K-Means on Azure
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Contribution
We present how parallel machine learning algorithms can be implemented on top of Microsoft Windows Azure cloud computing platform. The storage component of the platform is used to provide synchronization and communication between processing units. We report the speedups and scaleups of a parallel K-Means algorithm obtained with up to 200 processing units.

Distributed K-Means

Cost Modelization
Let:

- \( N \) be the number of points in \( \mathbb{R}^D \),
- \( D \) be the points dimension,
- \( K \) be the number of clusters,
- \( I \) be the number of iterations,
- \( F \) be the time needed to perform one floating point operation,
- \( B_1 \) be the time needed to read a double from the blobStorage,
- \( B_2 \) be the time needed to write a double into the blobstorage.

In the proposed algorithm, we can roughly model the cost of computation and communication by:

\[
T_{P}^{\text{comp}} = \frac{3NKDF}{P},
\]
\[
T_{P}^{\text{comm}} = 2\sqrt{TKDI}(B_1 + 0.5B_2)
\]

Speedup can therefore be modeled as:

\[
S_P = \frac{T_{P}^{\text{comp}} + T_{P}^{\text{comm}}}{TP^{\text{comp}} + TP^{\text{comm}}} = \frac{3NF}{P}\]

The optimal number of mapper PU is given by \( P^* = (3NF/(B_1 + 0.5B_2))^{1/3} \). For this value of \( P^* \), which depends neither on \( K \) nor on \( D \), the total processing time consists in one third of mapping and two third of reducing. Conversely, for \( N \) sufficient, communication is negligible and one can achieve good speedup.

Communication Tree

The reduce phase is a two-step procedure where all the partial reduce jobs are run in parallel.

Microsoft Azure
Our prototype is build on top of several components that ease access to storage and workers lifecycle management:

- Azure Queues provide a message delivery mechanism through distributed queues. Messages can be returned multiple times, which implies that jobs must be idempotent.
- Azure BlobStorage is a key/value pairs storage system. Workers are stateless: all the intermediate and final results are stored in the BlobStorage.
- Lokad-Cloud framework provides an abstraction layer on storage and workers.

Results
The algorithm has been run on different values of \( N \) and \( P \). We set \( K=1000 \) and \( D=1000 \) in all experiments so latency can be neglected, and experiments were run for 10 iterations to get stable timing estimates.

On the left figure, we fixed \( N \) and plot the speedup curve as a function of \( P \), which is relatively flat in a neighborhood of \( P^* \). But for \( P = P^* \), most of the time is spent in communication, resulting in a rather inefficient worker allocation.

The algorithm has also been run with much more points per mapper (50,000 points per worker on right figure). Loadwork in each worker being much more important, communication becomes small compared to computation, and satisfactory speedups and scaleups can be reached, provided no straggler issues are met.

As shown in right figure, each worker performs computation with very stable timing. But some workers may be slowed-down during a short period of time, as shown in worst cases of left figure. This mechanism slightly affects performance while running 100 workers, but may become very critical while running thousands of machines.

Conclusion
Communication costs induce a potential bound on scaling for cloud applications. As anticipated by the model, communication takes more time than computation while running \( P^* \) mappers. Conversely, heavy workload on each worker leads to very satisfactory speedups.

References
[1] Dhillon, Inderjit S. and Modha, Dharmendra S. A Data-Clustering Algorithm on Distributed Memory Multiprocessors. In Revised Papers from Large-Scale Parallel Data Mining, Workshop on Large-Scale Parallel KDD Systems, SIGKDD

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