the absence of thermodynamic promoter.

The predicted $p$-$T$ three-phase boundary for (CO\textsubscript{2} + N\textsubscript{2}) hydrates is also plotted in Figures 6.5 to 6.7. Based on the composition of the feed gas, the hydrate dissociation pressures (in the absence of TBAB) were predicted over the region of temperature considered using two commercial thermodynamic models: CSMGem (2008) and HWHYD (2000). The predicted values were obtained at the corresponding equilibrium temperature, CO\textsubscript{2} mole fraction in the feed gas, and water mole fraction introduced to the system. Dissociation pressures were observed to be lower for forming semi-clathrates than gas hydrates at a given temperature, and they generally decreased as the TBAB concentration increased.

Additionally, a comparison of Figures 6.5 to 6.7 shows that (under the same TBAB concentration and temperature conditions) increasing the concentration of CO\textsubscript{2} in the feed
generally decreases the pressure required for semi-clathrate formation. However, a higher molar concentration of CO$_2$ may also increase the competition between CO$_2$ and N$_2$ for cage occupancy, thus compromising CO$_2$ selectivity in the hydrate phase.

6.2.2 Compositional Properties for Semi-Clathrate Hydrates of the CO$_2$ + N$_2$ + Tetra-n-Butylammonium Bromide Aqueous Solution Systems

With the hydrate dissociation conditions for (CO$_2$ + N$_2$ + TBAB) semi-clathrates experimentally established in the previous section, the next step is to evaluate the compositions of the gas, liquid and hydrate phases under three-phase (L-H-G) equilibrium. The greatest experimental difficulties are generally encountered in the analysis of the equilibrium phases. In this work, compositional analyses for the gas and liquid phases have been carried out and are discussed herein. Gas chromatography and refractive index were used for this purpose. Measuring the compositional change in the hydrate phase remains a challenging task and it is not addressed in this study, as it requires other experimental techniques that are far beyond the scope of this research, namely X-ray diffraction, Raman or Nuclear magnetic resonance spectroscopy.

Three different molar concentrations of CO$_2$ (0.151, 0.399 and 0.749) in the feed gas are studied to cover a large range of potential applications, as mentioned earlier. The effect of TBAB aqueous solutions with mass fractions of (0.05 and 0.30) was also investigated in this work. The purities and chemicals used are similar to those reported in section 6.2. The equilibrium data were measured in the (275 to 289) K and (0.58 to 19.09) MPa ranges. The density data and correlation reported in the Appendix B were used to determine the density of TBAB aqueous solutions loaded into the system and their number of moles.

A summary of the experimental conditions where compositional measurements were carried out is given in Table 6.6. All compositional equilibrium data are reported in Tables A.11 and A.12 (Appendix A). It should be noted that the compositions of the gas phase are reported in water and TBAB free basis. The molar concentration of CO$_2$ resulted lower at the final (gas-hydrate-liquid) equilibrium state when compared to the loading. Thus, CO$_2$ is preferentially trapped into the hydrate lattice and a high selectivity of CO$_2$ in the hydrate phase is expected.
The experimental determination of compositional data of the gas phase for the (CO$_2$ + N$_2$ + TBAB + water) systems carried out in this work was restricted to (L-H-G) equilibrium. However, by examining the $T$-$w$ phase diagram for (TBAB + water) systems at atmospheric pressure (Figure 1.12), the equilibrium data measured below 277.15 K and 285.15 K for 0.05 and 0.30 TBAB mass fractions, respectively, most likely represent equilibrium conditions for (TBAB + H$_2$O) semi-clathrates (without gas).

To verify the effect of temperature on the molar concentration of CO$_2$ in the gas phase, the hydrate dissociation process was studied at selected isothermal conditions. A pressure-composition phase diagram for the (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems measured at various temperatures and 0.05 mass fractions TBAB is shown in Figure 6.8. It is clear from this figure that under similar pressure conditions, the concentration of CO$_2$ in the gas phase increases as the equilibrium temperature increases. Therefore, most likely less amount of CO$_2$ is trapped in the hydrate phase at high temperatures. Also, a lower CO$_2$ gas phase composition is observed at higher pressures, for a given temperature. For example, by adding 0.05 mass fraction TBAB aqueous solutions, the molar concentration of CO$_2$ in the gas phase at 282.2 K changed from 0.114 to 0.623, while the equilibrium pressure decreases from 18.12 to 0.9 MPa, as indicated in Table A.11. Similar behavior is observed at all studied temperatures.

The effect of 0.30 mass fraction TBAB aqueous mixtures on the equilibrium pressures and gas phase compositions of (CO$_2$ + N$_2$ + TBAB + H$_2$O) semi-clathrates is shown in Figure 6.9. The tendencies in the molar concentrations of CO$_2$ in the gas phase with respect to pressure or temperature are comparable to those observed in Figure 6.8 for 0.05 mass fractions TBAB. However, larger pressure reductions are observed for a given temperature in the presence of 0.30 mass fraction TBAB aqueous solutions. This effect can be better distinguished at the two selected temperatures presented in Figure 6.10. For instance, at temperatures ~ 285.2 K a pressure reduction of at least four times is observed for systems with initial TBAB mass fractions of 0.30 compared to systems where initial TBAB mass fractions are 0.05. Such pressure reduction effect is intensified at temperatures ~ 287.2 K. On the other hand, similar equilibrium pressures (~ 0.90 MPa) are only observed at lower temperatures (~ 282.2 K) for systems in 0.05 mass fractions TBAB, while by adding 0.30 mass fractions TBAB such pressures are achieved at
higher temperatures (~ 285.7 K). Therefore, the initial concentration of TBAB in aqueous solutions has a substantial effect on the thermodynamic stability of studied semi-clathrates systems and most likely results in different crystalline structures. Furthermore, the equilibrium data suggest that (CO$_2$ + N$_2$) gas mixtures can be stabilized in the form of semi-clathrates at low pressures by adding TBAB.

In addition to the gas phase compositional measurements, the compositional change of TBAB in the liquid phase was measured through refractometry technique under three-phase equilibrium conditions. A needle valve (identified as V$_3$ in Figure 4.1) was used to withdraw ~ 0.05 ml liquid samples, which were then analyzed by refractive index technique, as suggested by Duc and coworkers (2007), to determine the concentration of TBAB in the liquid phase. It is assumed that TBAB does not have a significant effect on the solubility of CO$_2$ and N$_2$ in the liquid phase (Duc et al., 2007). Thus, gases possibly dissolved in the liquid do not affect the refractive index measurements (Assane, 2008). Again, the measured data are given in Tables A.11 and A.12. Only few points are reported in Table A.12 for the experiments with a loading concentration of 0.30 mass fractions TBAB. In fact, such a high concentration of TBAB increases the volumetric fraction of hydrate formed, which in turn blocks the sampling line and in most cases it makes impossible to sample the liquid phase. Similar technical difficulties have been previously reported in the doctoral dissertation of Assane (2008). A representative pressure - liquid composition phase diagram is shown in Figure 6.11 for initial TBAB mass fractions of 0.05. As expected, the reduction of the concentration of TBAB in the liquid phase with pressure (at a given temperature) suggests that more TBAB incorporates in the crystalline structure as pressure increases. It should also be noted that under similar pressure conditions (e.g. at ~ 6, ~14 and ~18 MPa), the concentration of TBAB in the liquid phase increases with temperature. This possibly suggests less occupancy of TBAB in the hydrate structure at higher temperatures. However, no conclusions can be drawn in this respect from the present study. Indeed, such hypothesis requires further investigation through suitable crystallographic techniques.

For practical purposes, an isothermal operation is considered during the hydrate formation process and mass fractions of TBAB in the liquid phase are shown at three selected temperatures. It can be noticed that the equilibrium pressure increases as the concentration of TBAB in the
liquid phase decreases at a given temperature. Such behavior is consistent with the fact that mixed (CO$_2$ + N$_2$) hydrates form at higher pressures without TBAB. On the other hand, at constant TBAB concentration, an increase in the equilibrium pressure is evidenced as temperature rises.

Based on the above results, a conceptual three-stage hydrate separation process for capturing CO$_2$ from industrial/flue gases is proposed. The most favorable operating conditions (feeds, temperatures and pressures for two different concentrations of TBAB aqueous solution) of the three stages are given in Table 6.7. The three (CO$_2$ + N$_2$) gas mixtures studied, with CO$_2$ mole fractions of (0.151, 0.399 and 0.749) were used as the feed gases in the first, second and third separation stages, respectively. Two sets of operating conditions are provided at constant temperature and two concentrations of TBAB in the aqueous solution. Thus, a highly concentrated (> 75 mole %) CO$_2$ stream can be obtained from a typical flue gas mixture of (15.1 mole % CO$_2$/N$_2$), under moderate temperature and pressures in the presence of TBAB.

The experimental results presented in this chapter provide a better understanding of the phase behavior of simple and mixed TBAB semi-clathrates of carbon dioxide, methane or nitrogen and (carbon dioxide + nitrogen). Therefore, a better assessment of CO$_2$ hydrate-based technologies with TBAB as thermodynamic promoter can be obtained from practical point of view. Finally, it should be pointed out that modeling the hydrate phase equilibria for the systems studied here is still a challenge. To the best of our knowledge no predictive (thermodynamic or mathematical) model has ever been developed for semi-clathrates formed from gas mixtures + TBAB aqueous solutions. Only two predictive approaches have been reported in the literature for (gas) semi-clathrate systems: 1) A modeling tool based on an artificial neural network (ANN) algorithm proposed by Mohammadi et al. (2010) for hydrogen + TBAB semiclathrate hydrates and 2) A thermodynamic model proposed by Paricaud (2011) which combines the van der Waals-Platteeuw theory and the SAFT-VRE equation of state to determine the dissociation conditions of carbon dioxide + TBAB + H$_2$O systems. Hence, further investigation in this subject is required. Substantial savings in experimental effort could be indeed achieved with the development of accurate thermodynamic models capable of predicting the phase behavior of semi-clathrate hydrates.
Table 6.7. Conceptual three-stage CO$_2$ hydrate-based separation process from (CO$_2$ + N$_2$) gas mixtures using two different concentrations of TBAB in aqueous solutions.

<table>
<thead>
<tr>
<th>TBAB / mass fraction</th>
<th>0.05</th>
<th>0.30</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Temperature / K</strong></td>
<td>282.6</td>
<td>285.7</td>
</tr>
<tr>
<td>Feed gas molar composition / fraction</td>
<td>Stage</td>
<td>$p$ / MPa</td>
</tr>
<tr>
<td>CO$_2$ (0.151) + N$_2$ (0.849 mole)</td>
<td>1</td>
<td>3.157</td>
</tr>
<tr>
<td>CO$_2$ (0.399) + N$_2$ (0.601 mole)</td>
<td>2</td>
<td>2.782</td>
</tr>
<tr>
<td>CO$_2$ (0.749) + N$_2$ (0.251 mole)</td>
<td>3</td>
<td>1.471</td>
</tr>
</tbody>
</table>
Figure 6.8. Pressure-composition (gas phase) diagram for semi-clathrates of the (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems at various temperatures and 0.05 mass fraction TBAB.
Figure 6.9. Pressure-composition (gas phase) diagram for semi-clathrates of the (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems at various temperatures and 0.30 mass fraction TBAB.
Figure 6.10. Pressure-composition (gas phase) diagram for semi-clathrates of the \((\text{CO}_2 + \text{N}_2 + \text{TBAB} + \text{H}_2\text{O})\) systems at selected temperatures and different initial TBAB concentrations.
Figure 6.11. Pressure - composition (TBAB in the liquid phase) diagram for semi-clathrates of (CO$_2$ + N$_2$ + TBAB + H$_2$O) systems at various temperatures. TBAB mass fraction loaded = 0.05.
7 Conclusions et Perspectives

Le but de ce chapitre est de fournir les conclusions majeures concernant les travaux de recherche effectués dans cette thèse. La nécessité de données fiables d’équilibres de phases, sur des systèmes avec formation d’hydrate de CO₂ pertinentes dans le cadre des systèmes de technologies de captage-stockage géologique de CO₂ (CSC) a été le moteur principal de la thèse. Cette dernière a porté principalement sur des mesures expérimentales (équilibres à trois phases) sur des systèmes formateurs d’hydrates: CO₂, CH₄, N₂ et H₂ en présence d’eau pure et de solutions aqueuses de TBAB. Un nouvel appareil basé sur la technique ‘statique-analytique’ avec échantillonnage par capillaire (ROLSI™) de la phase gazeuse, a été développé avec le soutien de la chromatographie en phase gazeuse pour les analyses. Les résultats de l’interprétation thermodynamique des données expérimentales sont décrits. Les résultats des comparaisons avec les données de la littérature et avec les prédictions à partir de deux modèles thermodynamiques sont mis en évidence. L’effet de promotion thermodynamique dû au TBAB dans les équilibres de phases des gaz purs et des mélanges de gaz est souligné. Enfin, nous faisons des recommandations pour de futures recherches.

7 Conclusions and Outlook

The aim of this chapter is to provide the major conclusions from the research work carried out in this thesis. The need of reliable phase equilibrium data in CO₂ hydrate-forming systems relevant to CCS technologies was the main driver of the thesis. The thesis focused primarily on experimental measurements in the (CO₂, CH₄, N₂ and H₂) hydrate-forming systems in the presence of pure water and TBAB aqueous solutions under three-phase equilibrium. A new apparatus based on the ‘static-analytic’ technique and capillary gas phase sampling, with support from gas chromatography was developed for this purpose. Results from the thermodynamic interpretation of the experimental data are outlined. The outcome of comparisons with literature data and the predictions of two thermodynamic models are highlighted. The thermodynamic promotion effect of TBAB in the phase equilibria of pure gases and a gas mixture is emphasized. Directions for recommended future research are suggested.
7.1 Conclusions

La thermodynamique expérimentale joue un rôle important dans le cadre de la conception de technologies économiques, plus sûres, et durables. Dans cette thèse, une enquête approfondie concernant les travaux expérimentaux relatifs aux mélanges de gaz avec formation d'hydrate de CO$_2$ a été réalisée dans le cadre d'une approche alternative de capture du CO$_2$ par formation d'hydrates de gaz.

La compréhension des équilibres de phases avec hydrates requière d’une part un aperçu historique et d’autre part le contexte théorique tous deux présentés de façon concise au chapitre 1. Une description des structures les plus courantes des cristaux d'hydrates et de leurs implications microscopiques dans le comportement de phase des systèmes formateurs d'hydrates fournir la base pour l'étude des diagrammes de phases de ces systèmes. Le rôle des promoteurs thermodynamiques dans l'amélioration des conditions opératoires des procédés industriels potentiels de séparation à base d’hydrates est important en raison de la nécessité de réduire la pression requise pour la formation des hydrates par rapport aux systèmes aqueux en absence de promoteur. L'additif choisi pour cette étude, le TBAB, appartient à la famille des promoteurs thermodynamiques solubles dans l'eau et forme un clathrate particulier nommé «semi-clathrate».

Dans le deuxième chapitre, les techniques expérimentales disponibles pour les études à haute pression des équilibres de phases sont discutées en référence à des exemples actuels de la littérature. Le choix de la procédure expérimentale adoptée, à savoir: ‘isochoric-pressure search method’, se justifie en termes d'exactitude et de fiabilité de la méthode. Comme les données d'équilibres de phases en présence d'hydrates sont souhaitées avec la précision la plus élevée possible, et ce, à des fins de modélisation et d'ingénierie, les étalonnages de tous les outils de mesure ont été effectués soigneusement. En conséquence, les incertitudes expérimentales maximales estimées sont inférieures à ± 0.02 K et ± 0.002 MPa, pour la température et la pression, respectivement; ± 1-2 % pour les fractions molaires en phase gazeuse; ± 0.1 % pour les mesures des indices de réfraction; ± 0.5 cm$^3$ pour les volumes de liquide transférés dans la cellule d'équilibre. En outre, l'incertitude globale maximale pour les mesures de dissociation d'hydrates devrait se situer à ± 0.05 MPa et ± 0.2 K, comme résultante des déterminations graphiques à partir des courbes isochores.
Le cœur du travail expérimental réalisé dans cette thèse est discuté dans les chapitres 3 à 6. La résolution des difficultés techniques et expérimentales doit être inévitablement prise en compte en vue de la mesure précise des équilibres de phases. Les mesures préliminaires des équilibres de phases réalisées en présence d’hydrates (pour le mélange gazeux "CO$_2$ + CH$_4$") ont été présentées au chapitre 3. Dans cette étude, les mélanges de gaz "CO$_2$ + CH$_4$" (différentes compositions) ont été étudiés entre 279 et 290 K pour des pressions jusqu'à 13 MPa, en utilisant un appareil existant basé sur la méthode 'statique-analytique'. Les mélanges de gaz ont été préparés directement dans la cellule d'équilibre et la composition de la charge gazeuse a été déterminée par chromatographie en phase gazeuse. La procédure expérimentale liée à la méthode dite: “isochoric-pressure search method” a été suivie pour mesurer les conditions de dissociation des hydrates. Les données expérimentales ainsi que les données de la littérature ont été comparées aux prédictions du modèle thermodynamique HWHYD. De grandes déviations sur les pressions de dissociation (jusqu'à ~ 400%) ont été observées. Sur la base des données d'équilibre, il a été suggéré que la structure stable relative aux hydrates de gaz (dioxyde de carbone + méthane) est la structure I (AARD: 13.7%). En outre, les comparaisons de nos valeurs expérimentales de dissociation et des données de la littérature avec les prédictions d'une équation proposée par Adisasmito et al. (1991) montrent un accord plus cohérent (AARD: 7.9%).

Les expérimentations et les innovations continues pour améliorer à la fois l'appareil et les procédures expérimentales avec pour but d'accroître la précision des résultats, ont été la base du développement réussi d’un nouvel appareil. Ce dernier reposant sur la méthode ‘statique-analytique’ a ainsi été développé avec succès au cours de la thèse pour la mesure d'équilibres de phases avec hydrates. Le nouvel appareil et le contour des procédures d'exploitation sont le résultat de raffinements successifs tout au long de l'expérimentation conséquente. L’explication de la mesure simultanée, avec cet appareil, des conditions de dissociation des hydrates et des compositions de la phase gazeuse en équilibre avec les phases hydrate et liquide a été largement couverte dans les chapitres 4 et 5. La fiabilité de l’appareil et des procédures expérimentales est démontrée au travers de nouvelles mesures de dissociation d'hydrates effectuées sur le système: (CO$_2$ + CH$_4$ + H$_2$O) entre 278 et 286 K et entre 2.72 et 6.09 MPa. La comparaison entre les données expérimentales générées au cours de cette étude et les données de la littérature correspondantes montre une cohérence satisfaisante dans toutes les conditions étudiées. Les données d'équilibre $p, T, y$ entre 274 et 284 K, jusqu'à environ 7 MPa, permettent de déterminer...
les compositions en phase liquide et en phase hydrate en utilisant une approche par bilans de matière. La composition du CO$_2$ dans les phases gaz et hydrate diminue généralement alors que la pression augmente. Une concentration maximale de CO$_2$ égal à 0.88 en fraction molaire a été observée dans la phase hydrate à (~ 276 K et 1.99 MPa). L'augmentation de la température conduit généralement à une diminution de la quantité de CO$_2$ piégé en phase hydrate. Les données d'équilibre mesurées dans ce travail ont été comparées aux prédictions de deux modèles thermodynamiques, à savoir CSMGem (basé sur la minimisation de l'énergie Gibbs) et HWHYD (basé sur l'égalité de la fugacité de chaque composant dans toutes les phases). Les conditions de dissociation d'hydrates prédites présentent des écarts relatifs absolus moyens (AARD) d'environ 10 et 5 %, pour HWHYD et le modèle CSMGem, respectivement. Concernant les données d'équilibre $p$, $T$, $y$, $z$, le modèle HWHYD n’a pas du tout convergé aux conditions expérimentales étudiées. Les compositions de CO$_2$ prédites grâce au modèle CSMGem aboutissent à des accords moyens pour la phase hydrate. De meilleurs accords ont été obtenus pour la composition en CO$_2$ de la phase gazeuse en équilibre avec les phases hydrate et liquide.

Le chapitre 5 présente les équilibres de phases avec hydrate des systèmes: (CO$_2$ + N$_2$ + H$_2$O) et (CO$_2$ + H$_2$ + H$_2$O). Les mesures d'équilibre ont été effectuées à l'aide de l'appareil, et de procédures expérimentales similaires, comme décrit dans le chapitre 4. Des teneurs moyennes à hautes en CO$_2$ dans les mélanges ont été étudiées sur une large gamme de conditions expérimentales: $p$ et $T$. Le comportement de phases de (CO$_2$ + N$_2$ + H$_2$O) a été d'abord étudié entre 274 et 282 K jusqu'à ~ 17.63 MPa. Les fractions molaires de CO$_2$ dans le gaz d'alimentation variant entre 0.271 et 0.812 ont été mesurées par chromatographie en phase gazeuse. Il a été conclu que la structure d'hydrate stable dans le cadre du mélange (CO$_2$ + N$_2$) aux conditions étudiées dans ce travail est la structure I. La pression de dissociation dépend de la composition de la charge (gaz d'alimentation) et est une fonction inverse de fraction molaire de CO$_2$ dans la charge. La fiabilité des modèles thermodynamiques CSMGem et HWHYD a été discutée pour les hydrates de gaz étudiés (CO$_2$ + N$_2$). Les valeurs des AARD sur les pressions de dissociation des hydrates prédites par les modèles thermodynamiques CSMGem et HWHYD sont respectivement de 3.4 et 10 %. Les données de composition mesurées dans les gammes: 279 à 285 K et 3.24 à 29.92 MPa, ont été comparées aux données de la littérature avec un accord acceptable. Les données de dissociation générées ici et les données expérimentales disponibles dans la littérature pour les mélanges de gaz (CO$_2$ + N$_2$) ont été comparées aux prédictions de
deux modèles thermodynamiques de la littérature. En général, les comparaisons entre pressions de dissociation expérimentales d'hydrates (ce travail) et celles prédites pour le mélange \((\text{CO}_2 + \text{N}_2)\) et pour le mélange \((\text{CO}_2 + \text{CH}_4)\) suggèrent la nécessité de reconsidérer les modèles thermodynamiques actuels lorsque l’on s’intéresse à des mélanges binaires contenant du CO\(_2\). La révision des paramètres du modèle en utilisant à la fois des données de dissociation d'hydrates fiables et des données de composition des phases à l'équilibre avec l'hydrate de gaz est nécessaire pour les systèmes avechydrate de CO\(_2\). Cela est surtout nécessaire parce que ces modèles ont été historiquement développés pour les mélanges d'hydrocarbures.

La deuxième partie du chapitre 5, présente les mesures d'équilibres de phases des systèmes \((\text{CO}_2 + \text{H}_2 + \text{H}_2\text{O})\). Les compositions molaires de CO\(_2\) (et H\(_2\)) dans la phase gazeuse en équilibre avec de l'hydrate de gaz et les phases aqueuses mesurées pour différents mélanges de gaz \((\text{CO}_2 + \text{H}_2)\) + eau ont été étudiées entre 274 et 281 K jusqu’à environ 9 MPa. Les données expérimentales obtenues dans cette étude ont été comparées de manière satisfaisante aux données disponibles dans la littérature. A partir d’une étude bibliographique on a supposé que H\(_2\) n’est pas piégé dans les cavités d'hydrates aux conditions étudiées.

Dans les chapitres 3 à 5, les conditions de dissociation d'hydrates relatives à des mélanges de gaz contenant du CO\(_2\) en présence d'eau ont été établies expérimentalement à des températures basses et des pressions relativement élevées. Dans le but d'examiner l'effet promoteur d'hydrate par le TBAB, la stabilité thermodynamique de semi-clathrates formés à partir de CO\(_2\), CH\(_4\), N\(_2\) et \((\text{CO}_2 + \text{N}_2)\) dans mélanges aqueux de TBAB est étudiée au chapitre 6. Tout d’abord, la stabilité thermodynamique de semi-clathrates de \((\text{CO}_2, \text{CH}_4 \text{ ou } \text{N}_2 + \text{TBAB})\) a été examinée pour des fractions massiques de TBAB en solution aqueuse allant de 0.25 à 0.50, dans des plages de températures de \((283 \text{ à } 288), (286 \text{ à } 293), \text{ et } (286 \text{ à } 289)\) K, respectivement. L'effet promoteur le plus important est observé pour les systèmes avec azote, où l’on constate des réductions substantielles des pressions de dissociation d'hydrates de l’ordre de 90 %. Des accords satisfaisants avec les données de la littérature sont observés dans tous les domaines de comparaisons possibles. Dans la deuxième partie du chapitre 6, nous présentons les résultats des mesures de dissociation et de compositions pour les systèmes: \((\text{CO}_2 + \text{N}_2 + \text{TBAB} + \text{H}_2\text{O})\), avec des charges (gaz d’alimentation) de diverses compositions en CO\(_2\), effectuées expérimentalement de 275 à 291 K et de 0.58 à 19.09 MPa, en utilisant les méthodes décrites dans le chapitre 4. Les
semi-clathrates sont formés avec l'addition de solutions aqueuses de TBAB (fractions massiques de TBAB: 0.05 et 0.30). Les fractions molaires de CO₂ dans le gaz d'alimentation sont: 0.151, 0.399, et 0.749). Les températures et pressions d'opération d'un procédé de séparation du CO₂ par voie d'hydrates ont été établies sur la base des conditions expérimentales de dissociation et de compositions de mélanges de gaz. Un effet de promotion significatif est observé pour la formation des semi-clathrates, avec TBAB comme additif thermodynamique, et ce, par rapport à la formation des hydrates de gaz à la même température. Comme prévu, les pressions de dissociation diminuent généralement quand la concentration en TBAB de la solution aqueuse augmente. Dans les mêmes conditions de concentration en TBAB et de température, il a été mis en évidence que l'augmentation de la concentration en azote dans le gaz d'alimentation conduit à l'augmentation de la pression nécessaire à la formation des semi-clathrates. La comparaison avec les données de la littérature montre un accord cohérent sur tous les domaines de température et de pression. Le changement compositionnel dans les phases gazeuse et liquide, à différentes températures dans le cadre d'équilibres à trois phases, a été mesuré respectivement par chromatographie en phase gazeuse et par réfractométrie. L'effet de promotion thermodynamique dû au TBAB en solutions aqueuses a été établi en termes de pressions et de températures de dissociation. Les conditions d'exploitation les plus favorables pour un procédé de séparation du CO₂ par des hydrates ont été proposées. Le plus fort degré de promotion thermodynamique a été observé pour le mélange de gaz (CO₂ + N₂) à 0.749 molaire en CO₂, où une réduction de la pression de l'ordre de 60 % a été atteinte à 282.6 et 285.7 K, par rapport à des systèmes sans additif.

Les résultats expérimentaux permettent de montrer que le CO₂ peut être séparé des gaz industriels / de combustion qu'il soit à très faibles ou très hautes concentrations, et ce, à des conditions d'exploitation raisonnables, en présence de solutions aqueuses de TBAB. Les analyses thermodynamiques présentées dans les chapitres 3 à 6 fournissent des informations précieuses sur le comportement de phase des hydrates mixtes de dioxyde de carbone dans une gamme utile de températures et de pressions. Les données d'équilibre fournies dans la présente étude sont fondamentales pour le développement futur de modèles thermodynamiques et la conception de nouvelles technologies impliquant des hydrates de gaz de dioxyde de carbone. D'autres domaines d'amélioration et quelques indications pour des recherches futures sont suggérés dans la section suivante.
7.2 Perspectives

Bien que des résultats intéressants aient été exposés tout au long de ce travail, des recherches complémentaires sont encore nécessaires pour acquérir une meilleure compréhension de la complexité structurelle et thermodynamique des systèmes avec formation d'hydrates et semi-clathrates en présence de CO$_2$.

Il est clair, à l'examen de la littérature, que la quantité de données d'équilibres de phases disponibles pour les mélanges de gaz, contenant du CO$_2$, en solution dans des solutions aqueuses de TBAB est encore insuffisante. Les mesures des conditions de dissociation de l'hydrate de CO$_2$ pour d'autres mélanges de gaz, tels que (CO$_2$ + CH$_4$) et (CO$_2$ + H$_2$) en solutions aqueuses de TBAB seraient particulièrement utiles pour établir la zone de stabilité thermodynamique et estimer le degré de promotion du TBAB dans de tels systèmes, et également pertinentes pour les technologies de CSC ainsi que pour l'industrie du pétrole. De nouvelles études sur le comportement de phases sont nécessaires pour les mélanges binaires de gaz riches en hydrogène afin de mieux évaluer la forte dépendance des pressions de dissociation avec les concentrations molaires en H$_2$. D'autre part, l'effet des impuretés (par exemple: CO, O$_2$, NO, etc.), qui se trouvent généralement dans les gaz d'échappement industriels / de combustion au côté de CO$_2$, N$_2$, CH$_4$ et H$_2$, sur les équilibres de phase de systèmes avec formation d'hydrate de CO$_2$ a été peu étudié. Cela pourrait être, du point de vue pratique, un formidable champ d'intérêt de la recherche.

Comme il a été souligné à maintes reprises, la caractérisation directe de la phase hydrate est fortement encouragée et nécessaire afin de fournir des interprétations plus concluantes des observations thermodynamiques. Ceci peut être réalisé à l'aide de techniques physiques non intrusives appropriées (par exemple, RMN, rayons X, ou spectroscopie Raman). La connaissance des structures stables des hydrates, des occupations de cages et d'éventuelles transitions structurelles est nécessaire pour mieux comprendre le comportement de phases des hydrates mixtes et semi-clathrates de TBAB.

Dans cette thèse, il a été argumenté sur le fait que les paramètres du modèle thermodynamique doivent être réajustés sur des données d'équilibre fiables de systèmes formant des hydrates de CO$_2$, car les modèles existants ont généralement été développés uniquement pour des mélanges...
d'hydrocarbures. Seulement deux approches thermodynamiques prédictives (Mohammadi *et al.*, 2010 et Paricaud, 2011) ont été proposées, à ce jour, pour les semi-clathrates de (H₂ + TBAB) et (CO₂ + TBAB), respectivement. En conséquence, le développement de nouvelles approches thermodynamiques prédictives spécialement adaptées aux semi-clathrates est fortement encouragé, d’autant plus qu’un comportement structurel complexe (possibles transitions de structure) a été évoqué, comme hypothèse, à partir des équilibres de phases mesurés dans ce travail. Des économies substantielles sur les efforts expérimentaux sont attendues avec le développement de modèles thermodynamiques précis capables de prédire le comportement de phases des semi-clathrates hydrates.

Li *et al.* (2010) ont mené une étude comparative sur l'effet promoteur de divers sels d'ammonium quaternaire (par exemple TBAF, TBAB et TBAC) sur les équilibres de phases impliquant le CO₂. La recherche de Chapoy *et al.* (2007) a montré une capacité de stockage accrue de l'hydrogène dans les semi-clathrates de TBAB d'un ordre de grandeur (à 1 MPa), par rapport aux clathrates (H₂ + THF). En outre, Deschamps et Dalmazzone (2010) ont écrit qu'environ deux fois plus d'hydrogène peut être stocké dans les systèmes (H₂ + TBAC) et (H₂ + bromure de tétrabutylphosphonium) par rapport aux semi-clathrates (H₂ + TBAB). Sur la base de ces études, des travaux complémentaires concernant l'effet des sels de tétra alkyl ammonium sur les équilibres de phases des mélanges gazeux: (H₂ + CO₂), seraient certainement très utiles pour les applications en séparation et stockage.

Une procédure expérimentale alternative aux mesures fastidieuses des équilibres de phase en présence d'hydrates par la méthode dite: ‘isochoric pressure-search method’ a été récemment étudiée à CEP-TEP. Une étude préliminaire a été effectuée pour les hydrates de CO₂ pur à l’aide d’une cellule à volume variable en titane (Fontalba *et al.*, 1984), et a montré des résultats prometteurs (D. Richon, communication personnelle, 9 Mars, 2012). En effet, l’équilibre thermodynamique est atteint en quelques minutes et la pression de dissociation des hydrates est identifiée par la présence d'un plateau sur la courbe représentant la pression en fonction du volume accessible au mélange étudié. La composition de la phase hydrate peut être déterminée à partir des données PVT et de la détermination de la quantité de gaz émis lors de la dissociation des hydrates (à partir de la largeur du plateau). Cette méthode mériterait d’être approfondie.
Bien que l’appareil développé dans cette thèse fonctionne de manière satisfaisante, certaines améliorations sont recommandées pour les futurs montages expérimentaux destinés aux mesures d'équilibre de phases avec hydrates de gaz: un mélangeage plus efficace, la suppression des volumes morts dans les accessoires et dispositifs de mélange et une bonne caractérisation des compositions des phases liquide et hydrate au travers d'échantillonnages in situ. Enfin, la réalisation de mesures d'équilibres de phases à haute pression et avec des composés toxiques est potentiellement dangereuse. Ainsi, le souci de la sécurité doit être la priorité de tous les instants que ce soit au niveau de la conception des appareillages, de la conduite des manipulations et lors des opérations de routine.

7.1 Conclusions

Experimental thermodynamics play an important role in the design of economical, safer and sustainable technologies. In this thesis a comprehensive experimental investigation for CO₂ hydrate-forming gas mixtures has been carried out in the context of an alternative CO₂ capture approach, through gas hydrate formation.

The understanding of hydrate phase equilibrium implies a historical overview and theoretical background concisely presented in Chapter 1. An insight of the most common hydrate crystal structures and their microscopic implications in the phase behavior of hydrate forming systems provided the basis for studying the phase diagrams in gas hydrates forming systems. The role of thermodynamic promoters in enhancing the operating conditions of potential industrial gas hydrates-based processes was supported with the need of reducing the required pressure for hydrate formation compared to systems in the absence of promoter. The additive chosen for this investigation, TBAB, belongs to the water-soluble family of thermodynamic promoters and forms a different clathrate compound labeled ‘semi-clathrate’.

In the second chapter, the experimental techniques available for high-pressure phase equilibrium studies are discussed with reference to current examples from the literature. The choice of the experimental procedure adopted, namely ‘isochoric-pressure search method’, is justified in terms of the accuracy and reliability of the method. As hydrate phase equilibrium data with the highest possible accuracy are needed for modeling and engineering purposes, calibrations of all
measuring devices were carefully performed. Accordingly, maximum expected experimental uncertainties are within ± 0.02 K and ± 0.002 MPa, for temperature and pressure equilibrium measurements, respectively; ± 0.5 cm³ for liquids supplied to the equilibrium cell; ± 1-2% for molar gas phase compositions and ± 0.1% for refractive indices measurements. In addition, the maximum overall uncertainty for hydrate dissociation measurements is expected to be within ± 0.05 MPa and ± 0.2 K, derived from isochoric curves.

The core of the experimental work carried out in this thesis is discussed in Chapters 3 to 6. The resolution of technical and experimental difficulties must be unavoidably taken into account in the measurement of accurate hydrate phase equilibrium data. Preliminary phase equilibrium measurements carried out for clathrate hydrates of (CO₂ + CH₄) mixtures were presented in Chapter 3. In this study, gas mixtures with different CO₂/CH₄ ratios were investigated in the temperature ranges from (279 to 290) K and pressures up to 13 MPa, using an existent ‘static-analytic’ apparatus. The gas mixtures were prepared directly in the equilibrium cell and the composition of the feed was determined through gas chromatography. An isochoric pressure-search method was followed to measure the hydrate dissociation conditions. The experimental data along with the literature data were compared with the predictions of HWHYD thermodynamic model. Large deviations on the dissociation pressures (up to ~ 400%) were observed. Based on the equilibrium data, it was suggested that the stable hydrate structure for the (carbon dioxide + methane) gas hydrates is likely structure I (AARD: 13.7%). In addition, comparisons between dissociation experimental and literature data with the predictions of an equation proposed by Adisasmito et al. (1991) resulted more consistent (AARD: 7.9%).

As a result of continuous experimentation and innovation to improve both the apparatus and experimental procedures and with the aim of increasing the accuracy of the results, a new ‘static-analytic’ apparatus for hydrate phase equilibrium measurements was successfully developed within this thesis. The new apparatus and the outline of operating procedures are the outcome of successive refinement throughout substantial experimentation. Simultaneous measurement of hydrate dissociation conditions and compositions of the gas phase in equilibrium with the hydrate and liquid phases using this new apparatus were extensively covered in Chapters 4 and 5. The reliability of the apparatus and experimental procedures is demonstrated through new hydrate dissociation measurements carried out for (CO₂ + CH₄ + H₂O) systems in the (278 to
Comparison between the experimental data generated in this study and the corresponding literature data show satisfactory consistency throughout the investigated conditions. The measured $p$, $T$, $y$ equilibrium data in the (274 to 284) K and up to ~7 MPa, enabled the determination of liquid and hydrate phase compositions using a material balance approach. Composition of CO$_2$ in the gas and hydrate phases generally decreased as pressure increased. A maximum concentration of 0.88 mole fraction of CO$_2$ in the hydrate phase was observed at (~ 276 K and 1.99 MPa). Increasing the temperature generally leads to less CO$_2$ being trapped in the hydrate phase. The equilibrium data measured in this work were compared with the predictions of two thermodynamic models, namely CSMGem (based on the Gibbs energy minimization) and HWHYD (based on the equality of fugacity of each component throughout all phases). Predicted hydrate dissociation conditions showed average absolute relative deviations (AARD) of about 10 % and 5 %, for HWHYD and CSMGem models respectively. As for the $p$, $T$, $y$, $z$ equilibrium data, the HWHYD model did not converge at all at the studied experimental conditions. The predicted CO$_2$ compositions through CSMGem model resulted in poor agreements for the hydrate phase. Better agreements were obtained for the composition of CO$_2$ in the gas phase in equilibrium with hydrate and liquid phases.

Chapter 5 presents the hydrate phase equilibria of (CO$_2$ + N$_2$ + H$_2$O) and (CO$_2$ + H$_2$ + H$_2$O) systems. The equilibrium measurements were carried out using the apparatus described in Chapter 4 and following similar experimental procedures. Medium to high content CO$_2$ gas mixtures were investigated over a wide range of experimental conditions. The phase behavior of (CO$_2$ + N$_2$ + H$_2$O) systems was first investigated in the (274 to 282) K temperature range and pressures up to ~17.63 MPa. The relative molar ratios of CO$_2$ and N$_2$ in the feed gas varying between from (0.271 to 0.812) were measured by gas chromatography. It was suggested that the stable hydrate structure for the (CO$_2$ + N$_2$) clathrate hydrates at the conditions studied in this work is likely structure I. The equilibrium dissociation pressures were found to be dependent of the composition of the feed and were shifted to lower values as the mole fraction of CO$_2$ increased in the feed. The reliability of CSMGem and HWHYD thermodynamic models was investigated for the studied (CO$_2$ + N$_2$) gas hydrates. AARD of the predicted hydrate dissociation pressures by HWHYD and CSMGem thermodynamic models are 3.4 % and 10 %, respectively. The measured compositional data, in the (279 to 285) K and (3.24 to 29.92) MPa ranges, were compared with the literature data and a generally consistent agreement is found. The dissociation
data generated along with the experimental data reported in the literature for (CO₂ + N₂) gas mixtures were compared with the predictions of two thermodynamic literature models. In general, comparisons between experimental and predicted hydrate dissociation pressures carried out in this work for the latter system and for (CO₂ + CH₄) gas mixtures suggest a need for reconsidering current thermodynamic models for binary mixtures containing CO₂. Readjustment of model parameters using reliable both hydrate dissociation and compositional data of the existing phases in equilibrium with gas hydrate is necessary for CO₂ hydrate-forming systems. Especially, since such models have traditionally been developed for hydrocarbon systems.

The second part of Chapter 5, presents the phase equilibrium measurements carried out for (CO₂ + H₂ + H₂O) systems. The molar compositions of CO₂ (and H₂) in the gas phase in equilibrium with gas hydrate and aqueous phases measured for various (CO₂ + H₂) gas mixtures + water systems were investigated in the temperature range of (274 to 281) K at pressures up to ∼ 9 MPa. The experimental data generated in this study were compared with the data reported in the literature and acceptable agreement is generally observed. It was assumed that H₂ was not trapped in the hydrate cavities in the studied conditions, based on literature investigations.

In Chapters 3 through 5, hydrate dissociation conditions for gas mixtures containing CO₂ in the presence of water were experimentally established at low temperatures and relatively high pressures. With the aim of examining the hydrate promotion effect of TBAB, the thermodynamic stability of semi-clathrates formed from CO₂, CH₄, N₂ and (CO₂ + N₂) in TBAB aqueous mixtures is investigated in Chapter 6. First, the thermodynamic stability of semi-clathrates of (CO₂, CH₄ or N₂ + TBAB) in aqueous mixtures was examined, at 0.25 and 0.50 mass fraction of TBAB in aqueous solution, in the temperature ranges of (283 to 288), (286 to 293), and (286 to 289) K, respectively. The largest promotion effect is observed for nitrogen systems, where substantial reductions in the hydrate dissociation pressures of ∼ > 90 % are evidenced. Consistent agreements with the literature data in the whole region where comparisons could be made are generally found. In the second part of Chapter 6, dissociation and compositional data for the (CO₂ + N₂ + TBAB + H₂O) systems with various CO₂ feed gas molar compositions were experimentally measured in the (275 to 291) K and (0.58 to 19.09) MPa ranges, using the methodologies described in Chapter 4. Semi-clathrates were formed with the addition of TBAB aqueous solutions with mass fractions of (0.05 and 0.30). The relative molar fractions of CO₂ in
the feed gas were (0.151, 0.399, and 0.749). Fundamental process variables were established based on the experimental dissociation conditions and phase compositional data. A significant promotion effect is observed for forming semi-clathrates, with TBAB as thermodynamic additive, compared to gas hydrates at the same temperature. As expected, the dissociation pressures generally decrease as the concentration of TBAB in the aqueous solution increases. Under the same TBAB concentration and temperature conditions, it was evidenced that increasing the concentration of nitrogen in the feed gas increases the pressure required to form semi-clathrates. Comparison with literature data shows consistent agreement over the entire temperature and pressure ranges investigated. The compositional change in the gas and liquid phases, at different temperatures under three-phase equilibrium, was measured by gas chromatography and refractometry technique, respectively. The thermodynamic promotion effect of TBAB in aqueous solutions was established in terms of dissociation pressures and temperatures and the most favorable operating conditions for a CO₂ hydrate-based separation process were proposed. The highest degree of thermodynamic promotion was observed for the (0.749 mole fraction CO₂ + 0.251 mole fraction N₂) gas mixture, where a pressure reduction of ~60% was achieved at both temperatures (282.6 and 285.7) K, compared to clathrate hydrates systems (without additive).

The experimental results suggest that CO₂ can be separated from highly to low concentrated industrial / flue gas mixtures at reasonable operating conditions in the presence of TBAB aqueous solutions. The thermodynamic analyses presented in Chapters 3 to 6 provide valuable information on the phase behavior of mixed carbon dioxide hydrates at a useful range of temperatures and pressures. The equilibrium data provided in this underlying study are fundamental for future development of thermodynamic models and design of novel technologies involving carbon dioxide gas hydrates. Further areas of improvement and some directions on future research are suggested in the following section.

### 7.2 Outlook

Although some interesting findings have been outlined throughout this investigation, further research is still required to gain a better understanding of the thermodynamic and structural
complexity of CO₂ hydrate-forming systems and semi-clathrates.

It is clear from literature examination that the phase equilibrium data available for CO₂ containing gas mixtures in TBAB aqueous mixtures are still limited. Measurements of the dissociation conditions of other CO₂ hydrate-forming systems, such as (CO₂ + CH₄) and (CO₂ + H₂) gas mixtures in TBAB aqueous solutions would be particularly useful for establishing the thermodynamic stability region and investigating the degree of promotion of TBAB in such systems, also relevant to CCS technologies and petroleum industry. Especially, further phase behavior studies are required in H₂-rich binary gas mixtures for better assessing the strong dependency of the dissociation pressures on H₂ molar concentrations. On the other hand, besides CO₂, N₂, CH₄ and H₂, the effect of impurities (e.g., CO, O₂, NO etc.), that are usually found in industrial / flue exhaust gases, on the phase equilibria of CO₂ hydrate-forming systems has been scarcely studied. This could be an interest field of research from practical point of view.

As it has been pointed out repeatedly, direct characterization of the hydrate phase is highly encouraged and necessary to provide further conclusive interpretations of thermodynamic observations. This can be achieved using suitable non-intrusive physical techniques (e.g., NMR, X-ray, or Raman spectroscopy). Knowledge on the stable hydrate structures, cage occupancies and possible structural transitions is needed for better understanding the phase behavior of mixed hydrates and TBAB semi-clathrates.

In this thesis, it was argued that the parameters of thermodynamic model should be readjusted using reliable equilibrium data for CO₂ hydrate-forming systems, as the existent models have been generally developed for hydrocarbon systems. Provided that only two thermodynamic predictive approaches (Mohammadi et al., 2010 and Paricaud, 2011) have been proposed for semi-clathrates of (H₂ + TBAB) and (CO₂ + TBAB), respectively, the development of thermodynamic predictive approaches for semi-clathrates requires further research. Especially, since a complex structural behavior (possible structure transitions) is suspected from the phase equilibrium data measured in this work. Substantial savings in experimental effort are expected with the development of accurate thermodynamic models capable of predicting the phase behavior of semi-clathrate hydrates.
Li et al. (2010) conducted a comparative investigation on the promotion effect of various quaternary ammonium salts (e.g. TBAF, TBAB and TBAC) on the phase equilibria of CO₂. Moreover, the research of Chapoy et al. (2007) has shown an increased storage capacity for hydrogen in TBAB semi-clathrates of one order of magnitude (at 1 MPa), compared to (H₂ + THF) clathrates. Moreover, Deschamps and Dalmazzone (2010) suggested that approximately two times more hydrogen can be stored in (H₂ + TBAC) and (H₂ + tetrabutylphosphonium bromide) systems compared to (H₂ + TBAB) semi-clathrates. Based on these studies, further investigations on the effect of such tetra alkyl ammonium salts on the phase equilibria of H₂ and CO₂ containing gas mixtures, could be attractive for gas separation and storage applications.

An alternative experimental procedure to the time-consuming hydrate phase equilibrium measurements through the ‘isochoric pressure-search method’ has been recently investigated at CEP-TEP. A preliminary study has been conducted for pure CO₂ hydrates in a titanium variable volume cell (Fontalba et al., 1984), with promising results (D. Richon, Personal Communication, March 9, 2012). Thermodynamic equilibrium is reached within few minutes and the hydrate dissociation pressure is identified by the presence of a plateau in a pressure versus piston displacement plot. The composition of the hydrate phase can be determined from the PVT data and the amount of gas released during hydrate dissociation (known from the with of the plateau). This method should be further investigated.

Although the apparatus developed in this thesis operated satisfactorily, certain improvements are recommended for future experimental set-ups destined to gas hydrates phase equilibrium measurements: an efficient mixing, the avoidance of dead volumes in accessories and mixing devices and accurate characterization of the liquid and hydrate phases composition through in situ sampling. Finally, performing phase equilibrium measurements at high pressures and with toxic compounds is likely hazardous. Safety considerations must be thus a priority at all times in the design of experimental set-ups, start-up of new equipment and routine operation.
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De mi pais: Venezuela, agradezco a la Fundacion Gran Mariscal de Ayacucho por el financiamiento otorgado. A PDVSA Intevep por el espacio y tiempo concedido para llevar a cabo este proyecto y concluirlo y en especial al Ing. Hector Perozo por sus oportunos consejos y apoyo para emprender esta tesis doctoral.

Finalmente, un profundo y sincero agradecimiento va para toda mi familia, en especial a mis amados padres y hermanos, y a la familia Marfisi-Gonzalez, por todo el animo, apoyo y oraciones a Dios Todopoderoso. Y, por supuesto, a mi esposo y a mis hijas mi gratitud por su infinito amor, su tolerancia, y sobre todo por haber vivido conmigo esta experiencia que pasó de ser una meta profesional a un emprendimiento mas de nuestra familia.

Paris, June 2012.

Veronica BELANDRIA
Curriculum Vitae

Veronica Belandria

Education

1994 - 1995 Foreign exchange student program. Concord High School, Elkhart, IN. USA.

Employment

2002 - 2003 Junior field engineer in well completion and productivity operations Schlumberger Oilfield Services, Venezuela, Trinidad and Tobago.

Awards and Achievements

2009 Finalist (France) for the Best Young Researcher Award. 24th European Symposium on Applied Thermodynamics. Santiago de Compostela, Spain.
2008 - 2011 Scholarship for overseas graduate studies. FUNDAYACUCHO. Venezuela.
1994 Finalist of the 11th and 12th Venezuelan Olympiads for Chemistry. CENAMEC. Venezuela.
1995 Academic-athlete award for outstanding academic achievement. Concord Community High School. Elkhart, IN, USA.
Publications

Journal Papers

**Belandria V.**; Mohammadi A. H.; Richon D. Compositional Analysis of the Gas Phase for the $\text{CO}_2 + \text{N}_2 + \text{Tetra-n-Butylammonium Bromide Aqueous Solution Systems under Hydrate Stability Conditions.} \textbf{2012} (submitted).


**Conference Papers**


APPENDIX A

Measured Hydrate Phase Equilibrium Data for CO$_2$
Containing Gases
Table A.1. Experimental ($p_{\text{exp}}$) and predicted ($p_{\text{pred}}$) dissociation conditions using thermodynamic model (HWHYD, 2000) and the equation proposed by Adisasmito and coworkers (1991) for (carbon dioxide + methane) clathrate hydrates in the presence of pure water.

<table>
<thead>
<tr>
<th>CO$_2$ (load) / mole fraction</th>
<th>$T / \text{K}$</th>
<th>$p_{\text{exp}} / \text{MPa}$ using thermodynamic model (HWHYD, 2000) assuming structure I</th>
<th>$RD / %$</th>
<th>$p_{\text{pred}} / \text{MPa}$ using thermodynamic model (HWHYD, 2000) assuming structure II</th>
<th>$RD / %$</th>
<th>$p_{\text{pred}} / \text{MPa}$ the equation proposed by Adisasmito and coworkers (1991)</th>
<th>$RD / %$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.264</td>
<td>284.2</td>
<td>5.29</td>
<td>6.80</td>
<td>-2.9E+01</td>
<td>12.23</td>
<td>-1.3E+02</td>
<td>6.64</td>
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<tr>
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<td>287.2</td>
<td>9.83</td>
<td>9.94</td>
<td>-1.1E+00</td>
<td>18.86</td>
<td>-9.2E+01</td>
<td>9.76</td>
</tr>
<tr>
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<td>289.2</td>
<td>11.62</td>
<td>13.16</td>
<td>-1.3E+01</td>
<td>25.51</td>
<td>-1.2E+02</td>
<td>12.76</td>
</tr>
<tr>
<td>0.272</td>
<td>279.1</td>
<td>3.60</td>
<td>3.79</td>
<td>-5.3E+00</td>
<td>6.40</td>
<td>-7.8E+01</td>
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<tr>
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<tr>
<td>0.490</td>
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<td>12.41</td>
<td>15.10</td>
<td>-2.2E+01</td>
<td>40.36</td>
<td>-2.3E+02</td>
<td>12.90</td>
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<tr>
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<td>284.9</td>
<td>5.88</td>
<td>6.65</td>
<td>-1.3E+01</td>
<td>17.86</td>
<td>-2.0E+02</td>
<td>6.42</td>
</tr>
<tr>
<td>0.500</td>
<td>279.1</td>
<td>2.96</td>
<td>3.18</td>
<td>-7.4E+00</td>
<td>7.53</td>
<td>-1.5E+02</td>
<td>3.09</td>
</tr>
<tr>
<td>0.504</td>
<td>280.6</td>
<td>3.16</td>
<td>3.42</td>
<td>-8.2E+00</td>
<td>11.55</td>
<td>-2.7E+02</td>
<td>3.34</td>
</tr>
<tr>
<td>0.730</td>
<td>281.9</td>
<td>4.02</td>
<td>4.03</td>
<td>-2.5E-01</td>
<td>15.47</td>
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<td>3.95</td>
</tr>
<tr>
<td></td>
<td>289.1</td>
<td>13.06</td>
<td>15.21</td>
<td>-1.6E+01</td>
<td>63.88</td>
<td>-3.9E+02</td>
<td>10.92</td>
</tr>
</tbody>
</table>

AARD $^c$/%  

| 13.7E+00 | 16.1E+01 | 7.9E+00 |

Maximum uncertainties in mole fractions and dissociation temperatures and pressures are expected to be within ±1-2%, ±0.2 K and ±0.05 MPa, respectively.
Table A.2. Experimental ($p^{exp}$) and predicted ($p^{pred}$) dissociation conditions using two thermodynamic models: HWHYD (2000) and CSMGem (2008), for (carbon dioxide + methane) clathrate hydrates in the presence of pure water.

<table>
<thead>
<tr>
<th>Mole fraction of CO$_2$ in the gas feed</th>
<th>Mole fraction of H$_2$O supplied to the system</th>
<th>$T / K$</th>
<th>$p^{exp} / MPa$</th>
<th>$p^{pred}$ / MPa using HWHYD model</th>
<th>$ARD$ $^b$ / %</th>
<th>$p^{pred}$ / MPa using CSMGem model</th>
<th>$ARD$ / %</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.206</td>
<td>0.871</td>
<td>279.3</td>
<td>4.03</td>
<td>4.18</td>
<td>3.7</td>
<td>3.98</td>
<td>1.2</td>
</tr>
<tr>
<td>0.206</td>
<td>0.961</td>
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<td>5.48</td>
<td>5.86</td>
<td>6.9</td>
<td>5.67</td>
<td>3.5</td>
</tr>
<tr>
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<td>0.975</td>
<td>285.5</td>
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<td>8.84</td>
<td>6.9</td>
<td>8.71</td>
<td>5.3</td>
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<tr>
<td>0.476</td>
<td>0.877</td>
<td>277.9</td>
<td>2.72</td>
<td>2.97</td>
<td>9.2</td>
<td>2.78</td>
<td>2.2</td>
</tr>
<tr>
<td>0.476</td>
<td>0.959</td>
<td>279.8</td>
<td>3.61</td>
<td>3.94</td>
<td>9.1</td>
<td>3.68</td>
<td>1.9</td>
</tr>
<tr>
<td>0.476</td>
<td>0.973</td>
<td>285.0</td>
<td>6.09</td>
<td>7.62</td>
<td>25</td>
<td>7.34</td>
<td>21</td>
</tr>
<tr>
<td>0.744</td>
<td>0.877</td>
<td>279.0</td>
<td>2.72</td>
<td>2.85</td>
<td>4.8</td>
<td>2.73</td>
<td>0.4</td>
</tr>
<tr>
<td>0.744</td>
<td>0.956</td>
<td>280.1</td>
<td>3.21</td>
<td>3.42</td>
<td>6.5</td>
<td>3.26</td>
<td>1.6</td>
</tr>
<tr>
<td>0.744</td>
<td>0.972</td>
<td>283.2</td>
<td>4.70</td>
<td>5.39</td>
<td>15</td>
<td>5.12</td>
<td>8.9</td>
</tr>
</tbody>
</table>

AARD $^c$ % 9.7 5.1

Maximum uncertainties in CO$_2$ mole fractions and dissociation temperatures and pressures are expected to be within ± 1-2%, ± 0.2 K and ± 0.05 MPa, respectively. Uncertainties in mole fractions of H$_2$O supplied to the system are expected to be within 0.5%.

$^a$ (Assuming sI).

$^b$ \( ARD = 100 \times \left( \frac{p^{exp} - p^{pred}}{p^{exp}} \right) \)

$^c$ \( AARD = \frac{1}{n} \sum |ARD| \)
Table A.3. Three-phase equilibrium data for (CO₂ + CH₄ + H₂O) systems at different temperatures and pressures.

<table>
<thead>
<tr>
<th>Feed</th>
<th>T/K</th>
<th>p/MPa</th>
<th>Experimental data (Compositional analysis)</th>
<th>CSMGem model predictions (Compositional analysis)</th>
<th>Absolute relative deviations (ARD %)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CO₂ / mole</td>
<td>CH₄ / mole</td>
<td>H₂O / mole</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>Gas phase</td>
<td>Hydrate phase</td>
<td>Aqueous phase</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>1.43</td>
<td>273.6</td>
<td>2.234</td>
<td>0.141</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>5.236</td>
<td>273.6</td>
<td>2.416</td>
<td>0.125</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>8.185</td>
<td>273.6</td>
<td>2.440</td>
<td>0.081</td>
</tr>
<tr>
<td>0.116</td>
<td>0.115</td>
<td>1.65</td>
<td>273.6</td>
<td>1.844</td>
<td>0.345</td>
</tr>
<tr>
<td>0.116</td>
<td>0.115</td>
<td>5.355</td>
<td>273.6</td>
<td>1.941</td>
<td>0.288</td>
</tr>
<tr>
<td>0.116</td>
<td>0.115</td>
<td>8.48</td>
<td>273.6</td>
<td>2.048</td>
<td>0.220</td>
</tr>
<tr>
<td>0.181</td>
<td>0.057</td>
<td>1.696</td>
<td>273.6</td>
<td>1.510</td>
<td>0.630</td>
</tr>
<tr>
<td>0.181</td>
<td>0.057</td>
<td>5.182</td>
<td>273.6</td>
<td>1.607</td>
<td>0.545</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>1.43</td>
<td>275.2</td>
<td>2.583</td>
<td>0.166</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>5.236</td>
<td>275.2</td>
<td>2.712</td>
<td>0.129</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>8.185</td>
<td>275.2</td>
<td>2.766</td>
<td>0.086</td>
</tr>
<tr>
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<td>0.115</td>
<td>1.65</td>
<td>275.2</td>
<td>2.123</td>
<td>0.384</td>
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<tr>
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<td>0.115</td>
<td>5.355</td>
<td>275.2</td>
<td>2.220</td>
<td>0.302</td>
</tr>
<tr>
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<td>0.115</td>
<td>8.48</td>
<td>275.2</td>
<td>2.400</td>
<td>0.228</td>
</tr>
<tr>
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<td>1.696</td>
<td>275.2</td>
<td>1.792</td>
<td>0.657</td>
</tr>
<tr>
<td>0.181</td>
<td>0.057</td>
<td>5.182</td>
<td>275.2</td>
<td>1.865</td>
<td>0.565</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>1.43</td>
<td>276.1</td>
<td>2.813</td>
<td>0.179</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>5.236</td>
<td>276.1</td>
<td>3.025</td>
<td>0.134</td>
</tr>
<tr>
<td>0.048</td>
<td>0.165</td>
<td>8.185</td>
<td>276.1</td>
<td>3.027</td>
<td>0.096</td>
</tr>
<tr>
<td>0.116</td>
<td>0.115</td>
<td>1.65</td>
<td>276.1</td>
<td>2.318</td>
<td>0.405</td>
</tr>
<tr>
<td>0.116</td>
<td>0.115</td>
<td>5.355</td>
<td>276.1</td>
<td>2.503</td>
<td>0.315</td>
</tr>
<tr>
<td>0.116</td>
<td>0.115</td>
<td>8.48</td>
<td>276.1</td>
<td>2.690</td>
<td>0.232</td>
</tr>
<tr>
<td>0.181</td>
<td>0.057</td>
<td>1.696</td>
<td>276.1</td>
<td>1.985</td>
<td>0.669</td>
</tr>
<tr>
<td>AAD %</td>
<td>9.7 20.3 27.1 38.8 0.2</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>-------</td>
<td>------------------------</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

*: HWHYD model does not converge for the studied conditions.

*a* Some/all of constraints are not satisfied.

*b* No three phase flash convergence using CSMGem model.
Table A.4. Hydrate dissociation conditions of (CO$_2$ + N$_2$) binary gas mixtures in the presence of water.

<table>
<thead>
<tr>
<th>Mole fraction of CO$_2$ in the gas feed</th>
<th>Mole fraction of H$_2$O supplied to the system</th>
<th>$T^a$ / K</th>
<th>$p^{exp}$ / MPa</th>
<th>$p^{pred}$ / MPa using HWHYD model$^b$</th>
<th>ARD / %</th>
<th>$p^{pred}$ / MPa using CSMGem model</th>
<th>ARD / %</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.812</td>
<td>0.779</td>
<td>284.1</td>
<td>7.07</td>
<td>7.44</td>
<td>5.2</td>
<td>8.05</td>
<td>14</td>
</tr>
<tr>
<td>0.773</td>
<td>0.847</td>
<td>279.2</td>
<td>3.24</td>
<td>3.37</td>
<td>4.0</td>
<td>3.49</td>
<td>7.7</td>
</tr>
<tr>
<td>0.773</td>
<td>0.965</td>
<td>280.0</td>
<td>5.00</td>
<td>4.72</td>
<td>5.6</td>
<td>5.60</td>
<td>12</td>
</tr>
<tr>
<td>0.748</td>
<td>0.889</td>
<td>280.5</td>
<td>4.16</td>
<td>4.17</td>
<td>0.2</td>
<td>4.50</td>
<td>8.2</td>
</tr>
<tr>
<td>0.476</td>
<td>0.803</td>
<td>278.1</td>
<td>4.76</td>
<td>4.87</td>
<td>2.3</td>
<td>4.95</td>
<td>4.0</td>
</tr>
<tr>
<td>0.476</td>
<td>0.943</td>
<td>280.7</td>
<td>10.67</td>
<td>10.59</td>
<td>0.8</td>
<td>10.60</td>
<td>0.7</td>
</tr>
<tr>
<td>0.271</td>
<td>0.666</td>
<td>279.6</td>
<td>9.76</td>
<td>10.63</td>
<td>8.9</td>
<td>10.92</td>
<td>12</td>
</tr>
<tr>
<td>0.271</td>
<td>0.895</td>
<td>282.4</td>
<td>19.17</td>
<td>19.38</td>
<td>1.1</td>
<td>20.06</td>
<td>4.6</td>
</tr>
<tr>
<td>0.271</td>
<td>0.956</td>
<td>285.3</td>
<td>29.92</td>
<td>29.13</td>
<td>2.6</td>
<td>38.77</td>
<td>30</td>
</tr>
</tbody>
</table>

$^a$ Maximum uncertainties in dissociation temperatures and pressures are expected to be within ± 0.2 K and ± 0.05 MPa, as indicated in Chapter 2.

$^b$ Assuming sI for N$_2$ simple hydrates.

$$ARD = 100 \times \frac{|p^{exp} - p^{pred}|}{p^{exp}}$$
Table A.5. Three-phase equilibrium data for gas mixtures of (CO$_2$ + N$_2$) in the presence of water at different temperatures (T) and pressures (p): Experimental and predicted values.

<table>
<thead>
<tr>
<th>feed</th>
<th>experimental data</th>
<th>CSMGem model predictions*</th>
<th>absolute relative deviation (ARD %)*</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>gas phase</td>
<td>hydrate phase</td>
<td>aqueous phase</td>
</tr>
<tr>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>Column</td>
<td>Value</td>
<td>Column</td>
<td>Value</td>
</tr>
<tr>
<td>--------</td>
<td>-------</td>
<td>--------</td>
<td>-------</td>
</tr>
<tr>
<td>2066</td>
<td>0.695</td>
<td>1.543</td>
<td>277.1</td>
</tr>
<tr>
<td>2547</td>
<td>0.0898</td>
<td>2.7525</td>
<td>277.3</td>
</tr>
<tr>
<td>4371</td>
<td>0.1472</td>
<td>2.0555</td>
<td>277.8</td>
</tr>
<tr>
<td>2086</td>
<td>0.0695</td>
<td>1.543</td>
<td>278.1</td>
</tr>
<tr>
<td>2547</td>
<td>0.0898</td>
<td>2.7525</td>
<td>278.1</td>
</tr>
<tr>
<td>2086</td>
<td>0.0695</td>
<td>7.649</td>
<td>278.1</td>
</tr>
<tr>
<td>1947</td>
<td>0.5842</td>
<td>1.552</td>
<td>278.1</td>
</tr>
<tr>
<td>1947</td>
<td>0.5842</td>
<td>6.6615</td>
<td>278.1</td>
</tr>
<tr>
<td>2086</td>
<td>0.0695</td>
<td>7.649</td>
<td>279.7</td>
</tr>
<tr>
<td>1845</td>
<td>0.196</td>
<td>6.273</td>
<td>279.7</td>
</tr>
<tr>
<td>1947</td>
<td>0.5842</td>
<td>6.6615</td>
<td>279.7</td>
</tr>
<tr>
<td>1947</td>
<td>0.5842</td>
<td>6.6615</td>
<td>281.2</td>
</tr>
<tr>
<td>4371</td>
<td>0.1472</td>
<td>2.0555</td>
<td>281.7</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Total</th>
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<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
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<th></th>
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</thead>
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<td>9.9</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

\(^a\) Predictions of HWHYD model are not shown as N\(_2\) hydrate is modeled considering structure I.

\(^b\) \(\text{ARD} = 100 \times \frac{p_{\text{exp}} - p_{\text{pred}}}{p_{\text{exp}}}\)

\(^c\) Some/all of constraints are not satisfied.

\(^d\) No three phase flash convergence using CSMGem model.

\(^e\) Gas hydrate structure.
Table A.6. Hydrate dissociation conditions of (CO$_2$ + H$_2$) binary gas mixtures in the presence of water.

<table>
<thead>
<tr>
<th>Mole fraction of CO$_2$ in the gas feed</th>
<th>$T$ / K</th>
<th>$p$ / MPa</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.829</td>
<td>277.2</td>
<td>2.44</td>
</tr>
<tr>
<td>0.829</td>
<td>277.7</td>
<td>2.58</td>
</tr>
<tr>
<td>0.829</td>
<td>278.1</td>
<td>2.66</td>
</tr>
<tr>
<td>0.709</td>
<td>279.6</td>
<td>3.84</td>
</tr>
<tr>
<td>0.709</td>
<td>280.1</td>
<td>4.46</td>
</tr>
<tr>
<td>0.508</td>
<td>279.8</td>
<td>7.21</td>
</tr>
<tr>
<td>0.508</td>
<td>280.4</td>
<td>8.53</td>
</tr>
<tr>
<td>0.508</td>
<td>283.0</td>
<td>24.76</td>
</tr>
</tbody>
</table>
Table A.7. Compositional data for the gas phase in equilibrium with the hydrate and aqueous phases at different temperatures ($T$) and pressures ($p$) for various ($\text{CO}_2 + \text{H}_2$) gas mixtures in the presence of water.

<table>
<thead>
<tr>
<th>Gaseous feed</th>
<th>(L_w-H-G) equilibrium</th>
</tr>
</thead>
<tbody>
<tr>
<td>CO_2 / mole fraction</td>
<td>$T / \text{K}$</td>
</tr>
<tr>
<td>0.780</td>
<td>273.6</td>
</tr>
<tr>
<td>0.829</td>
<td>273.6</td>
</tr>
<tr>
<td>0.829</td>
<td>273.6</td>
</tr>
<tr>
<td>0.508</td>
<td>273.6</td>
</tr>
<tr>
<td>0.508</td>
<td>273.6</td>
</tr>
<tr>
<td>0.709</td>
<td>273.6</td>
</tr>
<tr>
<td>0.829</td>
<td>275.2</td>
</tr>
<tr>
<td>0.829</td>
<td>275.2</td>
</tr>
<tr>
<td>0.508</td>
<td>275.2</td>
</tr>
<tr>
<td>0.508</td>
<td>275.2</td>
</tr>
<tr>
<td>0.709</td>
<td>275.2</td>
</tr>
<tr>
<td>0.709</td>
<td>275.2</td>
</tr>
<tr>
<td>0.709</td>
<td>275.2</td>
</tr>
<tr>
<td>0.829</td>
<td>276.2</td>
</tr>
<tr>
<td>0.829</td>
<td>276.2</td>
</tr>
<tr>
<td>0.508</td>
<td>276.2</td>
</tr>
<tr>
<td>0.508</td>
<td>276.2</td>
</tr>
<tr>
<td>0.709</td>
<td>276.2</td>
</tr>
<tr>
<td>0.709</td>
<td>276.2</td>
</tr>
<tr>
<td>0.829</td>
<td>277.1</td>
</tr>
<tr>
<td>0.508</td>
<td>277.1</td>
</tr>
<tr>
<td>0.709</td>
<td>277.1</td>
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<tr>
<td>0.508</td>
<td>278.1</td>
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<tr>
<td>0.508</td>
<td>278.1</td>
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<tr>
<td>0.709</td>
<td>278.1</td>
</tr>
<tr>
<td>0.709</td>
<td>278.1</td>
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<tr>
<td>0.709</td>
<td>279.1</td>
</tr>
<tr>
<td>0.709</td>
<td>279.1</td>
</tr>
<tr>
<td>0.709</td>
<td>279.1</td>
</tr>
<tr>
<td>0.709</td>
<td>280.1</td>
</tr>
<tr>
<td>0.709</td>
<td>280.1</td>
</tr>
<tr>
<td>0.709</td>
<td>281.2</td>
</tr>
</tbody>
</table>
Table A.8. Experimental dissociation conditions of (TBAB + methane), (TBAB + carbon dioxide) and (TBAB + nitrogen) semi-clathrate hydrates ($w = 0.25$).

<table>
<thead>
<tr>
<th>$T/\text{K}$</th>
<th>$p/\text{MPa}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>(TBAB + methane) semi-clathrate hydrates</td>
<td></td>
</tr>
<tr>
<td>285.2</td>
<td>0.235</td>
</tr>
<tr>
<td>286.7</td>
<td>0.444</td>
</tr>
<tr>
<td>287.1</td>
<td>0.678</td>
</tr>
<tr>
<td>287.6</td>
<td>0.954</td>
</tr>
<tr>
<td>288.1</td>
<td>1.171</td>
</tr>
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<td>1.848</td>
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<tr>
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<td>2.888</td>
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<td>5.124</td>
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<tr>
<td>294.7</td>
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<td></td>
</tr>
<tr>
<td>284.0</td>
<td>0.104</td>
</tr>
<tr>
<td>284.9</td>
<td>0.293</td>
</tr>
<tr>
<td>285.6</td>
<td>0.530</td>
</tr>
<tr>
<td>286.5</td>
<td>0.769</td>
</tr>
<tr>
<td>287.9</td>
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</tr>
<tr>
<td>288.9</td>
<td>1.575</td>
</tr>
<tr>
<td>290.0</td>
<td>1.989</td>
</tr>
<tr>
<td>(TBAB + nitrogen) semi-clathrate hydrates</td>
<td></td>
</tr>
<tr>
<td>281.1</td>
<td>0.470</td>
</tr>
<tr>
<td>284.0</td>
<td>0.780</td>
</tr>
<tr>
<td>284.5</td>
<td>0.870</td>
</tr>
<tr>
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<td>2.190</td>
</tr>
<tr>
<td>286.8</td>
<td>3.000</td>
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</table>
Table A.9. Experimental dissociation conditions of (TBAB + methane), (TBAB + carbon dioxide) and (TBAB + nitrogen) semi-clathrate hydrates ($w = 0.50$).

<table>
<thead>
<tr>
<th>$T$ / K</th>
<th>$p$ / MPa</th>
</tr>
</thead>
<tbody>
<tr>
<td>(TBAB + methane) semi-clathrate hydrates</td>
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<tr>
<td>285.6</td>
<td>0.317</td>
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<tr>
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<td>291.3</td>
<td>5.247</td>
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<tr>
<td>292.8</td>
<td>8.260</td>
</tr>
<tr>
<td>(TBAB + carbon dioxide) semi-clathrate hydrates</td>
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<tr>
<td>282.6</td>
<td>0.698</td>
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<tr>
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<td>286.9</td>
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<tr>
<td>287.9</td>
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<td>(TBAB + nitrogen) semi-clathrate hydrates</td>
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<tr>
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<td>2.790</td>
</tr>
<tr>
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</table>
Table A.10. Semi-clathrate hydrate phase equilibrium data for the (CO₂ + N₂ + TBAB + H₂O) mixtures.

<table>
<thead>
<tr>
<th>Feed gas composition / CO₂ mole fraction</th>
<th>TBAB / mass fraction</th>
<th>T / K</th>
<th>p / MPa</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.05</td>
<td>0.749</td>
<td>281.0</td>
<td>0.67</td>
</tr>
<tr>
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<td></td>
<td>281.5</td>
<td>0.91</td>
</tr>
<tr>
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<td></td>
<td>282.8</td>
<td>1.47</td>
</tr>
<tr>
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<td></td>
<td>284.2</td>
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</tr>
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<td></td>
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<td>1.06</td>
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<td>289.7</td>
<td>2.70</td>
<td></td>
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<tr>
<td></td>
<td>291.0</td>
<td>3.70</td>
<td></td>
</tr>
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<td>0.399</td>
<td>283.6</td>
<td>3.78</td>
</tr>
<tr>
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<td></td>
<td>286.2</td>
<td>6.58</td>
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<td>287.1</td>
<td>1.78</td>
<td></td>
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<td>5.46</td>
</tr>
<tr>
<td></td>
<td></td>
<td>285.1</td>
<td>8.14</td>
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</tr>
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<td></td>
<td>289.2</td>
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</tr>
<tr>
<td>0.30</td>
<td>285.7</td>
<td>1.55</td>
<td></td>
</tr>
</tbody>
</table>
Table A.11. Compositional phase equilibrium data for (CO$_2$ + N$_2$) gas mixtures in (0.05 mass fraction) TBAB aqueous solutions.

<table>
<thead>
<tr>
<th>CO$_2$ / molar fraction</th>
<th>p / MPa</th>
<th>$n_{\text{gas mixture}}$ / mole</th>
<th>CO$_2$ / mole</th>
<th>N$_2$ / mole</th>
<th>TBAB aqueous sol. (0.05 mass fraction)</th>
<th>T / K</th>
<th>p / MPa</th>
<th>$y_{\text{CO2}}$ / molar composition of CO$_2$ in the gas phase</th>
<th>$x_{\text{TBAB}}$ / mass fraction of TBAB in the liq. phase</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.749</td>
<td>0.960</td>
<td>0.076</td>
<td>0.057</td>
<td>0.019</td>
<td>0.241</td>
<td>275.15*</td>
<td>0.786</td>
<td>0.640</td>
<td>0.024</td>
</tr>
<tr>
<td>0.749</td>
<td>1.415</td>
<td>0.113</td>
<td>0.085</td>
<td>0.028</td>
<td>0.213</td>
<td>275.20*</td>
<td>0.942</td>
<td>0.586</td>
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</tr>
<tr>
<td>0.399</td>
<td>3.236</td>
<td>0.256</td>
<td>0.102</td>
<td>0.154</td>
<td>0.195</td>
<td>275.18*</td>
<td>3.519</td>
<td>0.289</td>
<td>0.018</td>
</tr>
<tr>
<td>0.399</td>
<td>3.236</td>
<td>0.256</td>
<td>0.102</td>
<td>0.154</td>
<td>0.423</td>
<td>275.18*</td>
<td>5.492</td>
<td>0.172</td>
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</tr>
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<td>0.151</td>
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<td>0.980</td>
<td>0.147</td>
<td>0.833</td>
<td>0.149</td>
<td>275.17*</td>
<td>12.254</td>
<td>0.080</td>
<td>0.013</td>
</tr>
<tr>
<td>0.151</td>
<td>12.606</td>
<td>0.980</td>
<td>0.147</td>
<td>0.833</td>
<td>0.268</td>
<td>275.23*</td>
<td>14.525</td>
<td>0.058</td>
<td>0.012</td>
</tr>
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<td>0.960</td>
<td>0.076</td>
<td>0.057</td>
<td>0.019</td>
<td>0.241</td>
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<td>0.803</td>
<td>0.596</td>
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</tr>
<tr>
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<td>0.960</td>
<td>0.076</td>
<td>0.057</td>
<td>0.019</td>
<td>0.241</td>
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</tr>
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<td>0.057</td>
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<td>279.69</td>
<td>14.032</td>
<td>0.129</td>
<td>0.013</td>
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<td>0.833</td>
<td>0.268</td>
<td>279.69</td>
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<td>0.195</td>
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<td>0.833</td>
<td>0.149</td>
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<td>0.013</td>
</tr>
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</table>
Cont. Table A.11. Compositional phase equilibrium data for (CO$_2$ + N$_2$) gas mixtures in (0.05 mass fraction) TBAB aqueous solutions.

<table>
<thead>
<tr>
<th>CO$_2$ / molar fraction</th>
<th>Feed</th>
<th>p / MPa</th>
<th>$n_{\text{gas mixture}}$ / mole</th>
<th>CO$_2$ / mole</th>
<th>N$_2$ / mole</th>
<th>TBAB aqueous sol. (0.05 mass fraction)</th>
<th>Compositional Equilibrium Data</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>T / K</td>
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<td>0.195</td>
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<tr>
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<td>0.147</td>
<td>0.833</td>
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</tr>
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<td>0.102</td>
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<td>0.423</td>
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<td>283.73</td>
</tr>
<tr>
<td>0.151</td>
<td>12.606</td>
<td>0.980</td>
<td>0.147</td>
<td>0.833</td>
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*: Likely represents semi-clathrates of (TBAB + water).
Table A.12. Compositional phase equilibrium data for (CO$_2$ + N$_2$) gas mixtures in (0.30 mass fraction) TBAB aqueous solutions.

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<tr>
<th>Feed</th>
<th>CO$_2$ / molar fraction</th>
<th>p / MPa</th>
<th>n$_{\text{gas mixture}}$ / mole</th>
<th>CO$_2$ / mole</th>
<th>N$_2$ / mole</th>
<th>TBAB aqueous sol. (0.30 mass fraction)</th>
<th>Compositional Equilibrium Data</th>
<th>T / K</th>
<th>p / MPa</th>
<th>y$_{\text{CO}_2}$ / molar composition of CO$_2$ in the gas phase</th>
<th>x$_{\text{TBAB}}$ / mass fraction of TBAB in the liq. phase</th>
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<td>0.239</td>
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</table>

*: Likely represents semi-clathrates of (TBAB + water); “: no liquid phase sample due to valve obstruction by hydrates.
Tetra-n-Butyl Ammonium Bromide + Water Systems: Density Measurements and Correlation†

Appendix B: Tetra-n-Butyl Ammonium Bromide + Water Systems: Density Measurements and Correlation

In this study, density data for the binary mixtures of (water + tetra-n-butyl ammonium bromide) at atmospheric pressure and various temperatures are given and correlated. Research grade TBAB aqueous solution with a concentration of (50 mass% TBAB) was purchased from Aldrich. Double-distilled and deionized water obtained from a Direct-Q5 Ultrapure Water System (Millipore™) was degassed and used to prepare the aqueous solutions. Samples were prepared following the gravimetric procedure described below. An Anton Paar vibrating-tube digital densimeter (model DMA 5000) with a certified precision of $10^{-5}$ g.cm$^{-3}$ for density and ±0.01 K for temperature was used to carry out the density measurements. The density determination is based on measuring the period of oscillation of a vibrating U-shaped hollow tube that is filled with the sample. The densimeter was calibrated with double-distilled, degassed water, and dry air at 293.15 K and atmospheric pressure before measuring each sample. Samples were carefully loaded using a syringe avoiding the introduction of any air bubbles and achieving satisfactory purging. Densities were measured at thermal equilibrium after successive increases of temperature. After each series of measurements, the densimeter was washed and dried. All measurements were repeated at least three times and average density values are reported.

The gravimetric procedure used to prepare the TBAB aqueous solutions is essentially similar to that of previous studies performed in our laboratory (Valtz et al. 2004). Briefly, 20 cm$^3$ glass bottles were air-tight closed with a septum and then evacuated using a vacuum pump through a syringe needle introduced across the septum. Empty bottles were weighed, and then water (freshly degassed through vacuum distillation) was introduced by means of a syringe. After weighing the bottle loaded with water, TBAB was added and the bottle was weighed again. All weighing were carried out using an analytical balance (Mettler AT200) with an accuracy of 0.0001 g. As no chemical reaction is expected to occur between the two components in the mixture, the average uncertainty in molar compositions is assumed to be better than 0.0003, as demonstrated by Mokraoui and coworkers (2006). The above preparation and loading procedures were followed not only to obtain accurate compositions, but also to avoid the formation of gas bubbles inside the vibrating tube. This may occur at high temperatures, especially if the liquid is not well degassed (Mokraoui et al., 2006).
As TBAB aqueous solutions may crystallize under atmospheric pressure and temperatures between 0 and 12 °C (Darbouret et al., 2005), density measurements were carried out from (293.15 to 333.15) K. The measured density data are reported in Table B.1 and are correlated using the equation proposed by Söhnel and Novotny (1985), as follows:

\[ \rho_w = \rho_2 + B_1 100w + B_2 (100w)^2 + B_3 (100w)^3 \]  

(B.1)

where \( w \) is the mass fraction of salt, which is used instead of mole fraction for this system, and \( \rho_w \) is the density of water. \( B_i \) are assumed temperature dependent as follows:

\[ B_i = e_i + f_i (T/K) + g_i (T/K)^2 \]  

(B.2)

where \( e_i, f_i \) and \( g_i \) are empirical constants. Results of density calculations using equation (B.1) are given in Table B.1. The derived coefficients are used section 6.2.2 to estimate the density of the liquid phase (at the given equilibrium temperature) and the corresponding number of moles loaded to the system, reported in Tables A.11 and A.12.

Experimental and calculated values from equation (B.1) for densities of (TBAB + water) systems show a consistent agreement. The average absolute deviation (AAD) between measured and calculated values from this polynomial equation for density was 0.06 %. The concentration dependence of the present density measurements and the TBAB mass fraction is shown in Figure B.1. It is evident from the values given in Table B.2 and shown Figure 6.1 that density increases as the mass fraction of TBAB increases at a given the temperature. Also, density decreases as temperature increases at a given concentration of TBAB.

The AAD [%] was determined using the following relationship:

\[ AAD(\rho) = \frac{1}{N} \sum_{n=1}^{N} \left| \frac{\rho_{\text{exp}} - \rho_{\text{cal}}}{\rho_{\text{exp}}} \right| \]  

(B.3)
Table B.1. Determined parameters of density equation (eq. B.1) for (TBAB + H\textsubscript{2}O) binary system.

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<th>TBAB/H\textsubscript{2}O</th>
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</tr>
<tr>
<td>(f_1)</td>
<td>5.963 (\cdot) 10\textsuperscript{-6}</td>
</tr>
<tr>
<td>(e_1)</td>
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<tr>
<td>(g_2)</td>
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<tr>
<td>(f_2)</td>
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</tr>
<tr>
<td>(e_2)</td>
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<tr>
<td>(g_3)</td>
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<td>(f_3)</td>
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<td>AAD %</td>
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<td>No. of data points</td>
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Figure B.1. Density (\(\rho\)) against mass fraction (\(w\)) for binary mixtures of (TBAB + H\textsubscript{2}O) calculated with equation (6.1), at \(T = 333.15\) K (-); 328.15 K (\(\triangle\)); 323.15 K (+); 318.15 K (\(\bullet\)); 313.15 K (\(\ast\)); 308.15 K (\(\times\)); 303.15 K (\(\uparrow\)); 298.15 K (\(\blacksquare\)), and 293.15 K (\(\blacklozenge\)). Density values at \(w = 0\) are experimental data. Solid lines are tendency curves.
Table B.2. Mass fraction of TBAB and density ($\rho$ (g.cm$^{-3}$)) of (TBAB + H$_2$O) mixtures from (293.15 to 333.15) K.

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Étude expérimentale des équilibres d’hydrates de mélanges de gaz contenant du CO₂ en solutions aqueuses de promoteur thermodynamique

**RESUME** : Cette thèse présente les mesures et l'analyse thermodynamique d'équilibres de phases de systèmes d'hydrates contenant du dioxyde de carbone (CO₂), dans le contexte de procédés alternatifs de captage du CO₂. Le développement de nouveaux procédés de séparation par voie de cristallisation par hydrates est un point crucial de cette thématique. Les conditions de température et de pression requises et l'utilisation de promoteurs thermodynamiques sont au-delà des opérations habituelles et des bases de données existantes. La connaissance précise des conditions de formation et dissociation d'hydrates de gaz en présence d'additifs chimiques constitue une contrainte importante d'un point de vue thermodynamique et est nécessaire pour la modélisation et l'établissement de la faisabilité de nouveaux procédés industriels impliquant des hydrates de gaz. Dans cette thèse, nous présentons un nouveau dispositif expérimental qui combine techniques statiques et techniques analytiques, ce dernier a été spécialement développé pour mesurer des données d'équilibres des phases hydrate-liquide-gaz à des températures variant entre 233 et 373 K et à des pressions jusqu'à 60 MPa. De nouvelles données d'équilibre de phases des systèmes (CO₂ + méthane), (CO₂ + azote) et (CO₂ + hydrgène) ont été mesurées dans des conditions de formation d'hydrates en suivant la méthode isochorique avec variation de la pression en fonction de la température, et en analysant la composition en phase gazeuse. Les données d'équilibre et les conditions de dissociation d'hydrates générées dans ce travail sont comparées avec les données de la littérature. La fiabilité des modèles thermodynamiques les plus couramment utilisés est aussi étudiée. Les comparaisons entre les données expérimentales et prédites de dissociation d'hydrates suggèrent la nécessité de réajuster les paramètres des modèles thermodynamiques pour les systèmes contenant des hydrates de CO₂. En outre, l'effet promoteur du bromure de tetrabutylammonium (TBAB) sur les équilibres des phases des gaz purs et de mélanges contenant du CO₂ a été étudié. L'effet le plus important de promotion (réduction de la pression de formation des hydrates > 90%) est observé pour le système (TBAB + azote). Les résultats expérimentaux suggèrent que le CO₂ peut être séparé de mélanges de gaz industriels ou de combustion à des températures douces et à de basses pressions à l'aide de TBAB en tant que promoteur thermodynamique. La pression requise pour la formation d'hydrates à partir de mélanges de (CO₂ + azote) est réduite de 60 % en présence de TBAB.

**Mots clés** : Hydrates de gaz, semi-clathrate, dioxyde de carbone, TBAB, mesure expérimentale, équilibre des phases.

**Hydrate Phase Equilibria Study of CO₂ Containing Gases in Thermodynamic Promoter Aqueous Mixtures**

**ABSTRACT** : This thesis addresses the measurement and thermodynamic analysis of the phase equilibrium behavior of carbon dioxide (CO₂) hydrate-forming systems in the context of alternative capture engineering approaches. The development of new technologies based on gas hydrates requires specific temperature and pressure conditions and the utilization of thermodynamic promoters that are beyond usual operations and existing databases. Accurate knowledge of gas hydrates formation and dissociation from thermodynamics point of view in the presence of chemical additives is necessary for modeling purposes and to establish the feasibility of emerging industrial processes involving gas hydrates. In this thesis, a new experimental set-up and method for measuring pressure, temperature and compositional phase equilibrium data of high accuracy are presented. The equipment is based on the ‘static-analytic’ technique with gas phase capillary sampling and it is suitable for measurements in a wide temperature range (i.e. 233 to 373 K) and pressures up to 60 MPa. New phase equilibrium data in the (CO₂ + methane), (CO₂ + nitrogen) and (CO₂ + hydrogen) systems under hydrate formation conditions were measured following an isochoric pressure-search method in combination with gas phase compositional analysis. The equilibrium data generated in this work are compared with literature data and also with the predictions of two thermodynamic literature models. Comparisons between experimental and predicted hydrate dissociation data suggest a need of readjusting model parameters for CO₂ hydrate-forming systems. In addition, the thermodynamic stability of Tetra-n-Butyl Ammonium Bromide (TBAB) semi-clathrates (sc) with pure and mixed gases was investigated. The largest promotion effect (> 90% reduction in hydrate formation pressure) is observed for (TBAB + nitrogen) sc. The experimental results suggest that CO₂ can be separated from highly to low concentrated industrial/flue gas mixtures at mild temperatures and low pressures by using TBAB as thermodynamic promoter. The pressure required for hydrate formation from (CO₂ + nitrogen) gas mixtures is reduced by 60% in the presence of TBAB.

**Keywords** : Gas hydrate, semi-clathrate, carbon dioxide, TBAB, experimental measurement, phase equilibria.